

# $K^+K^-\pi^0$ update

# Data and cuts

Dataset:

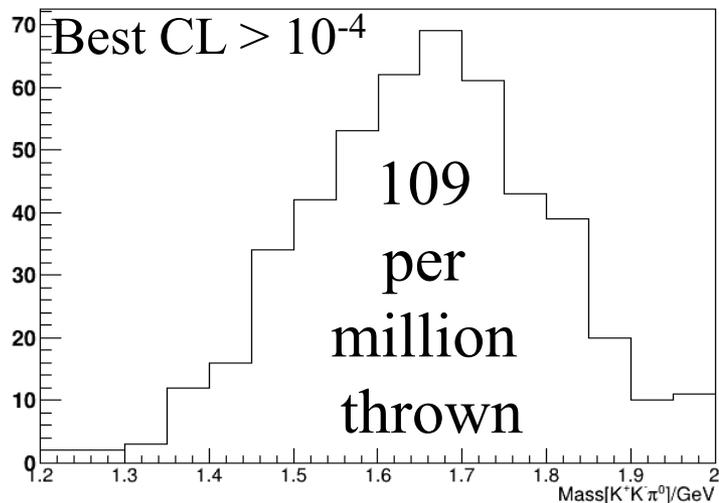
- Spring 2018 data

Restrictions:

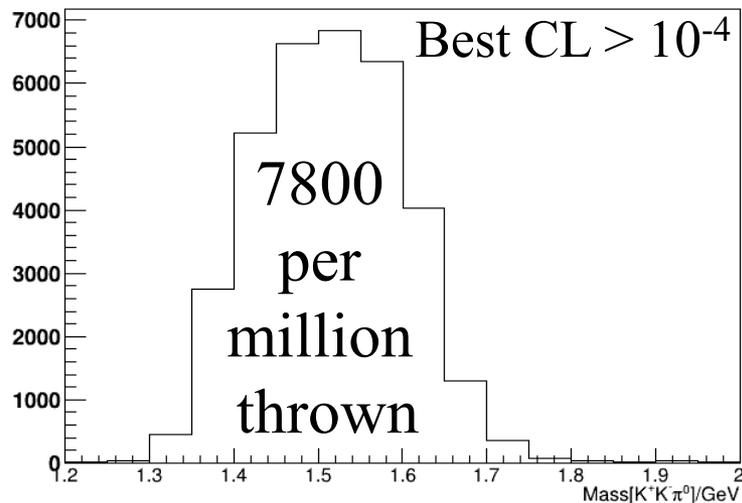
- Incident photon timed to be within central peak
- Only best Confidence Level ( $CL$ ) per event kept
- $CL$  must be above  $10^{-4}$
- Kaons must be forward directed (seen in TOF)
- Kaons must have momentum  $< 3$  GeV
- Missing mass within 3 standard deviations of central peak
- $0.12 \text{ GeV} < \text{Mass}[\pi^0] < 0.15 \text{ GeV}$

# Contamination study (4.4 million thrown)

$\pi^+\pi^-\pi^0$  seen as  $K^+K^-\pi^0$

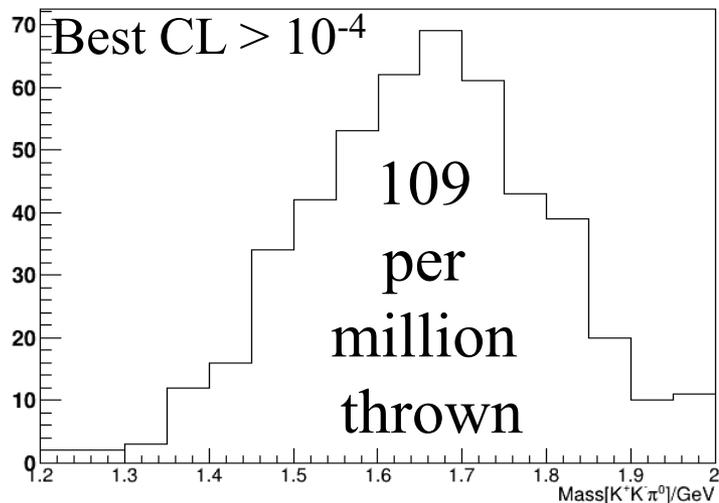


$K^+\pi^-\pi^0$  seen as  $K^+K^-\pi^0$

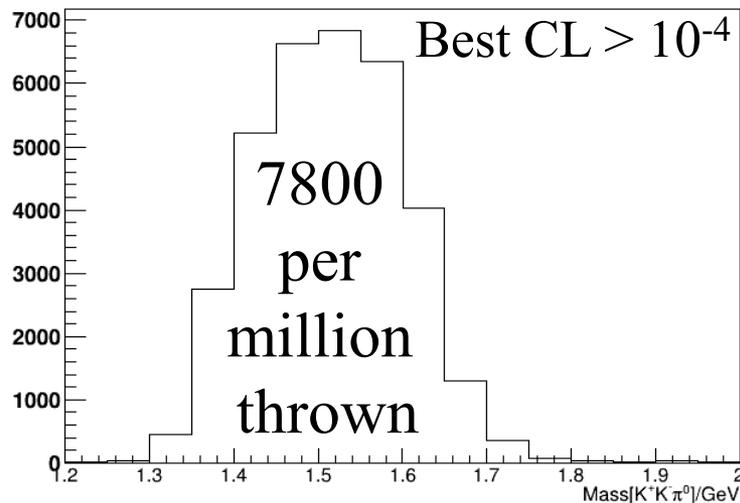


# Contamination study (4.4 million thrown)

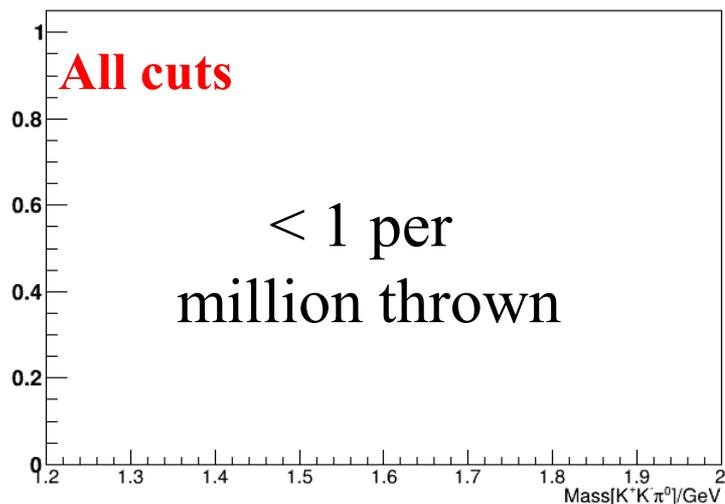
$\pi^+\pi^-\pi^0$  seen as  $K^+K^-\pi^0$



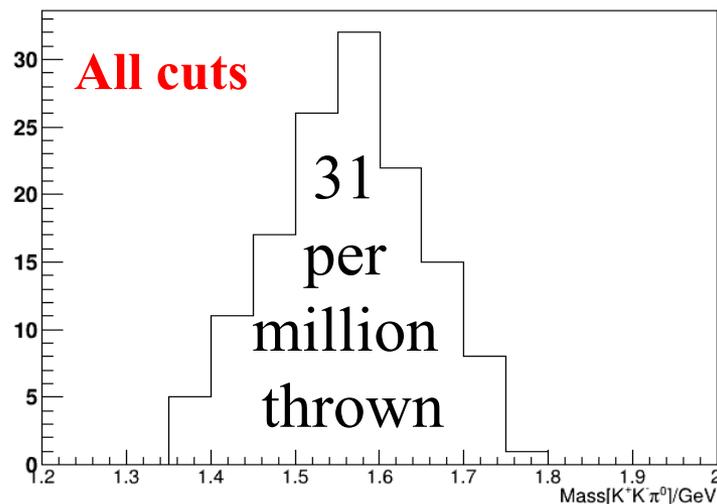
$K^+\pi^-\pi^0$  seen as  $K^+K^-\pi^0$



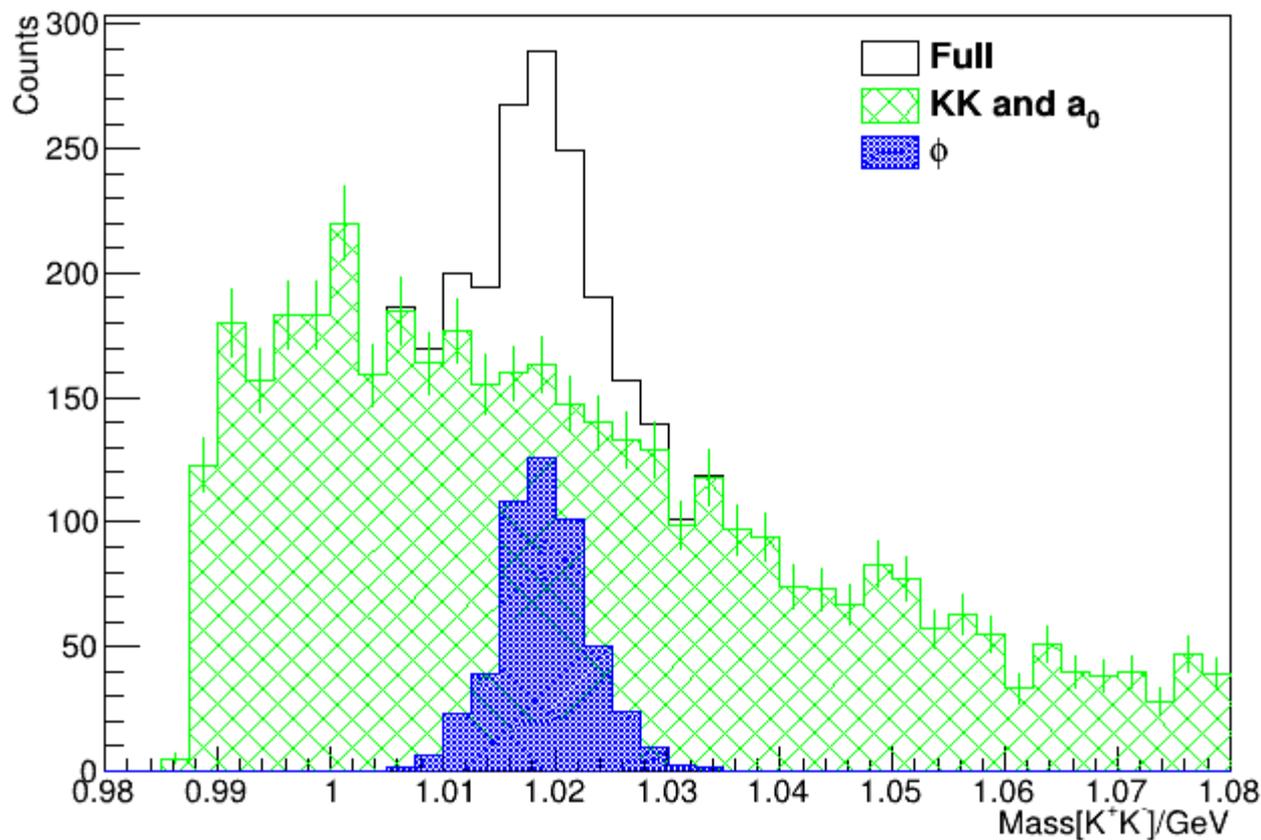
$\pi^+\pi^-\pi^0$  seen as  $K^+K^-\pi^0$



