

Early stage Low-mass $K^+K^-\pi^0$ study



Data

Dataset:

- Spring 2018 data

Restrictions:

- Incident photon timed to be within central peak
- Only best Confidence Level (CL) per event kept
- CL must be above 10^{-4}
- Kaons must be seen in TOF
- Missing mass within 3 standard deviations of central peak
- $0.12 \text{ GeV} < \text{Mass}[\pi^0] < 0.15 \text{ GeV}$
- $\text{Mass}[K^+K^-\pi^0] < 1.32$
- Incident photon energy: $5.4 \text{ GeV} < E_\gamma < 9 \text{ GeV}$



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**Need to study and remove
 $\varphi\pi$ contamination**

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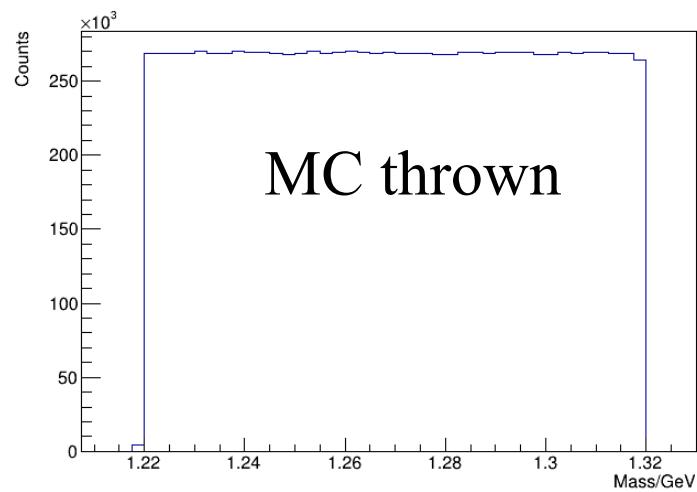
$$K^+ K^- \pi^0$$

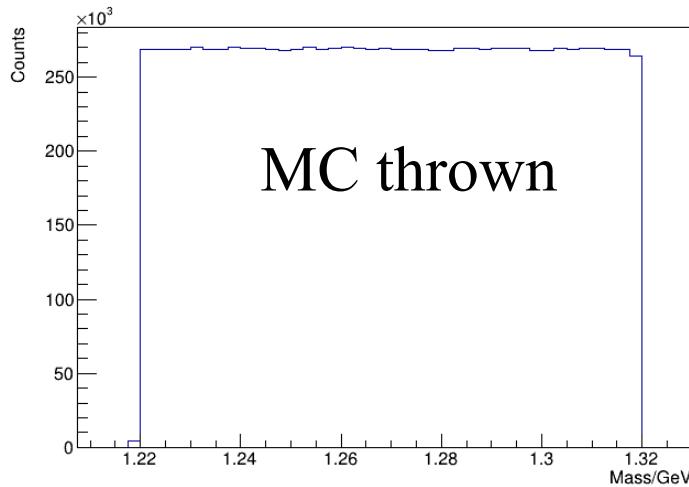
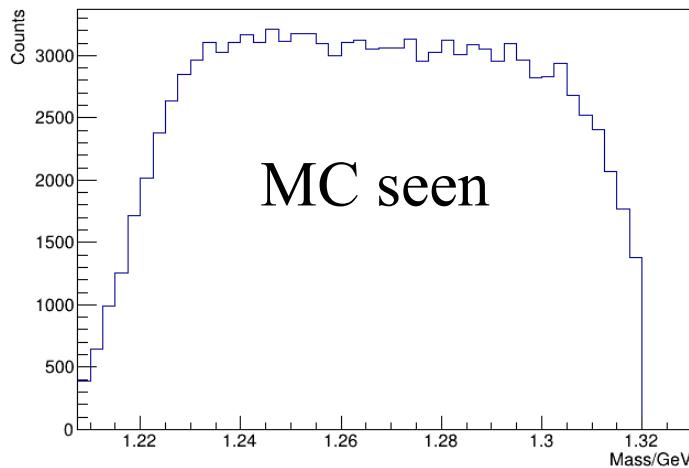
The event generator:

- Flat in mass between 1.22 and 1.32
- Modified t -slope to match the data
- Used actual data to model photon energy spectrum
 - Will need to use normalization distribution in next round of generator refinement
- Over 10 million thrown events

