$K^+K^-\pi^0$ update $a_0(980)$ mass parameterization



Using $a_0(980)$ isobar as parameterized by BESIII:

The ordinary intermediate resonance is parametrized by a relativistic Breit-Wigner (BW) propagator with a constant-width

$$BW(s) = \frac{1}{M^2 - s - iM\Gamma},\tag{4.2}$$

where s is the invariant mass squared of resonances, M and Γ are the corresponding mass and width. For $a_0(980)^0$ with mass near $K\bar{K}$ threshold, we use dispersion integrals to describe its lineshape



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$$\operatorname{Im}\Pi_{ch}(s) = g_{ch}^2 \rho_{ch}(s) F_{ch}(s), \tag{5}$$

while real parts are given by principal value integrals,

$$\operatorname{Re}\Pi_{ch}(s) = \frac{1}{\pi} P \int_{s_{ch}}^{\infty} \frac{\operatorname{Im}\Pi_{ch}(s')ds'}{(s'-s)}.$$
 (6)



In the above expressions $\rho_{ch}(s)$ is the available phase space for a given channel, obtained from the corresponding decay momentum $q_{ch}(s)$: $\rho_{ch}(s) = 2q_{ch}(s)/\sqrt{s}$. The integral in Eq. (6) is divergent when $s \to \infty$, so the phase space is modified by a form factor $F_{ch}(s) = e^{-\beta q_{ch}^2(s)}$, where the parameter β is related to the root-mean-square (rms) size of an emitting source [20]. We use $\beta = 2.0 [\text{GeV}/c^2]^{-2}$ corresponding to rms = 0.68 fm, and we verify that our results are not sensitive to the value of β . The integration in Eq. (6)



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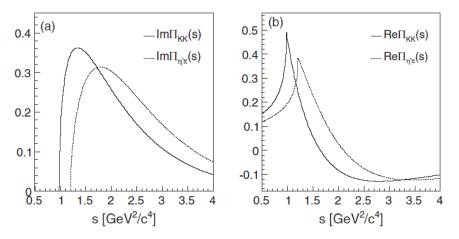


FIG. 4. Line shapes of (a) $Im\Pi(s)$ and (b) $Re\Pi(s)$ for the $K\bar{K}$ and $\eta'\pi$ production with arbitrary normalization.



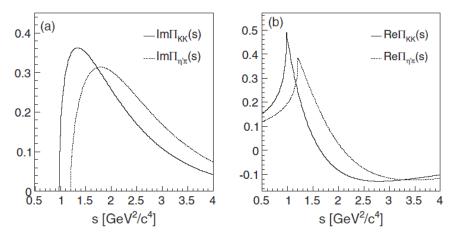


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I used Mathematica to perform the principal value integrals



BESII

$a_0(980)$

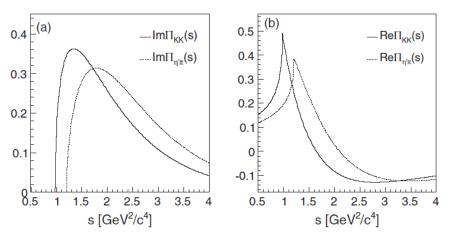
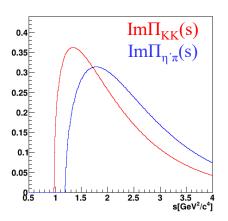


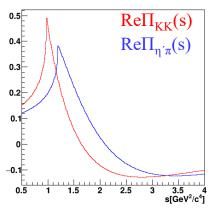
FIG. 4. Line shapes of (a) Im $\Pi(s)$ and (b) Re $\Pi(s)$ for the $K\bar{K}$ and $\eta'\pi$ production with arbitrary normalization.