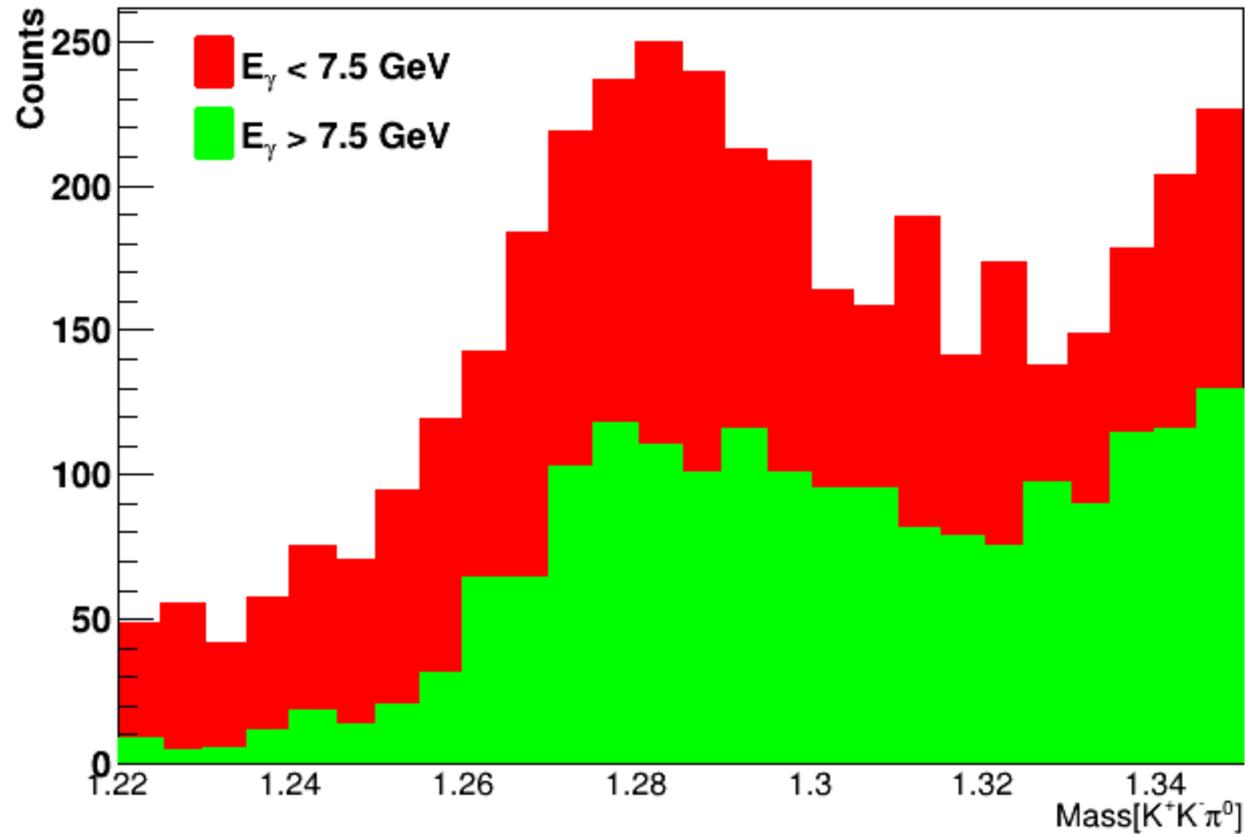
$K^+\pi^-\pi^0$  seen as  $K^+K^-\pi^0$



# $Q$ -factors to separate $\phi\pi$ from $K^+K^-\pi^0$ and $a_0\pi^0$ events

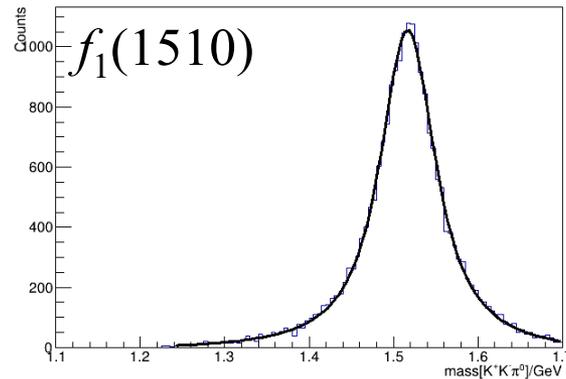
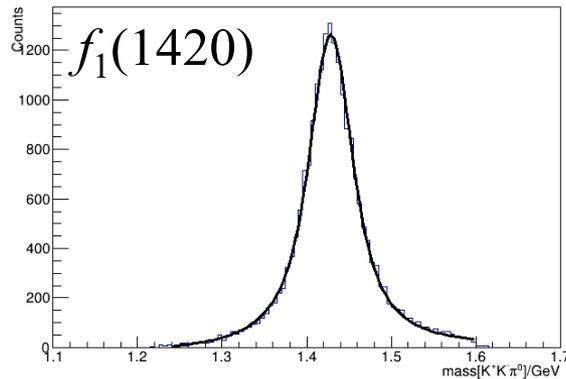
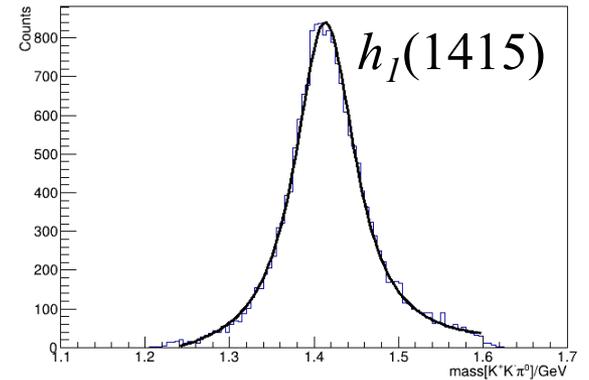
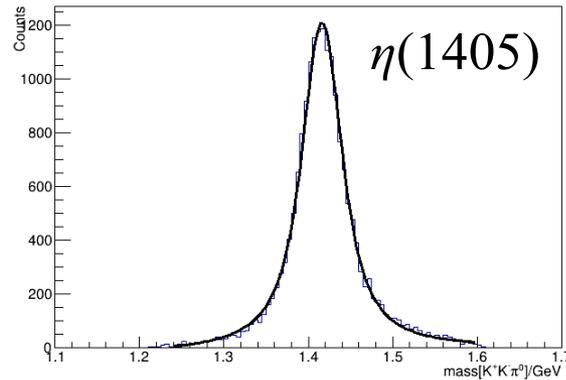
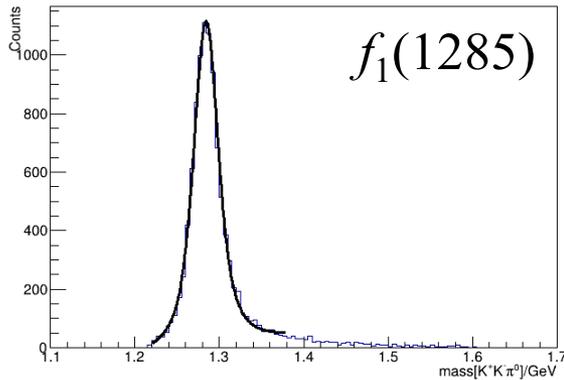


# Additional $E_\gamma$ cut



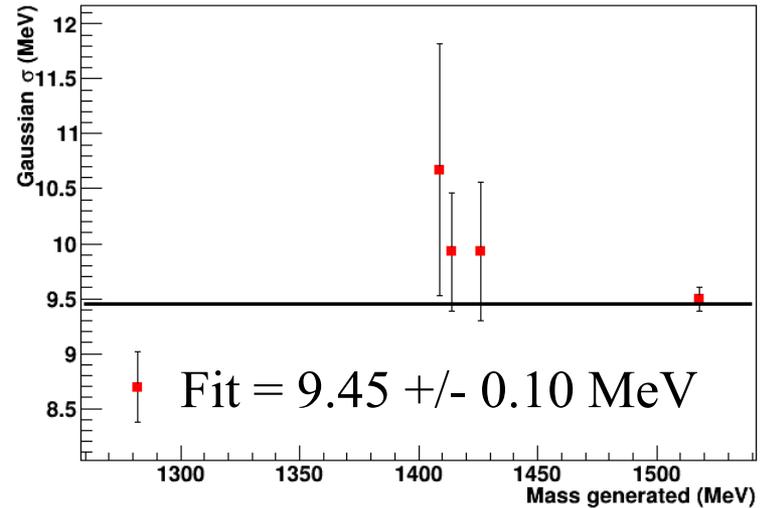
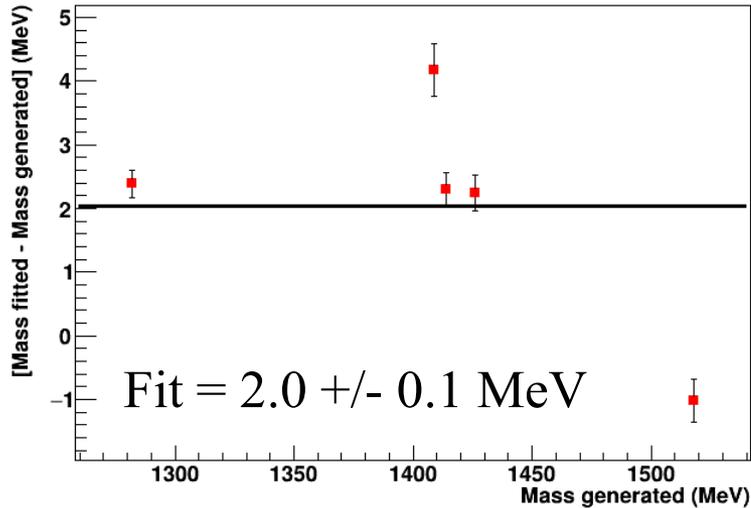
For now, only using events with  $E_\gamma$  below 7.5 GeV

# Monte Carlo peak fits



- Each mass spectrum was fit to voigtian line shape

# Results of Monte Carlo peak fits



- Reconstructed masses are systematically high by about 2 MeV
- Gaussian broadening ( $\sigma$ ) of Voigtian line shape is about 9.45 MeV

# Intensity (Justin Stevens)

$$I(\Phi, \Omega, \Omega_H) = 2\kappa \sum_k \left\{ (1 - P_\gamma) \left[ \left| \sum_{i_N, m} [J_i^N]_{m, k}^{(+)} \text{Im}(Z) + \sum_{i_U, m} [J_i^U]_{m, k}^{(-)} \text{Im}(Z) \right|^2 + \left| \sum_{i_N, m} [J_i^N]_{m, k}^{(-)} \text{Re}(Z) + \sum_{i_U, m} [J_i^U]_{m, k}^{(+)} \text{Re}(Z) \right|^2 \right] + (1 + P_\gamma) \left[ \left| \sum_{i_N, m} [J_i^N]_{m, k}^{(-)} \text{Im}(Z) + \sum_{i_U, m} [J_i^U]_{m, k}^{(+)} \text{Im}(Z) \right|^2 + \left| \sum_{i_N, m} [J_i^N]_{m, k}^{(+)} \text{Re}(Z) + \sum_{i_U, m} [J_i^U]_{m, k}^{(-)} \text{Re}(Z) \right|^2 \right] \right\}$$

The  $[J_i^{N,U}]_{m,k}^{(\epsilon)}$  are the free complex parameters in the fit for a given reflectivity amplitude.

where  $Z_m^i(\Omega, \Omega_H) = e^{-i\Phi} X_m^i(\Omega, \Omega_H)$  is the phase-rotated decay amplitude and  $\Phi$  is the angle between the production plane and the photon polarization

$K^+K^-\pi^0$  update

$a_0(980)$  mass parameterization

# $a_0(980)$

Using  $a_0(980)$  isobar as parameterized by BESIII:

The ordinary intermediate resonance is parametrized by a relativistic Breit-Wigner (BW) propagator with a constant-width

$$BW(s) = \frac{1}{M^2 - s - iM\Gamma}, \quad (4.2)$$

where  $s$  is the invariant mass squared of resonances,  $M$  and  $\Gamma$  are the corresponding mass and width. For  $a_0(980)^0$  with mass near  $K\bar{K}$  threshold, we use dispersion integrals to describe its lineshape

# $a_0(980)$

The  $a_0(980)$  amplitude is constructed using the following denominator:

$$D_\alpha(s) = m_0^2 - s - \sum_{ch} \Pi_{ch}(s), \quad (4)$$

where  $m_0$  is the  $a_0(980)$  mass and  $\Pi_{ch}(s)$  in the sum over channels is a complex function, with imaginary part

$$\text{Im}\Pi_{ch}(s) = g_{ch}^2 \rho_{ch}(s) F_{ch}(s), \quad (5)$$

while real parts are given by principal value integrals,

$$\text{Re}\Pi_{ch}(s) = \frac{1}{\pi} P \int_{s_{ch}}^{\infty} \frac{\text{Im}\Pi_{ch}(s') ds'}{(s' - s)}. \quad (6)$$

# $a_0(980)$

In the above expressions  $\rho_{ch}(s)$  is the available phase space for a given channel, obtained from the corresponding decay momentum  $q_{ch}(s)$ :  $\rho_{ch}(s) = 2q_{ch}(s)/\sqrt{s}$ . The integral in Eq. (6) is divergent when  $s \rightarrow \infty$ , so the phase space is modified by a form factor  $F_{ch}(s) = e^{-\beta q_{ch}^2(s)}$ , where the parameter  $\beta$  is related to the root-mean-square (rms) size of an emitting source [20]. We use  $\beta = 2.0[\text{GeV}/c^2]^{-2}$  corresponding to  $\text{rms} = 0.68$  fm, and we verify that our results are not sensitive to the value of  $\beta$ . The integration in Eq. (6)