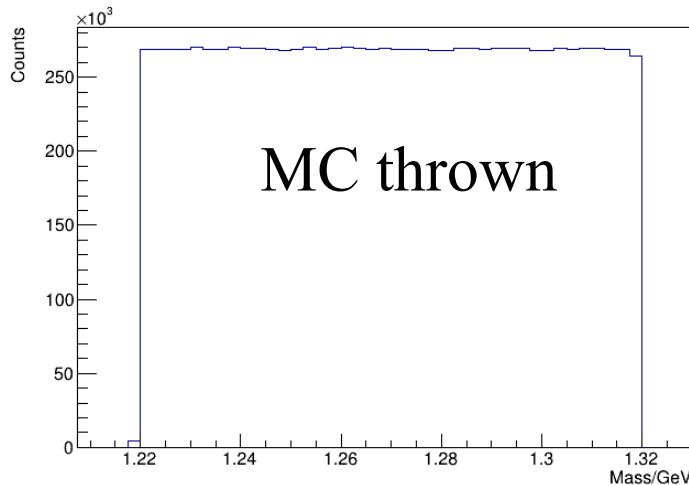
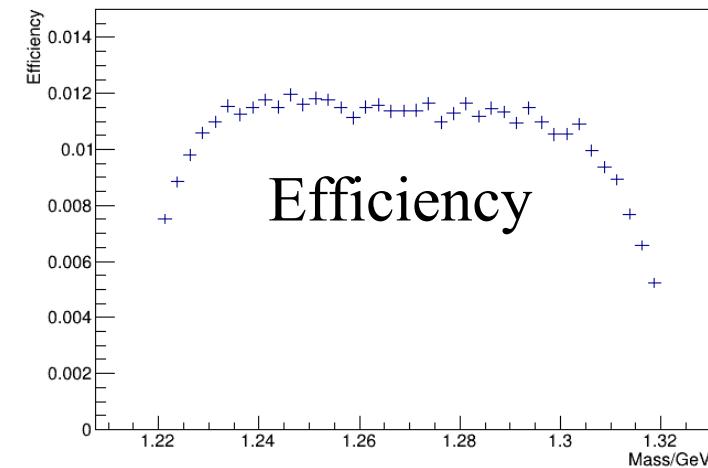
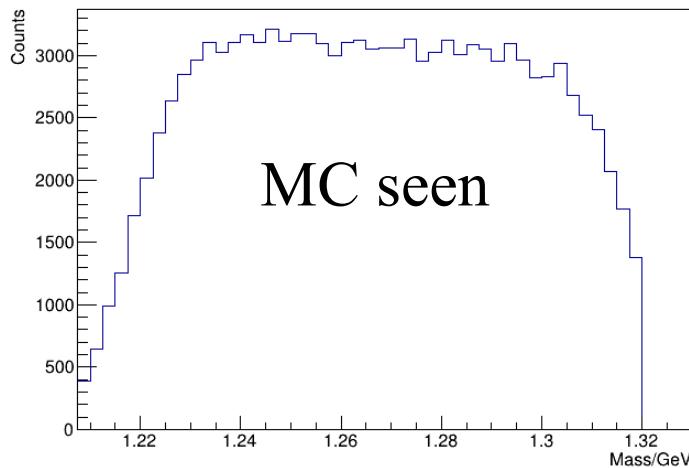