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Included waves

• Uniform background



Included waves

- Uniform background
- J = 0:

 - a₀π⁰
 K*+K-
 - K*-K+



Included waves

- Uniform background
- J = 0:
 - $a_0\pi^0$
 - K*+K-
 - *K**-*K*+
- J = 1:
 - $a_0\pi^0$
 - $K^{*+}K^{-}(L=0, \text{ and } L=1)$
 - K^*-K^+ (L=0, and L=1)

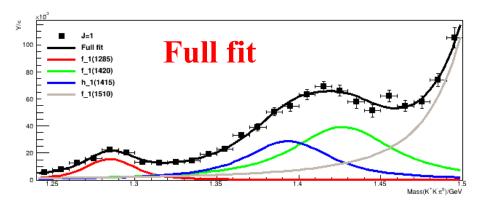


Comparison of OLD to NEW

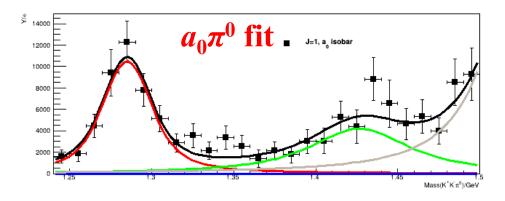
- Previous results I showed in October had standard Breit-Wigner for $a_0(980)$
- New results have BESIII style $a_0(980)$



OLD fit: Simultaneous fit to J=1 isobars

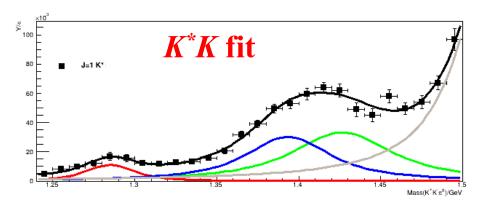


The blue line does not exist in the $a_0\pi^0$

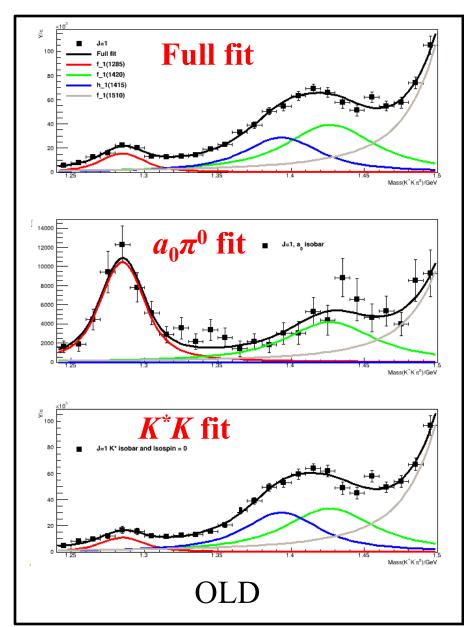


 \Rightarrow

the blue line is consistent with being an h_1

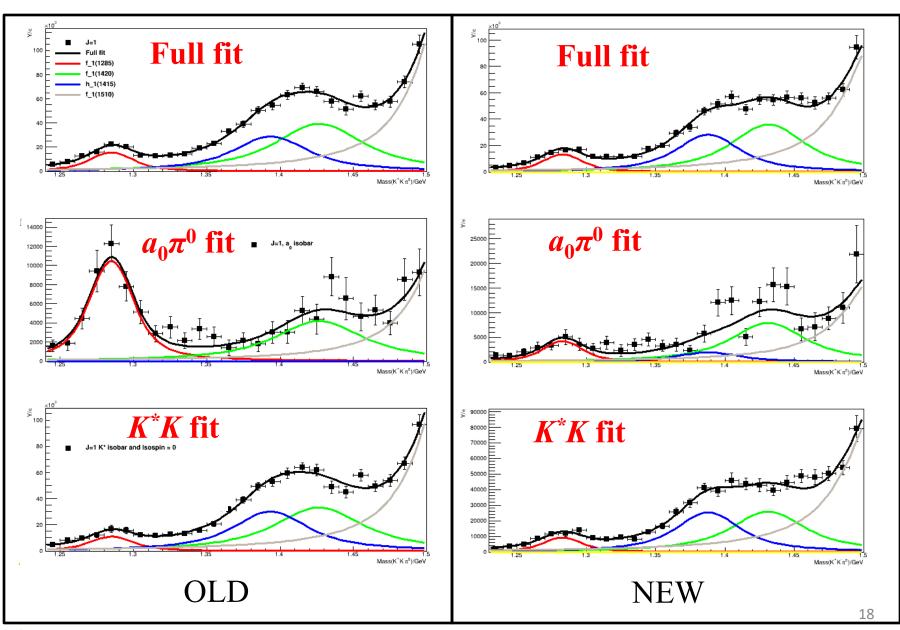


Simultaneous fit to J=1 isobars



NEW

Simultaneous fit to J=1 isobars



Title