# $a_0(980)$

BESIII

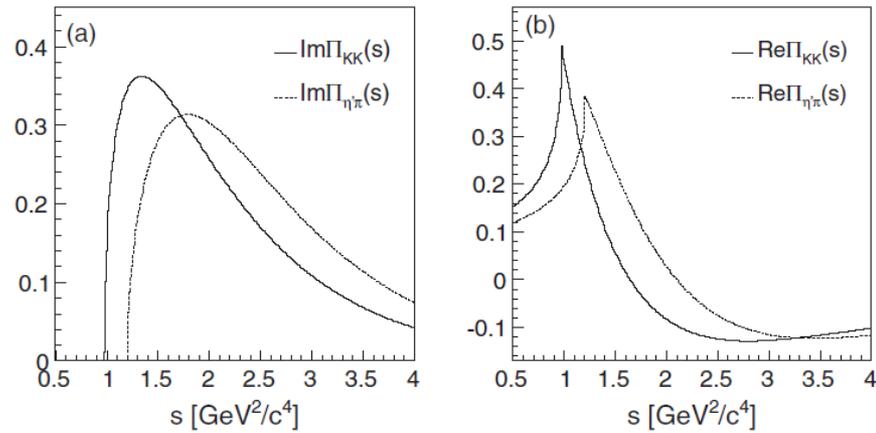
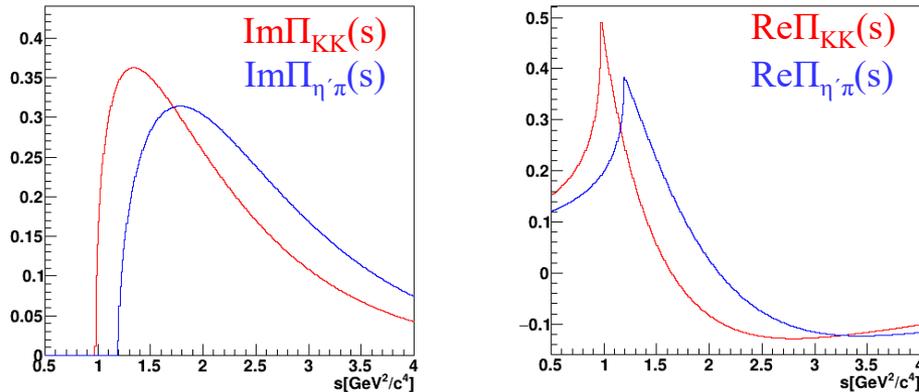


FIG. 4. Line shapes of (a)  $\text{Im}\Pi(s)$  and (b)  $\text{Re}\Pi(s)$  for the  $K\bar{K}$  and  $\eta'\pi$  production with arbitrary normalization.

I used Mathematica to perform the principal value integrals

GlueX



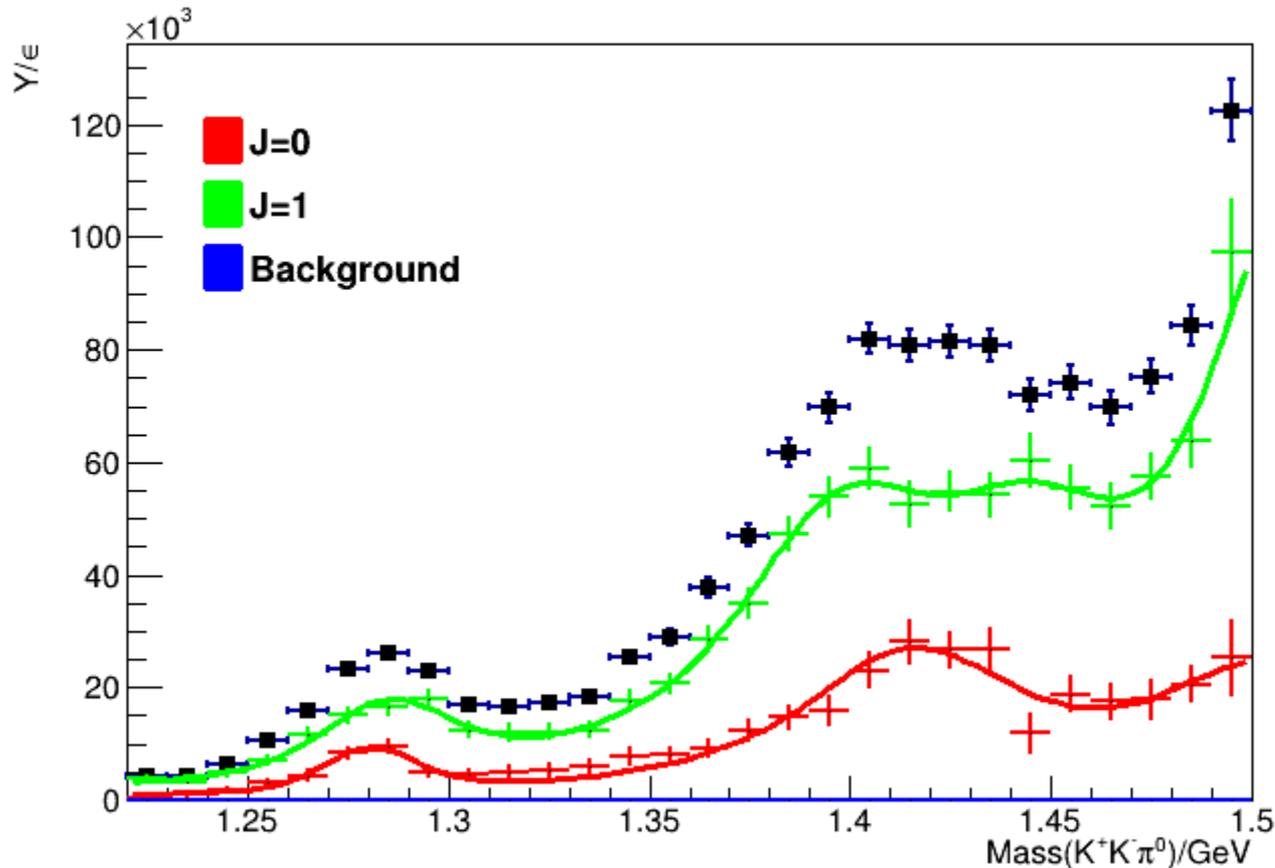
# Isobar fits

# Included waves

- Uniform background
- $J = 0$  :
  - $a_0\pi^0$
  - $K^{*+}K^-$
  - $K^{*-}K^+$
- $J = 1$  :
  - $a_0\pi^0$
  - $K^{*+}K^-$  ( $L=0$ , and  $L=1$ )
  - $K^{*-}K^+$  ( $L=0$ , and  $L=1$ )

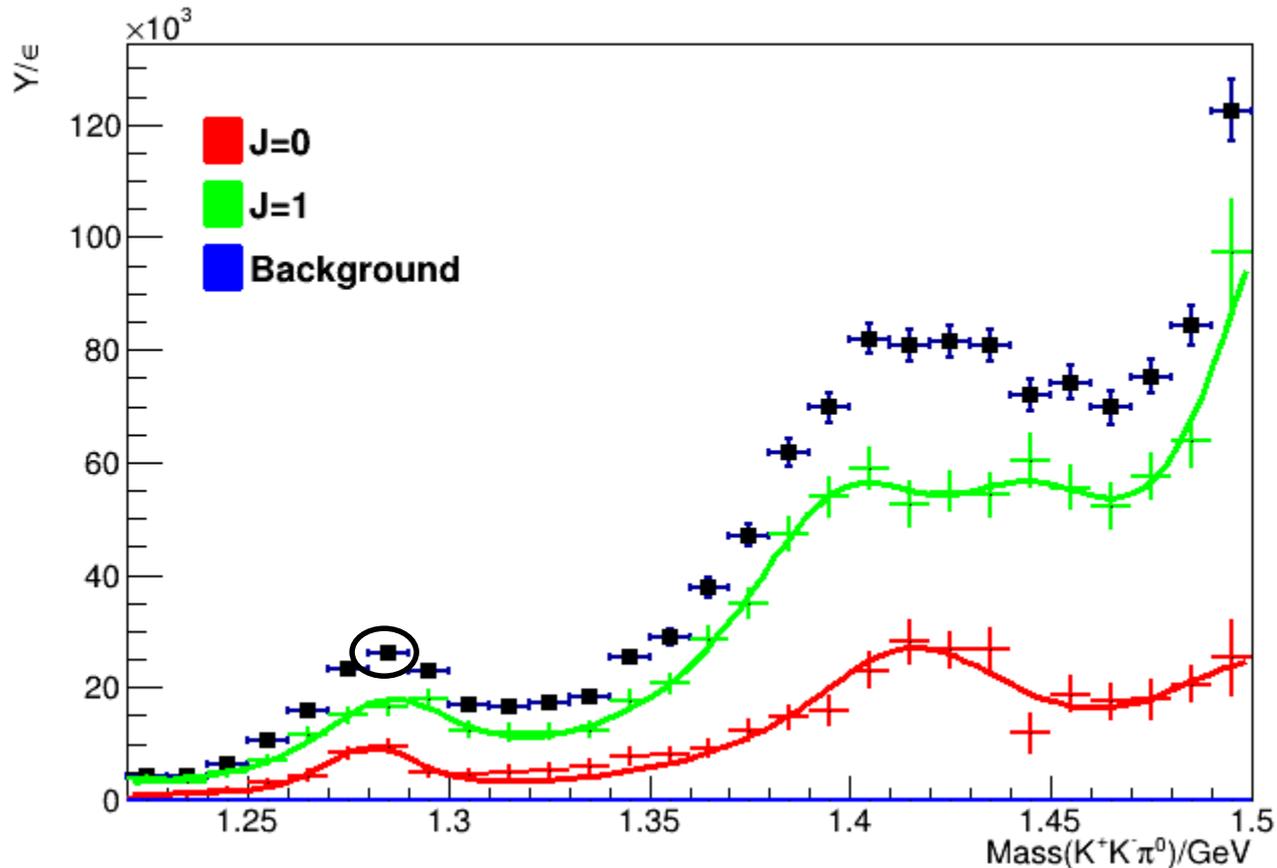
# PWA Results for $J = 0, 1$ and background

## Isobar fit results



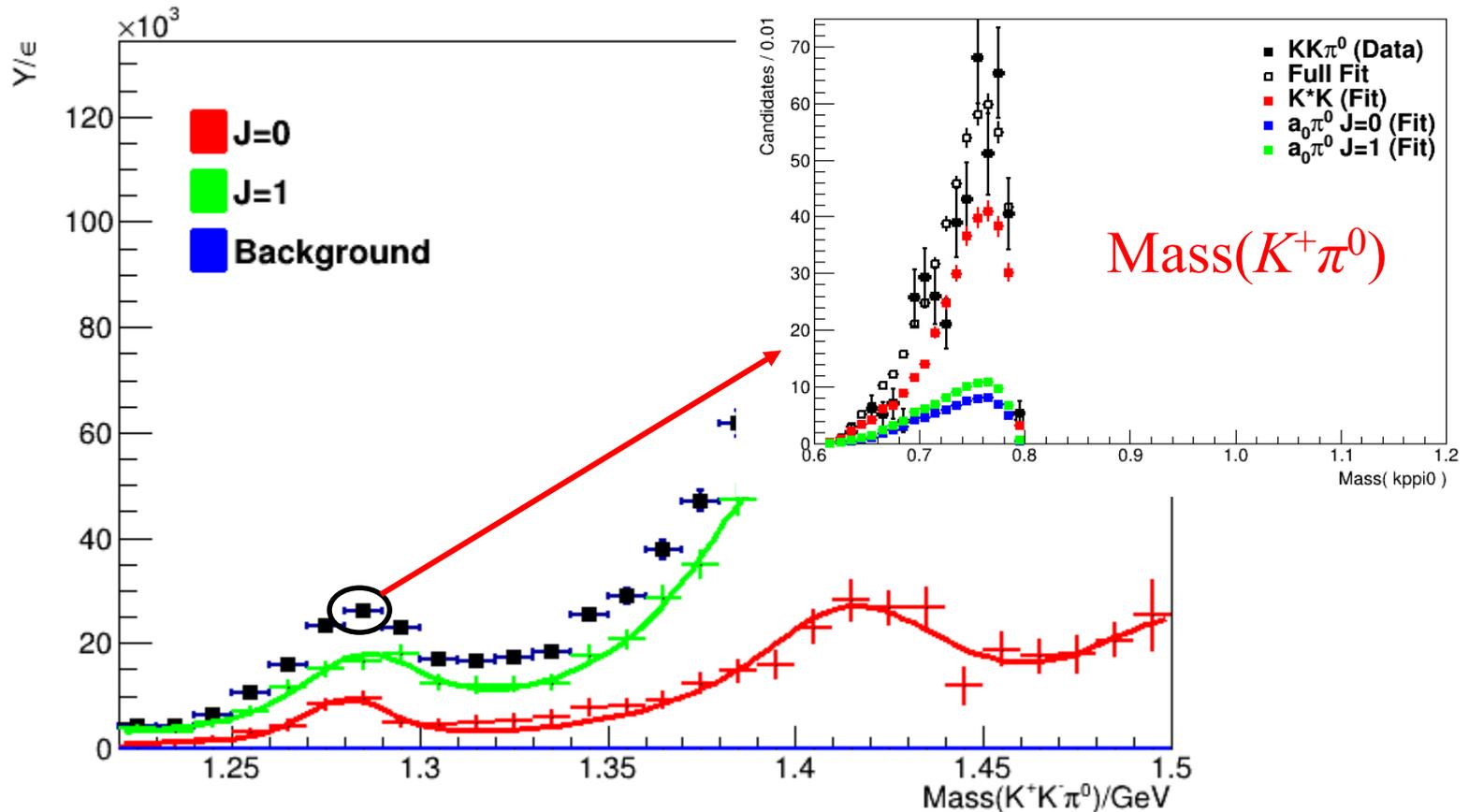
# PWA Results for $J = 0, 1$ and background