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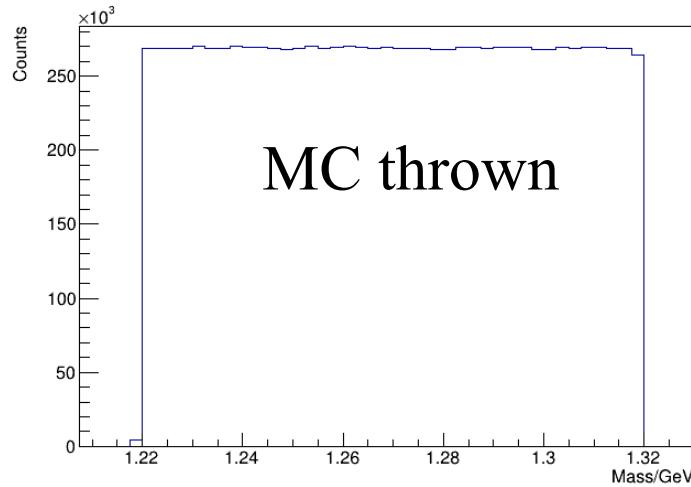
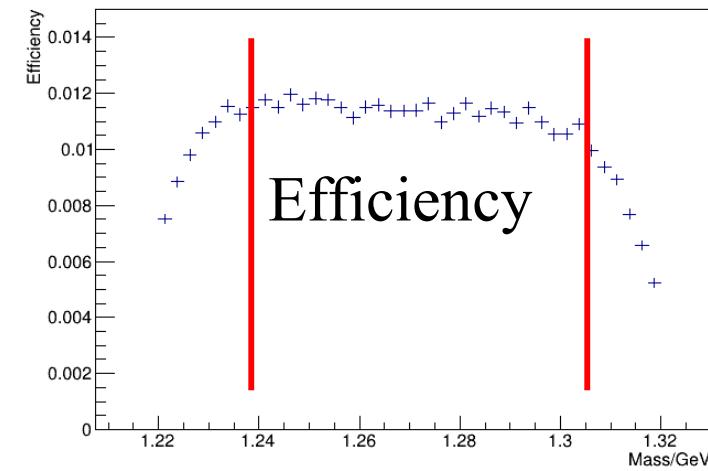
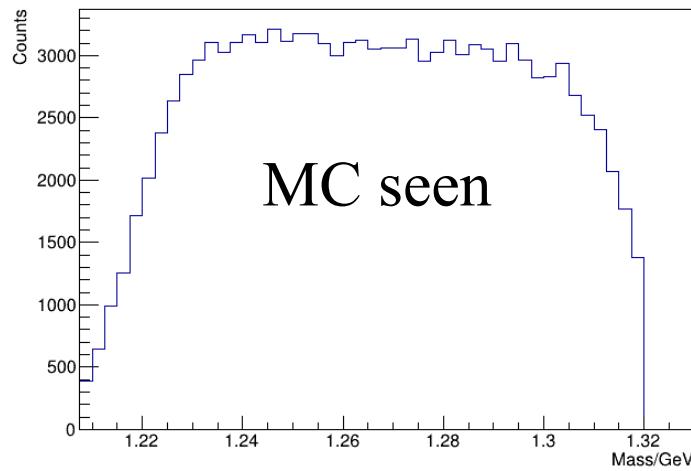


$K^+K^-\pi^0$ 

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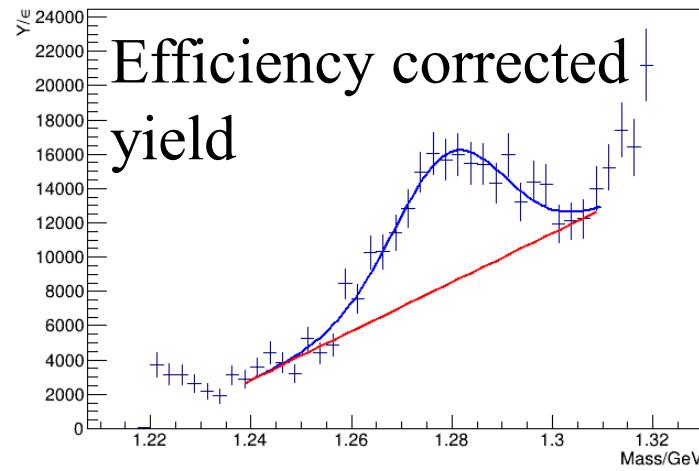
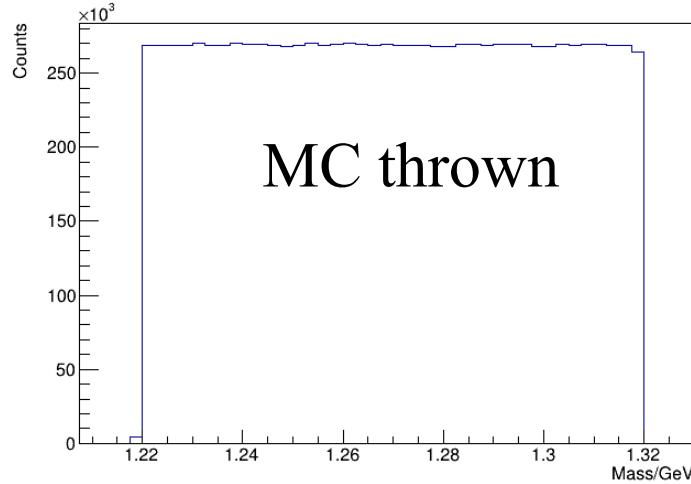
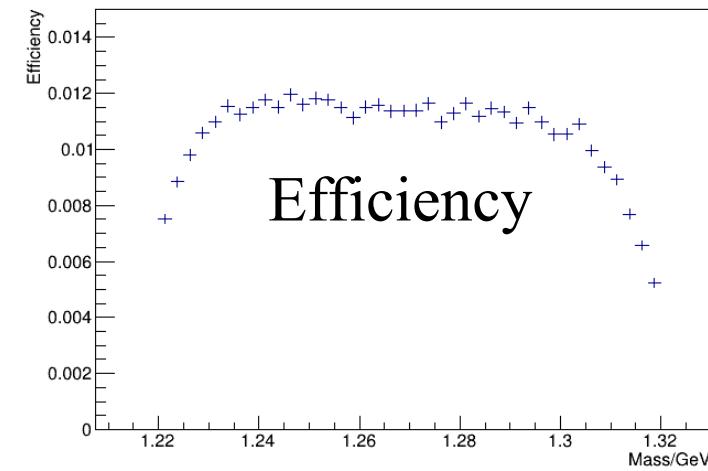
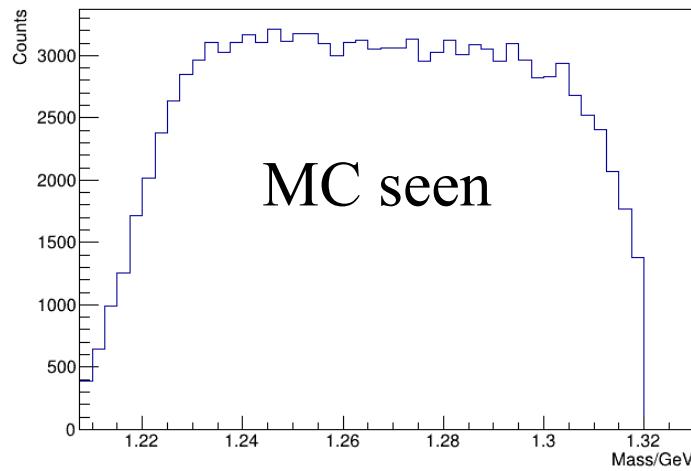
$K^+K^-\pi^0$