## Isobar fit results



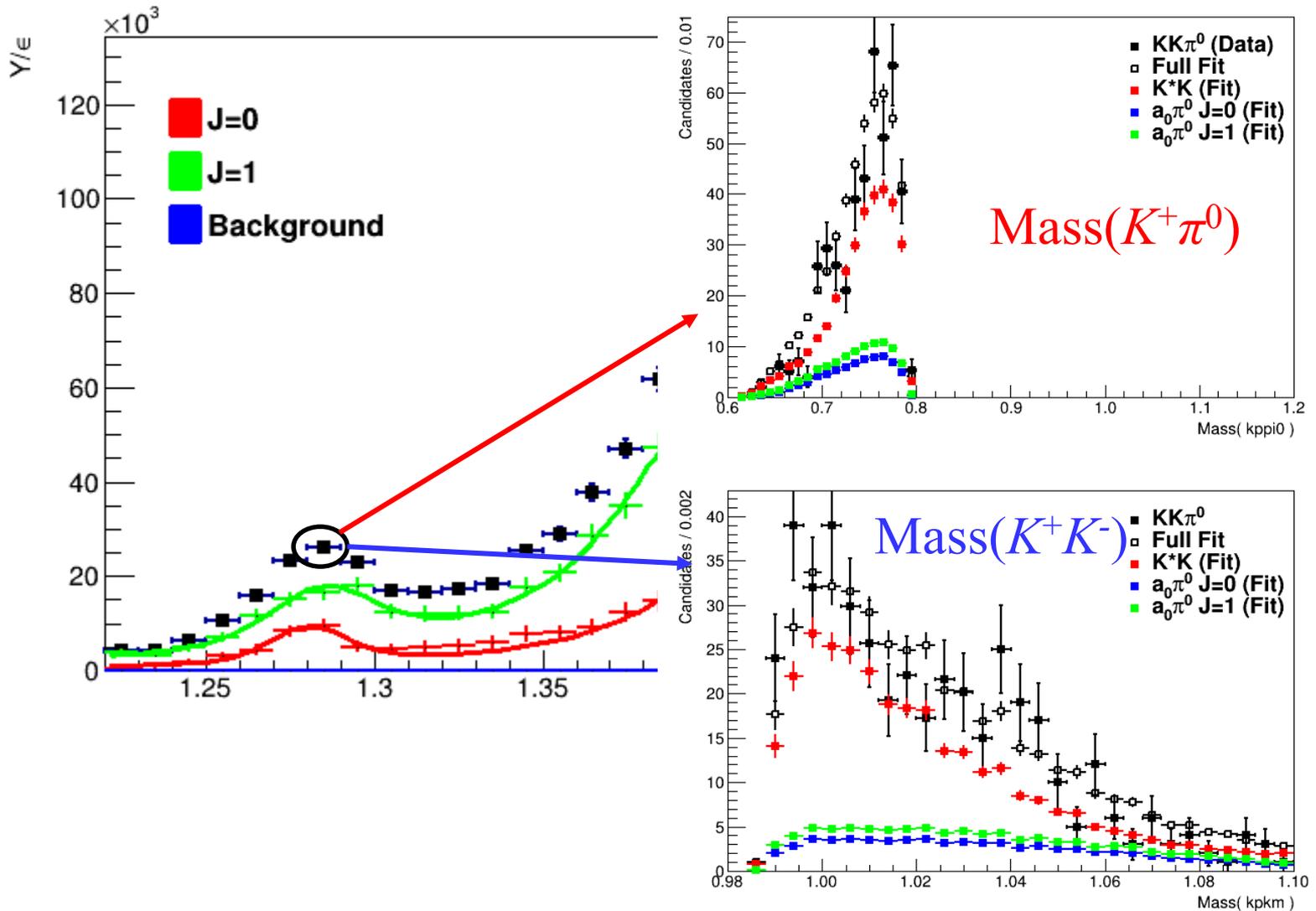
# PWA Results for $J = 0, 1$ and background

## Isobar fit results



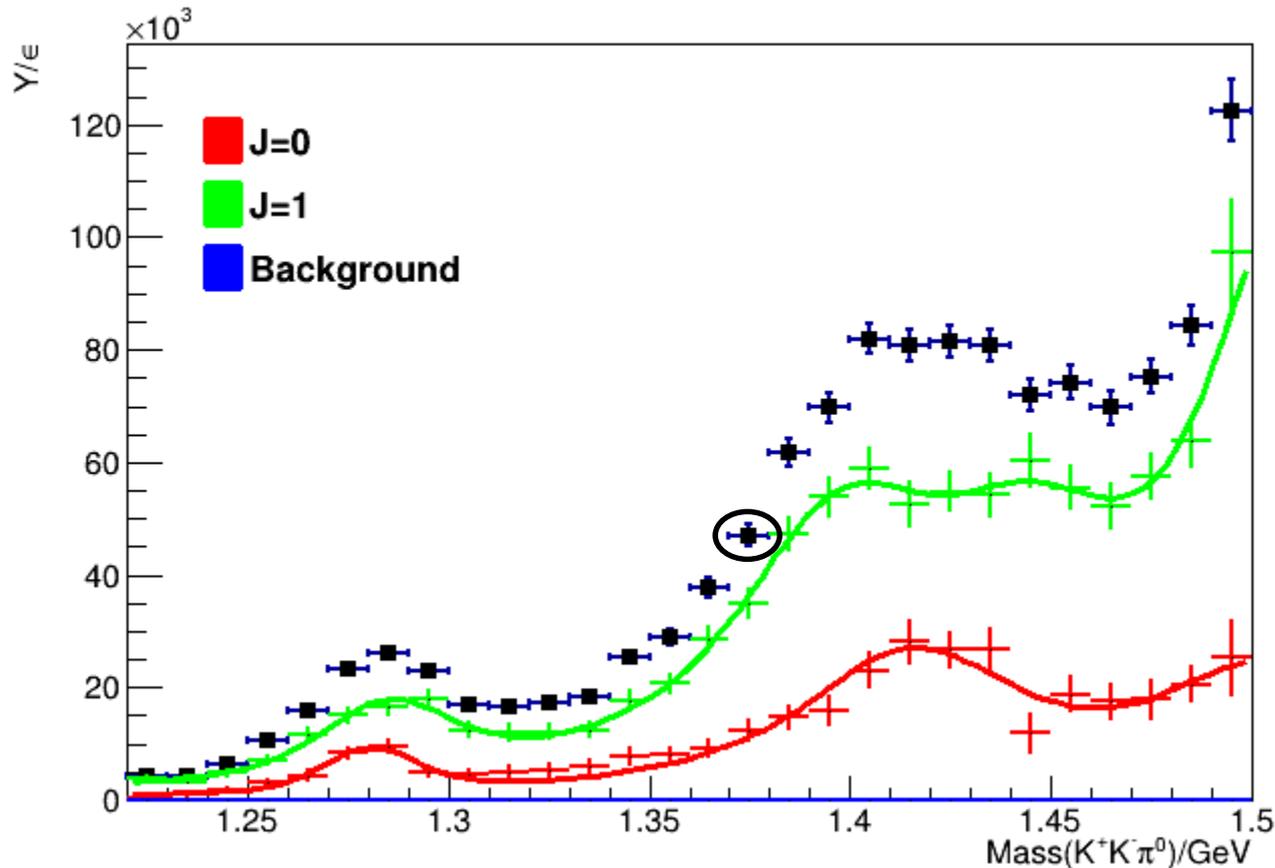
# PWA Results for $J = 0, 1$ and background

## Isobar fit results



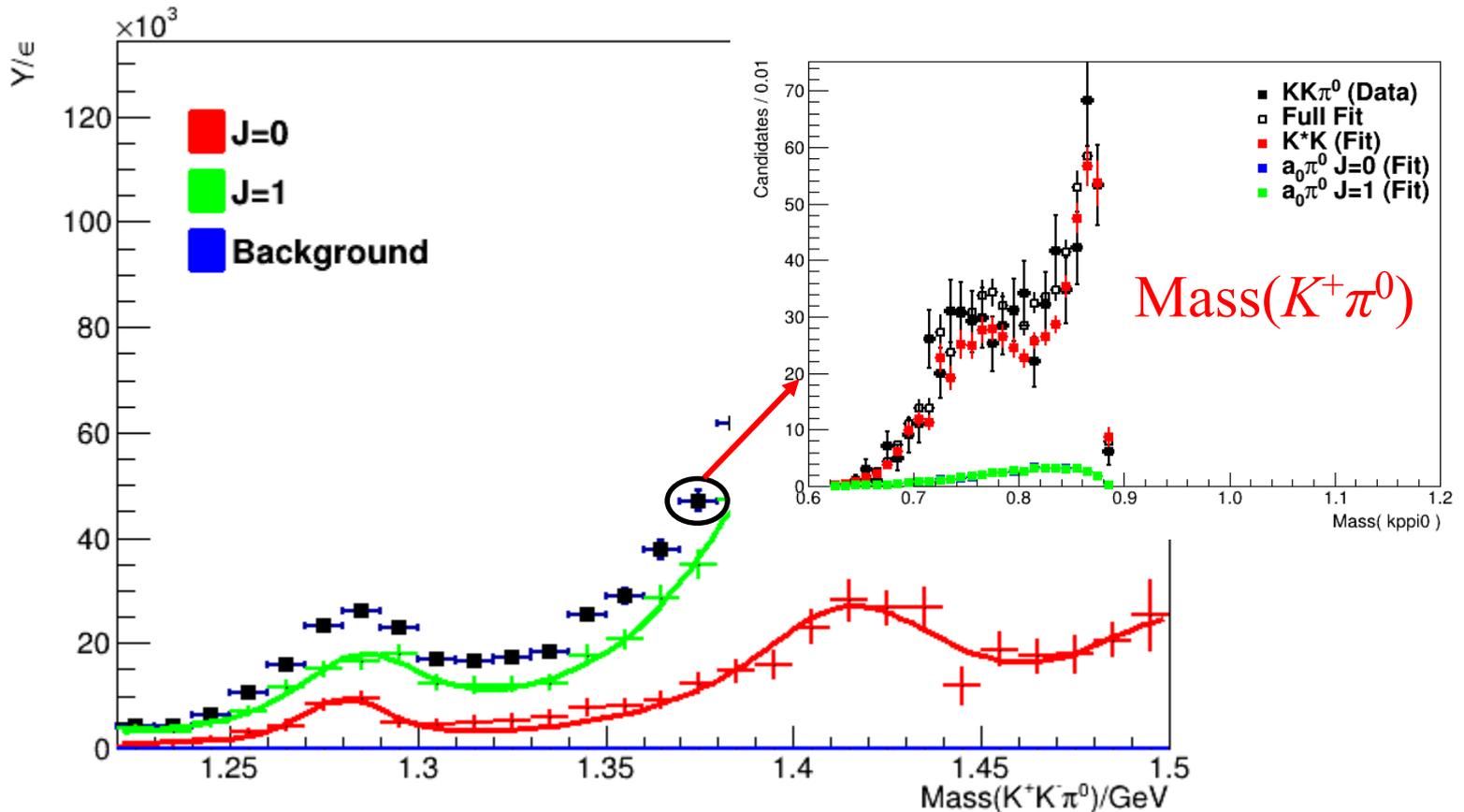
# PWA Results for $J = 0, 1$ and background

## Isobar fit results



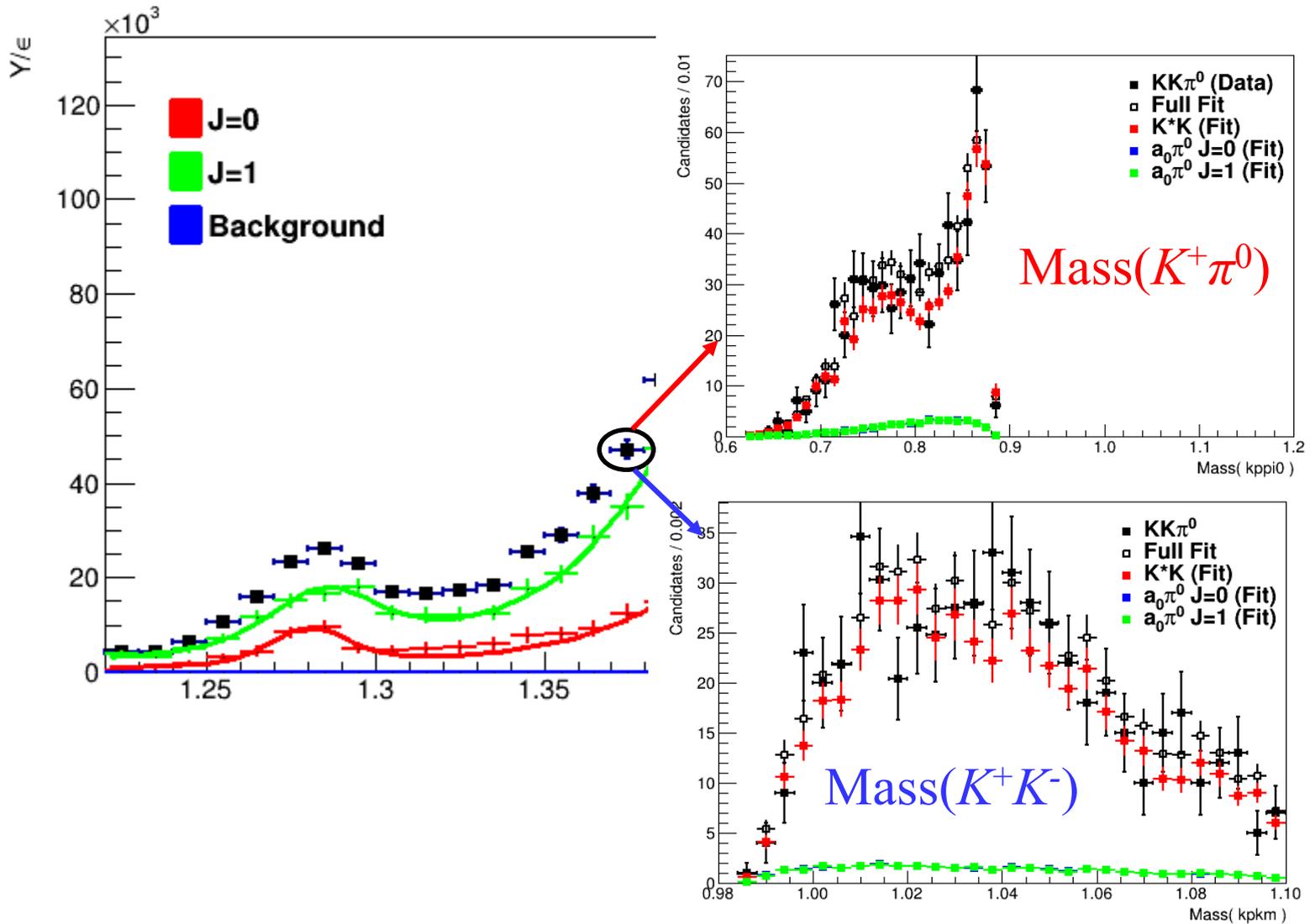
# PWA Results for $J = 0, 1$ and background

## Isobar fit results



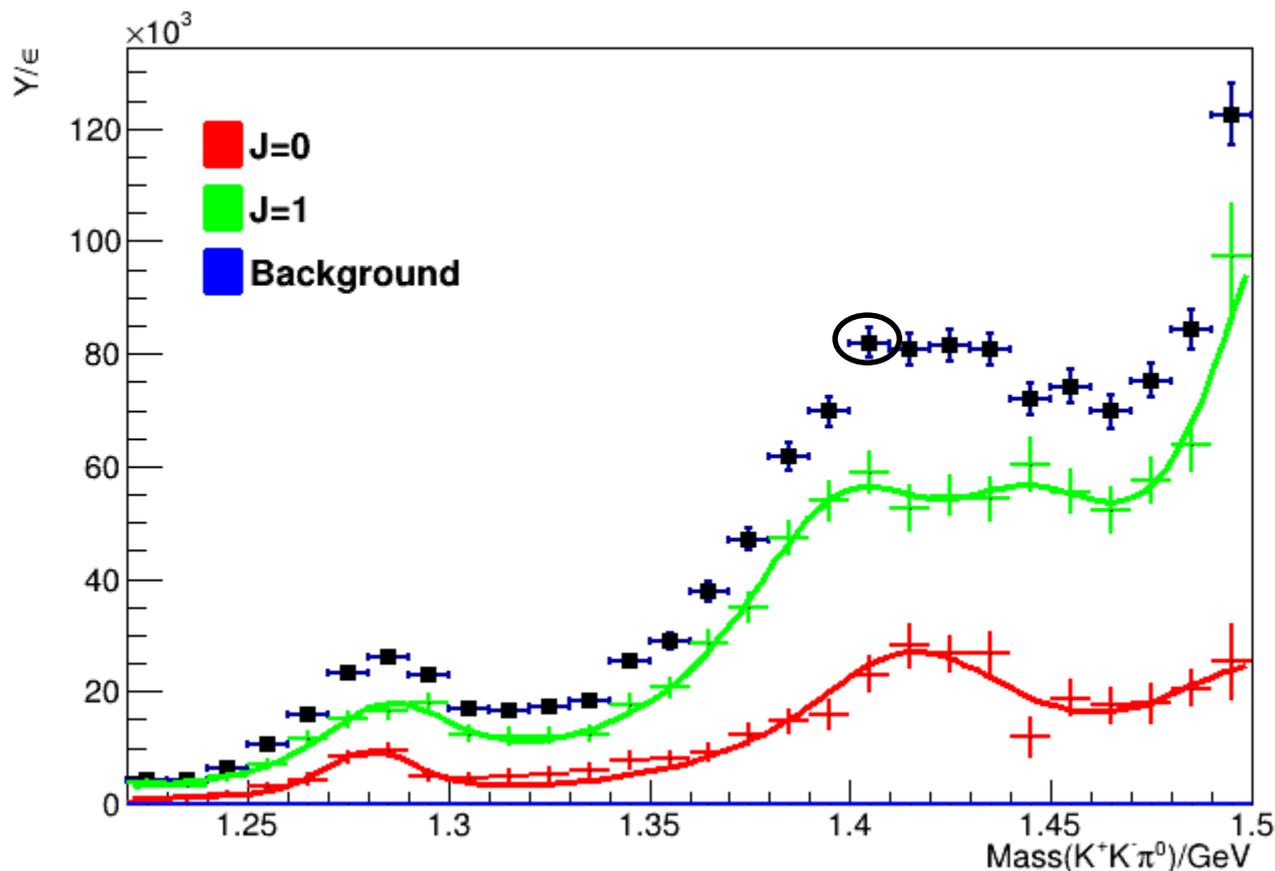
# PWA Results for $J = 0, 1$ and background

## Isobar fit results



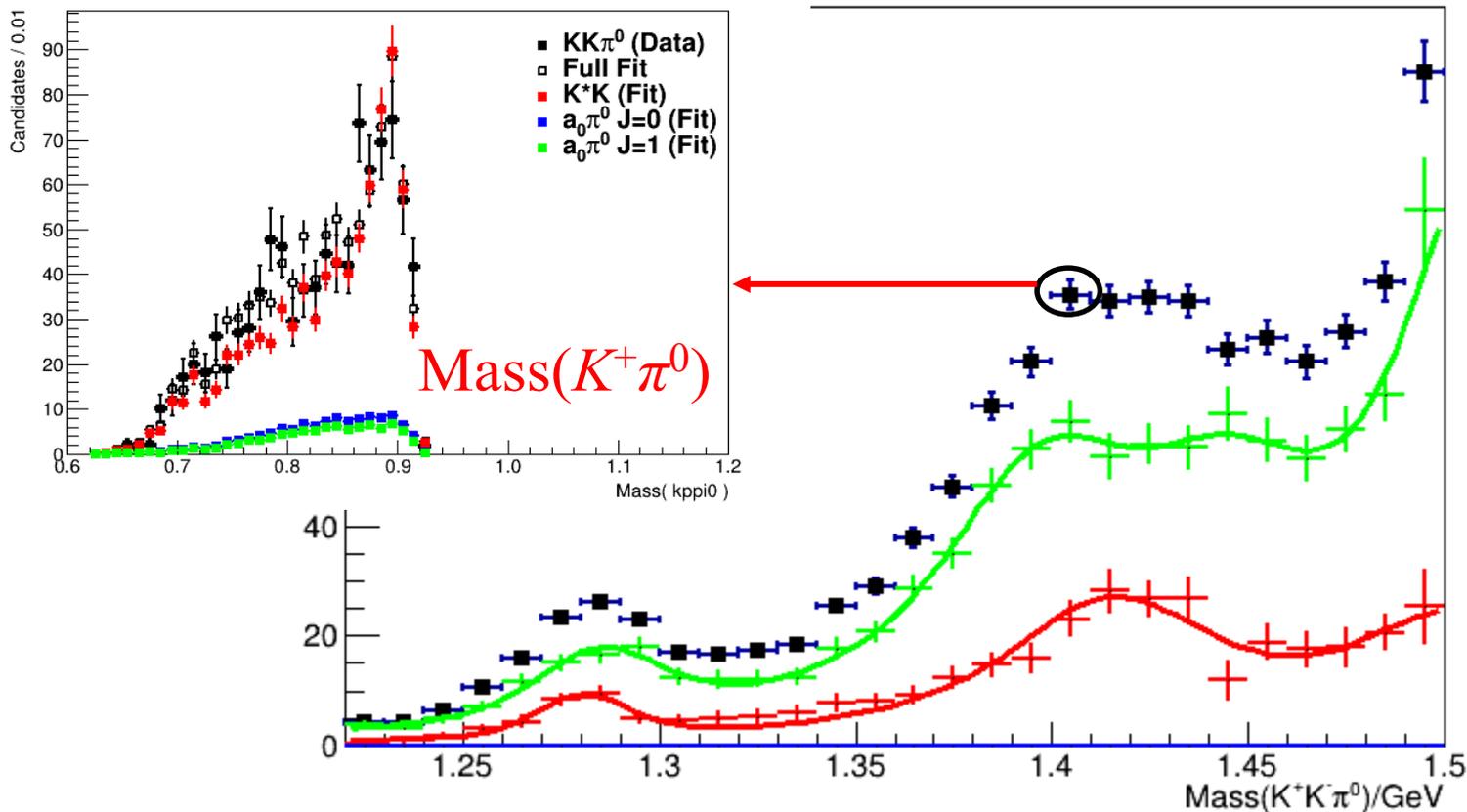
# PWA Results for $J = 0, 1$ and background

## Isobar fit results



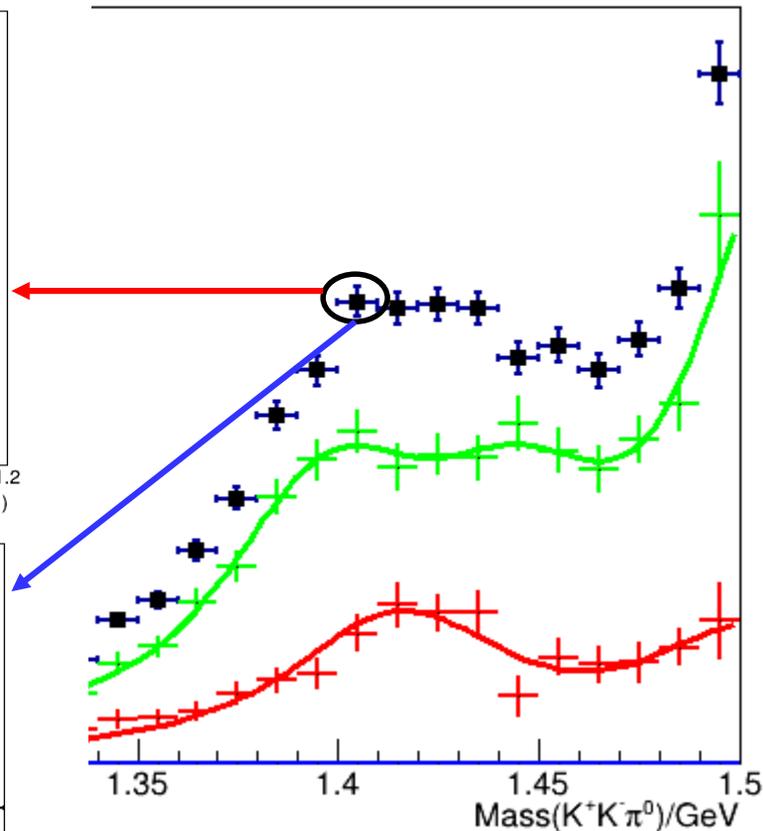
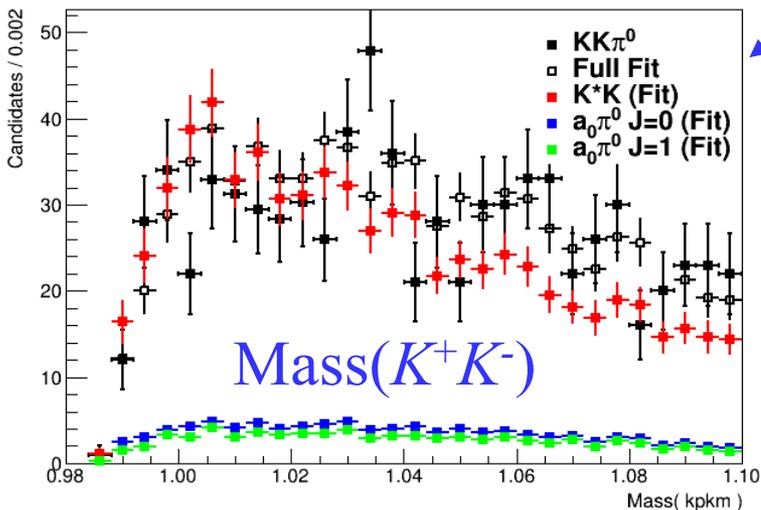
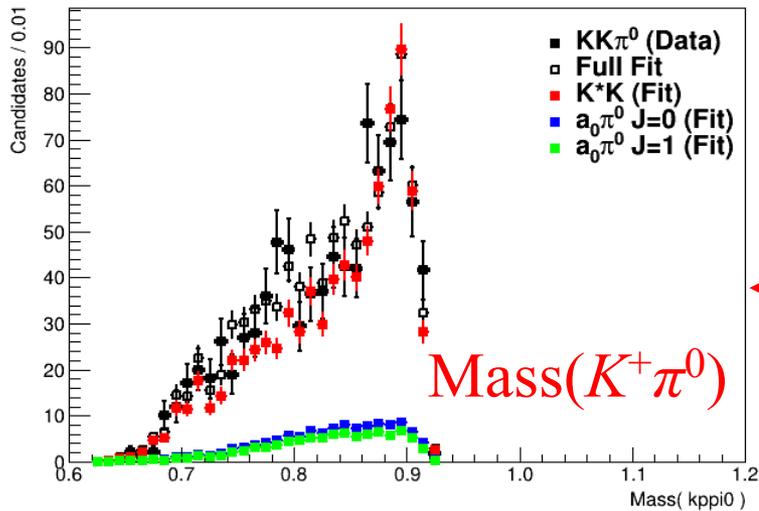
# PWA Results for $J = 0, 1$ and background