Fairly flat over region 1.24 to 1.31 GeV

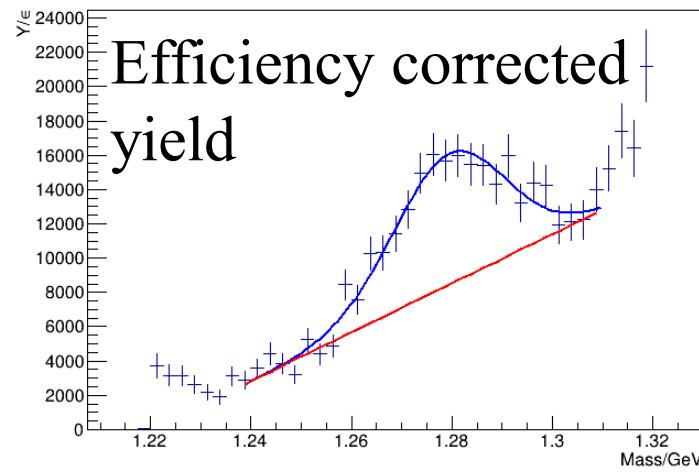
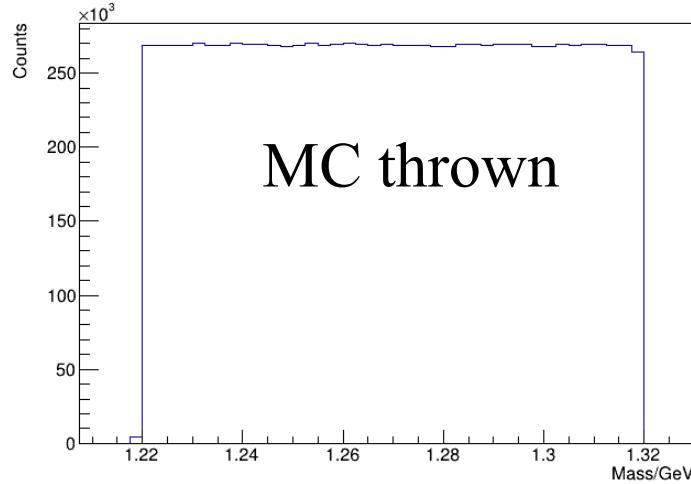
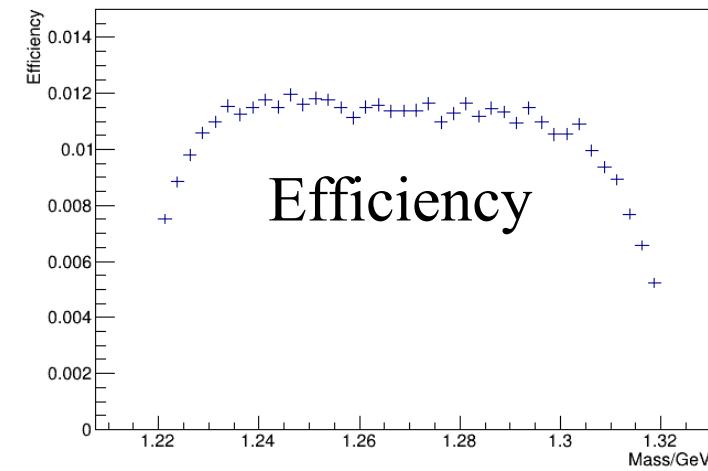
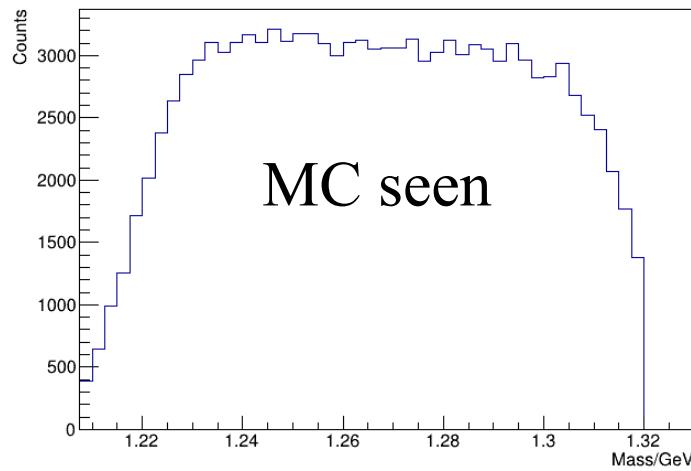