## Isobar fit results



# PWA Results for $J = 0, 1$ and background

## Isobar fit results



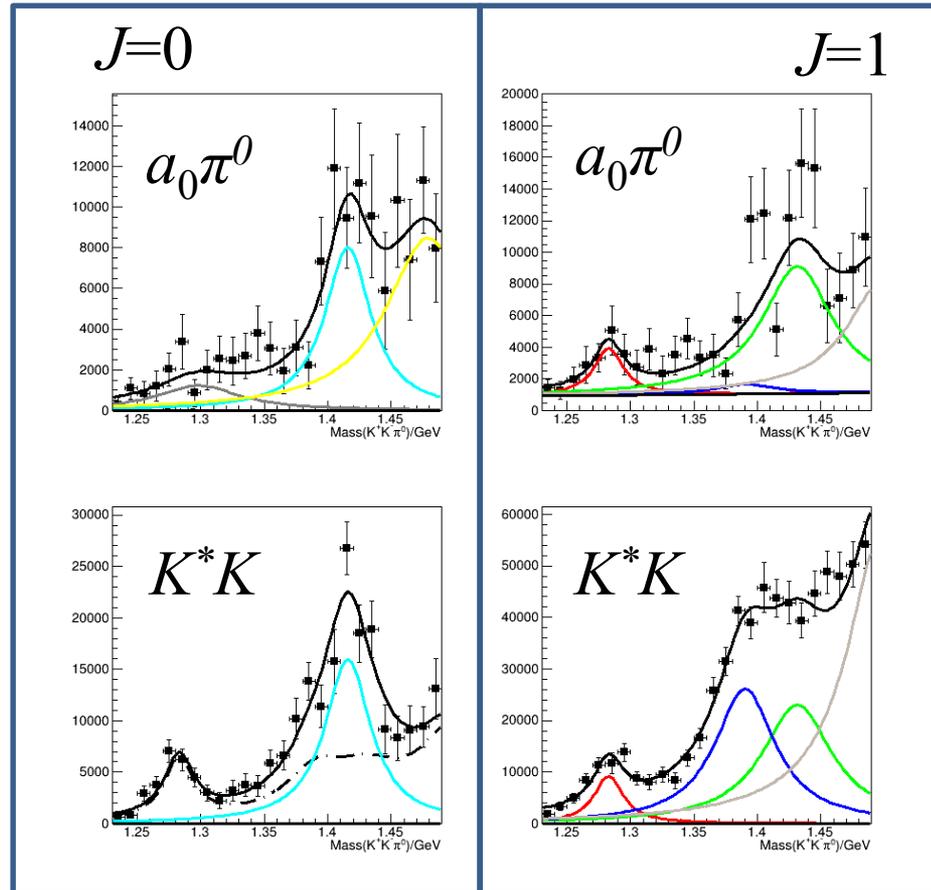
# Simultaneous fit

$J=0$

Gray:  $\eta(1295)$

Cyan:  $\eta(1405)$

Yellow:  $\eta(1475)$



$J=1$

Red:  $f_1(1285)$

Blue:  $h_1(1415)$

Green:  $f_1(1420)$

Brown:  $f_1(1510)$

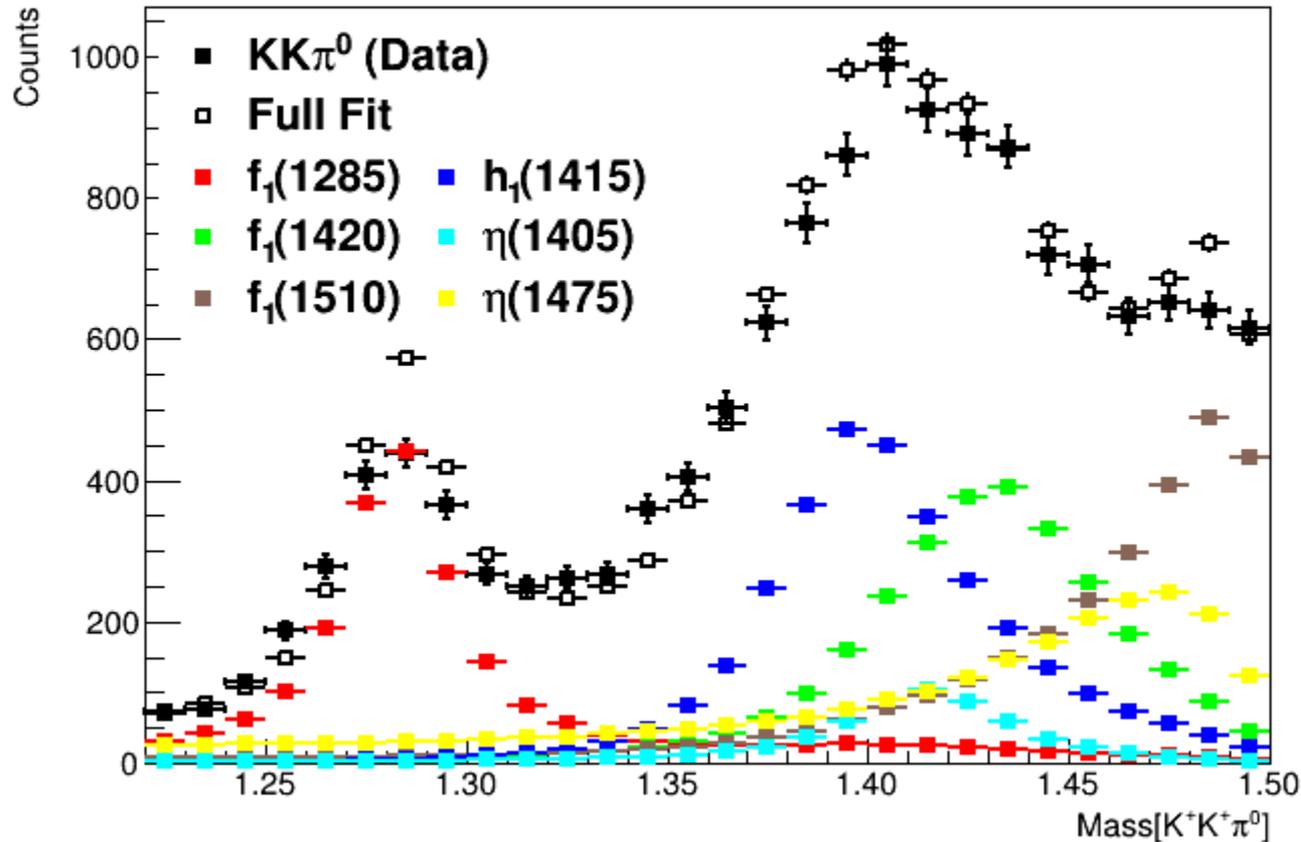
- Dashed-dotted line is estimated leakage of  $J=1$  into  $J=0$
- Used parameters (centers and widths) of Breit-Wigners from the above fit to lock down those parameters for mass-dependent fit

# Leakage study

# Included waves for mass dependent fit

- $J = 0$  :
  - ~~$\eta(1295)$~~  **Not included**
  - $\eta(1405) \rightarrow a_0\pi^0, K^*K$
  - $\eta(1475) \rightarrow a_0\pi^0$
- $J = 1$  :
  - $f_1(1285) \rightarrow a_0\pi^0, K^*K$
  - $h_1(1415) \rightarrow K^*K$  (Note:  $h_1 \rightarrow a_0\pi^0$  not allowed)
  - $f_1(1420) \rightarrow a_0\pi^0, K^*K$
  - $f_1(1510) \rightarrow a_0\pi^0, K^*K$

# PWA mass-dependent fit



- Used fit parameters from above fit to simulate signal using gen\_amp
- Did mass-independent fit using the gen\_amp simulation to help verify leakage assumption

# Included waves for mass dependent fit

- $J = 0$  :
  - ~~$\eta(1295)$~~  **Not included**
  - $\eta(1405) \rightarrow a_0\pi^0, K^*K$  **Branch measured**
  - $\eta(1475) \rightarrow a_0\pi^0$
- $J = 1$  :
  - $f_1(1285) \rightarrow a_0\pi^0, K^*K$  **Branch measured**
  - $h_1(1415) \rightarrow K^*K$  **(Note:  $h_1 \rightarrow a_0\pi^0$  not allowed)**
  - $f_1(1420) \rightarrow a_0\pi^0, K^*K$  **Branch measured**
  - $f_1(1510) \rightarrow a_0\pi^0, K^*K$

# Included waves for mass dependent fit

- $J = 0$  :
    - ~~$\eta(1295)$~~  **Not included**
    - $\eta(1405) \rightarrow a_0\pi^0, K^*K$  Branch measured
    - $\eta(1475) \rightarrow a_0\pi^0$
  - $J = 1$  :
    - $f_1(1285) \rightarrow a_0\pi^0, K^*K$  Branch measured
    - $h_1(1415) \rightarrow K^*K$  (Note:  $h_1 \rightarrow a_0\pi^0$  not allowed)
    - $f_1(1420) \rightarrow a_0\pi^0, K^*K$  Branch measured
    - $f_1(1510) \rightarrow a_0\pi^0, K^*K$
- No PDG branch, just generic  $KK\pi$**
- 

# Included waves for mass dependent fit

- $J = 0$  :
    - ~~$\eta(1295)$~~  **Not included**
    - $\eta(1405) \rightarrow a_0\pi^0, K^*K$  Branch measured
    - $\eta(1475) \rightarrow a_0\pi^0$
  - $J = 1$  :
    - $f_1(1285) \rightarrow a_0\pi^0, K^*K$  Branch measured
    - $h_1(1415) \rightarrow K^*K$  (Note:  $h_1 \rightarrow a_0\pi^0$  not allowed)
    - $f_1(1420) \rightarrow a_0\pi^0, K^*K$  Branch measured
    - $f_1(1510) \rightarrow a_0\pi^0, K^*K$
- No PDG branch, just generic  $KK\pi$**
- Peak outside of fit region**

# Included waves for mass dependent fit

- $J = 0$  :

- ~~$\eta(1295)$~~  **Not included**

- $\eta(1405) \rightarrow a_0\pi^0, K^*K$  **Branch measured**

- $\eta(1475) \rightarrow a_0\pi^0$

- $J = 1$  :

- $f_1(1285) \rightarrow a_0\pi^0, K^*K$  **Branch measured**

- $h_1(1415) \rightarrow K^*K$  **(Note:  $h_1 \rightarrow a_0\pi^0$  not allowed)**

- $f_1(1420) \rightarrow a_0\pi^0, K^*K$  **Branch measured**

- $f_1(1510) \rightarrow a_0\pi^0, K^*K$

**Compared  
to PDG**

## $\eta(1405)$ BRANCHING RATIOS

$\Gamma(a_0(980)\pi)/\Gamma(KK\pi)$

$\Gamma_3/\Gamma_1$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
• • •				We do not use the following data for averages, fits, limits, etc. • • •
~ 0.15		<sup>1</sup> BERTIN	95	OBLX $0 \bar{p}p \rightarrow K\bar{K}\pi\pi\pi$
~ 0.8	500	<sup>1</sup> DUCH	89	ASTE $\bar{p}p \rightarrow \pi^+\pi^-K^\pm\pi^\mp K^0$
~ 0.75		<sup>1</sup> REEVES	86	SPEC $6.6 \rho\bar{p} \rightarrow KK\pi X$

<sup>1</sup> Assuming that the  $a_0(980)$  decays only into  $K\bar{K}$ .

**Measured for charged kaons:**

$$\Gamma(a_0\pi^0/KK\pi^0) = 0.59 \pm 0.13$$

## $\eta(1405)$ BRANCHING RATIOS

$\Gamma(a_0(980)\pi)/\Gamma(KK\pi)$					$\Gamma_3/\Gamma_1$
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	

• • • We do not use the following data for averages, fits, limits, etc. • • •

$\sim 0.15$		<sup>1</sup> BERTIN	95	OBLX	$0 \bar{p}p \rightarrow K\bar{K}\pi\pi\pi$
$\sim 0.8$	500	<sup>1</sup> DUCH	89	ASTE	$\bar{p}p \rightarrow \pi^+\pi^-K^\pm\pi^\mp K^0$
$\sim 0.75$		<sup>1</sup> REEVES	86	SPEC	$6.6 p\bar{p} \rightarrow KK\pi X$

<sup>1</sup> Assuming that the  $a_0(980)$  decays only into  $K\bar{K}$ .

Measured for charged kaons:  
 $\Gamma(a_0\pi^0/KK\pi^0) = 0.59 \pm 0.13$

## $f_1(1420)$ BRANCHING RATIOS

$\Gamma(K\bar{K}^*(892)+c.c.)/\Gamma(K\bar{K}\pi)$					$\Gamma_2/\Gamma_1$
VALUE		DOCUMENT ID	TECN	COMMENT	

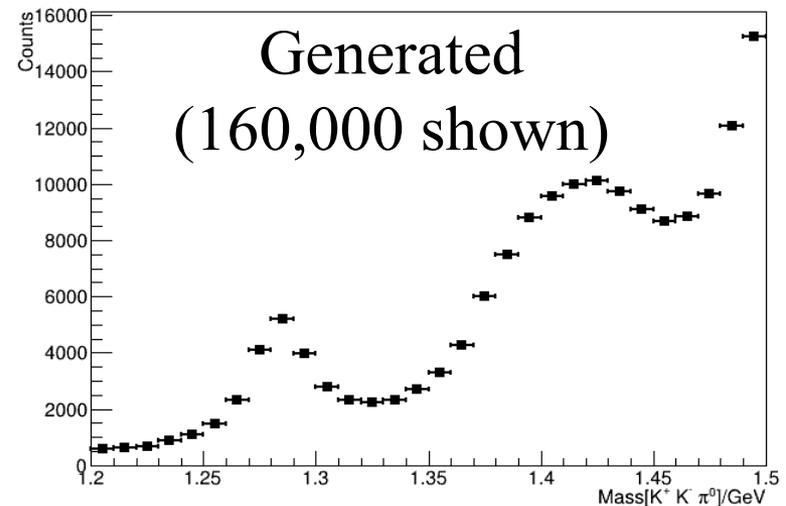
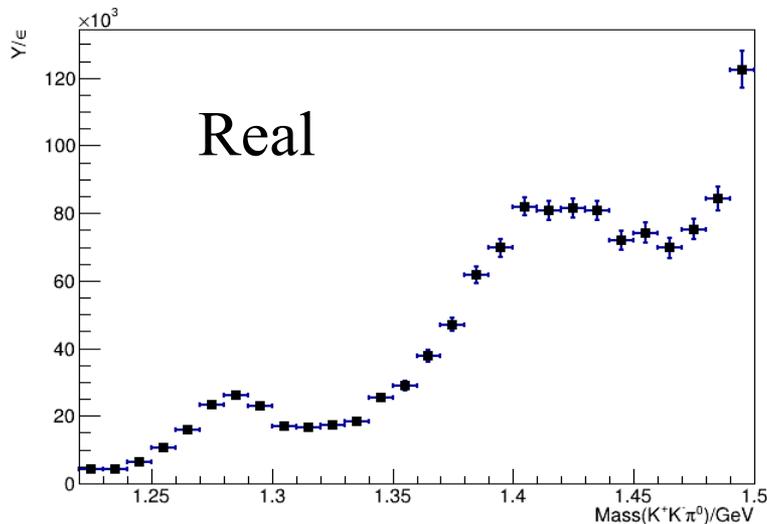
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$0.76 \pm 0.06$		BROMBERG	80	SPEC	$100 \pi^- p \rightarrow K\bar{K}\pi X$
$0.86 \pm 0.12$		DIONISI	80	HBC	$4 \pi^- p \rightarrow K\bar{K}\pi n$

Measured for charged kaons:  
 $\Gamma(K^*K/KK\pi^0) = 0.87 \pm 0.08$

# Comparison of Mass[ $K^+K^-\pi^0$ ] between efficiency corrected real data and generated (gen\_amp)

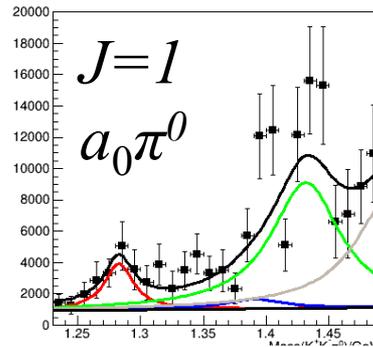
# Comparison of Mass[ $K^+K^-\pi^0$ ] between efficiency corrected real data and generated (gen\_amp)



- Integral of efficiency corrected real data = 1.3 million
- More than enough generated data pushed through glueX simulation
- Next step was : PWA of the gen\_amp data as though it was real

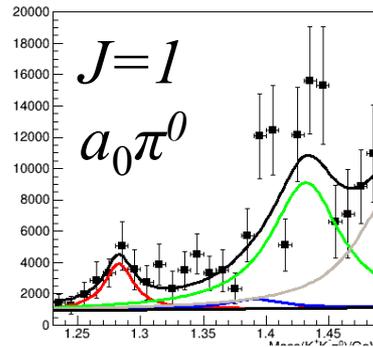
# Comparison of Real to Fake: Mass[ $K^+K^-\pi^0$ ]

**REAL**

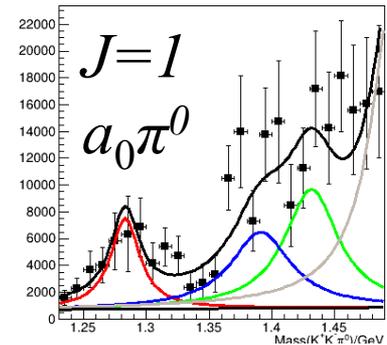


# Comparison of Real to Fake: Mass[ $K^+K^-\pi^0$ ]

**REAL**



**FAKE**

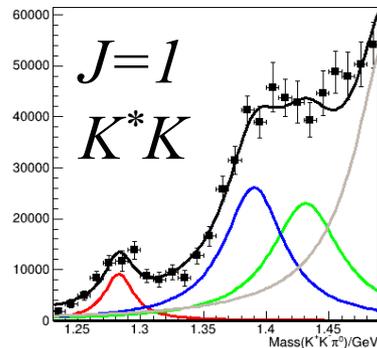
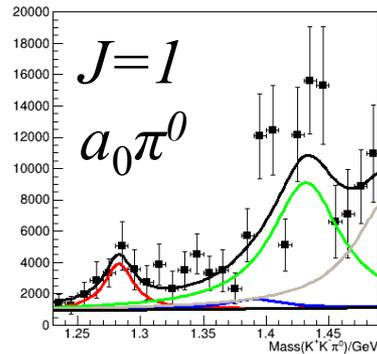


Note:

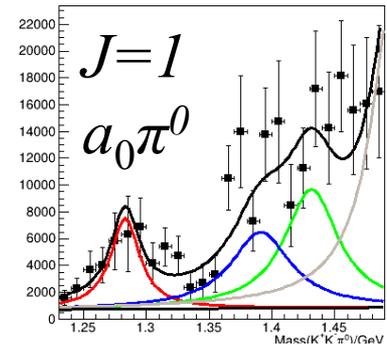
- $h_1 \rightarrow a_0\pi^0$  (**Blue**) was not generated

# Comparison of Real to Fake: Mass[ $K^+K^-\pi^0$ ]

**REAL**



**FAKE**

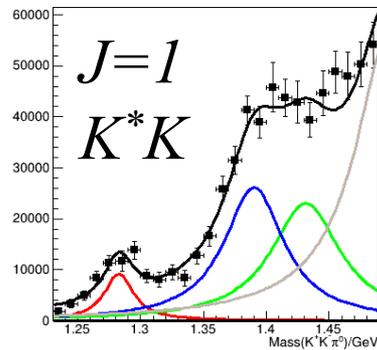
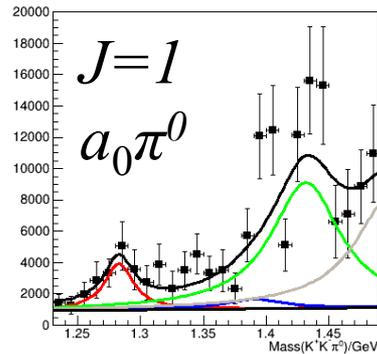


Note:

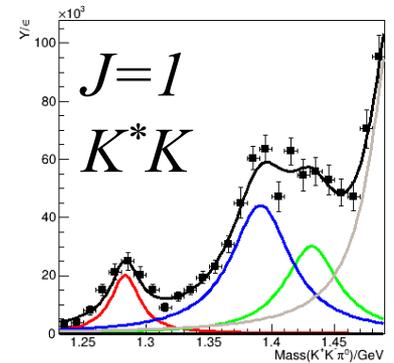
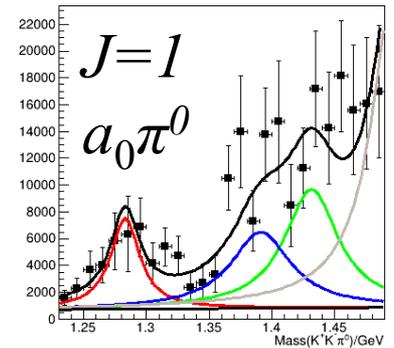
- $h_1 \rightarrow a_0\pi^0$  (**Blue**) was not generated

# Comparison of Real to Fake: Mass[ $K^+K^-\pi^0$ ]

**REAL**



**FAKE**

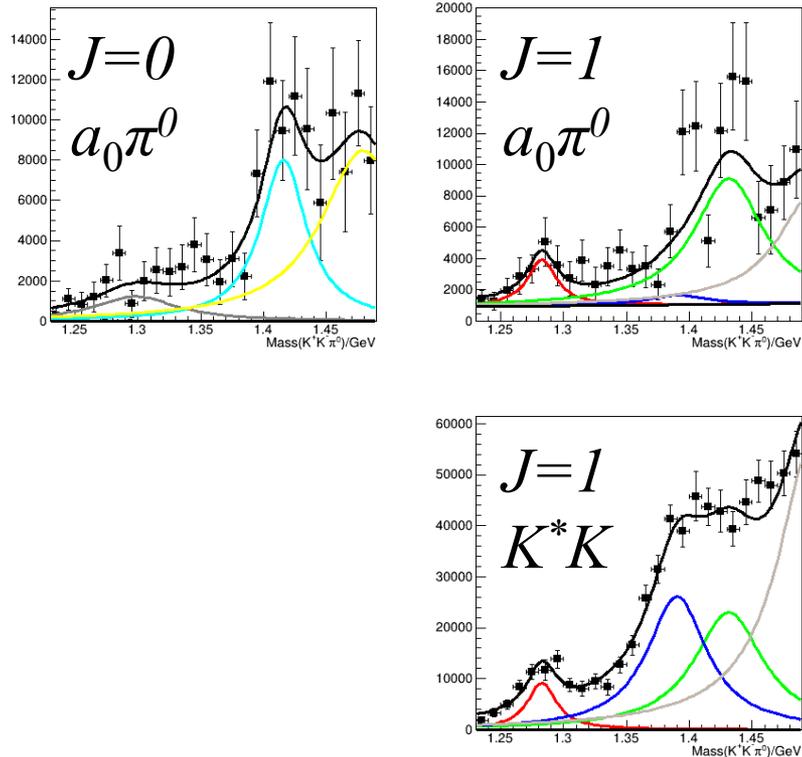


Note:

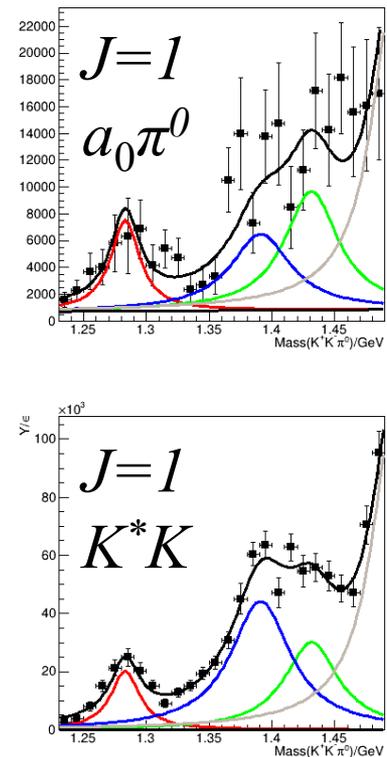
- $h_1 \rightarrow a_0\pi^0$  (**Blue**) was not generated

# Comparison of Real to Fake: Mass[ $K^+K^-\pi^0$ ]

**REAL**



**FAKE**

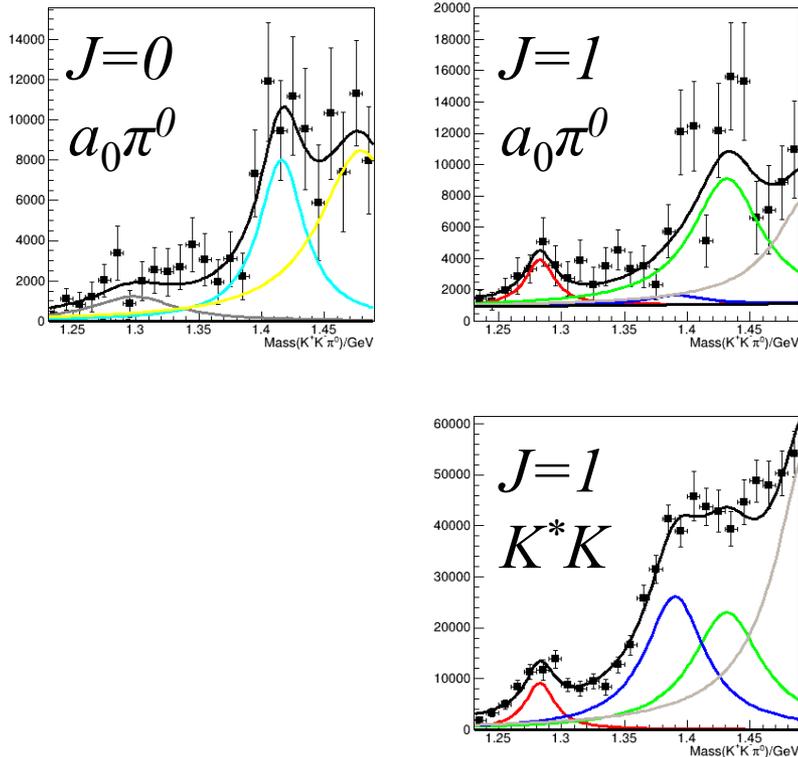


Note:

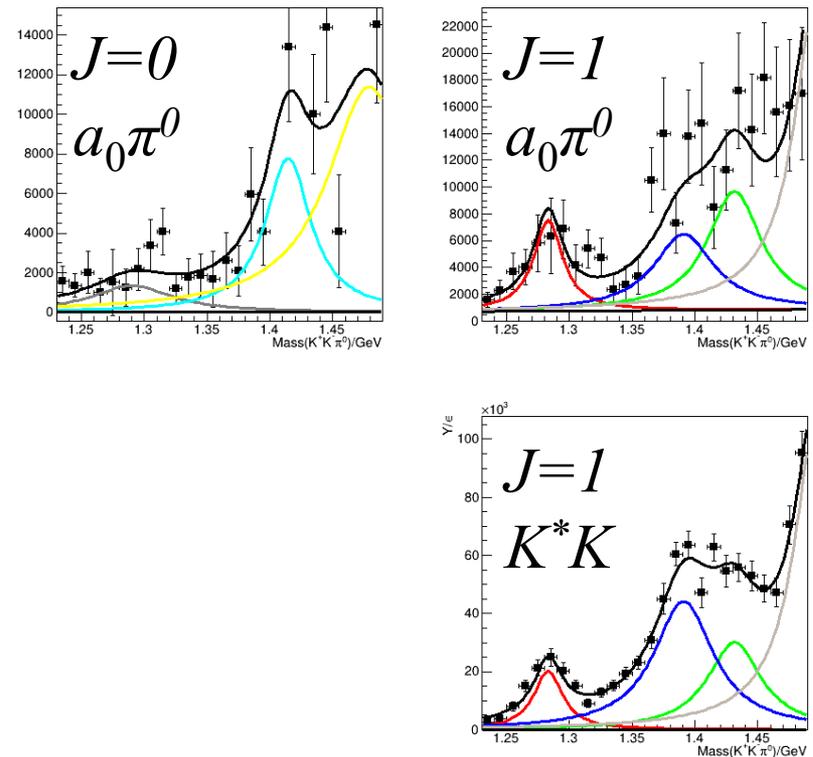
- $h_1 \rightarrow a_0\pi^0$  (**Blue**) was not generated

# Comparison of Real to Fake: Mass[ $K^+K^-\pi^0$ ]

**REAL**



**FAKE**



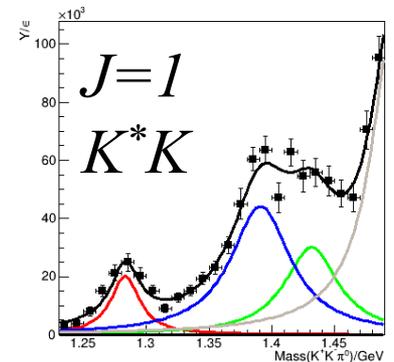
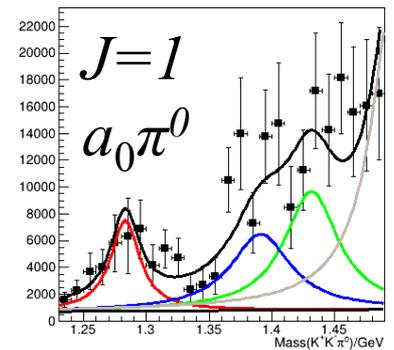
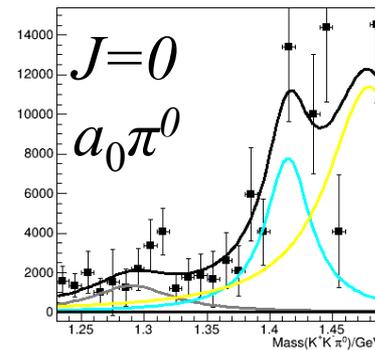
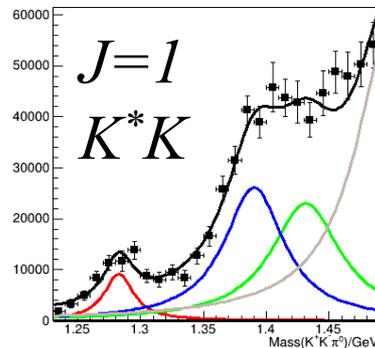
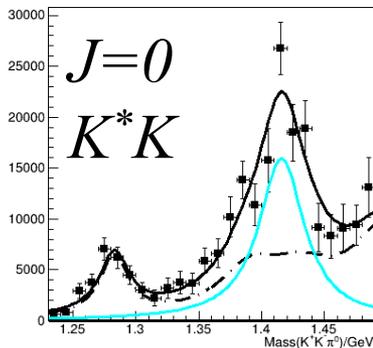
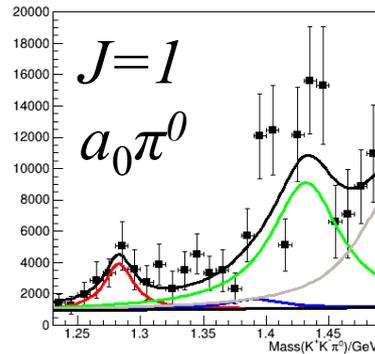
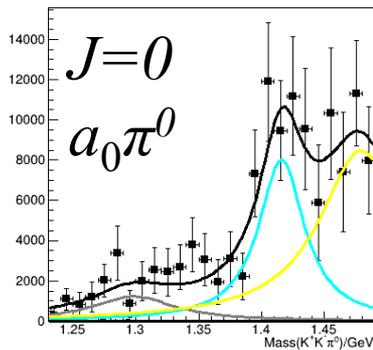
Note:

- $h_1 \rightarrow a_0\pi^0$  [Blue] was not generated
- $\eta(1295)$  [Gray] was not generated

# Comparison of Real to Fake: Mass[ $K^+K^-\pi^0$ ]

**REAL**

**FAKE**



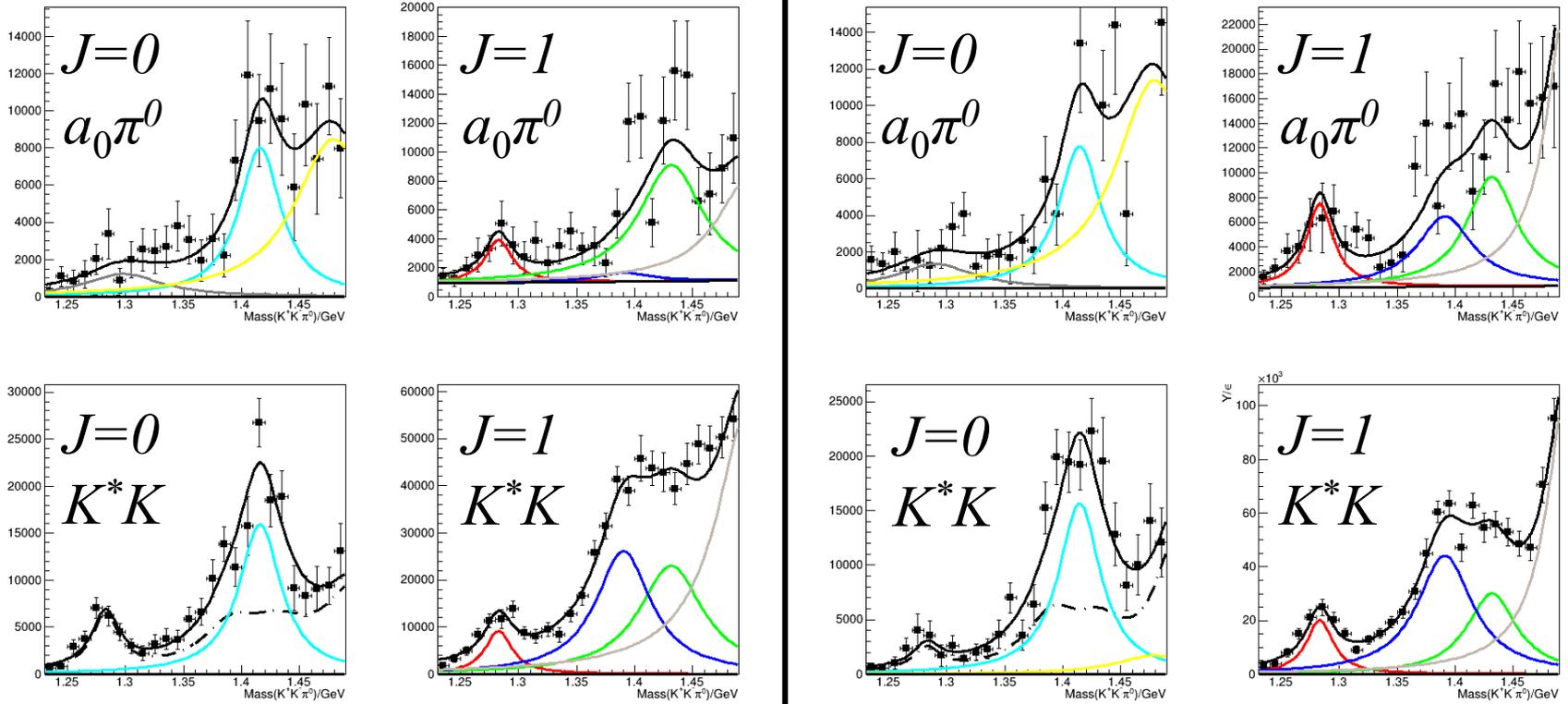
Note:

- $h_1 \rightarrow a_0\pi^0$  [Blue] was not generated
- $\eta(1295)$  [Gray] was not generated

# Comparison of Real to Fake: Mass[ $K^+K^-\pi^0$ ]

**REAL**

**FAKE**



Note:

- $h_1 \rightarrow a_0\pi^0$  [Blue] was not generated
- $\eta(1295)$  [Gray] was not generated
- Assumed leakage (dashed-dotted lines) looks similar 😊 46



# Title