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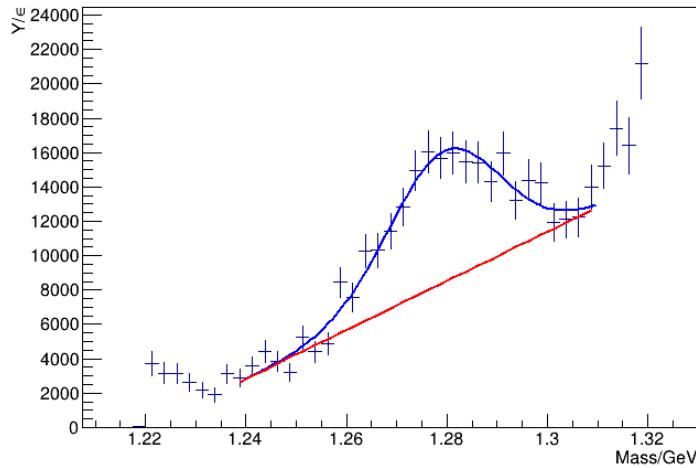
Background subtracted peak is 22% of total counts

$K^+K^-\pi^0$



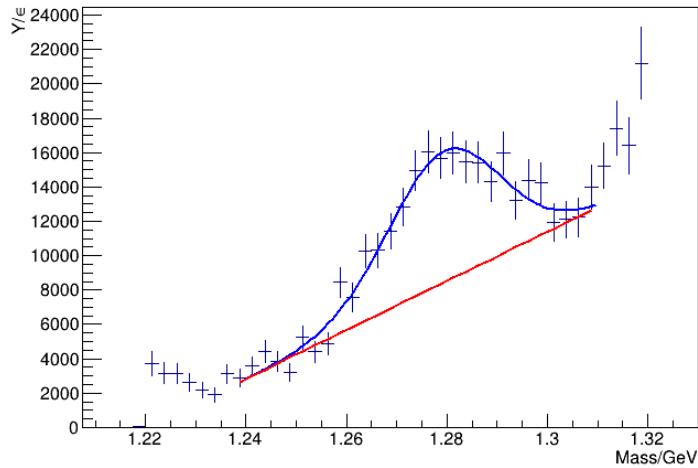
Center = 1279(2) MeV
FWHM = 24(5) MeV



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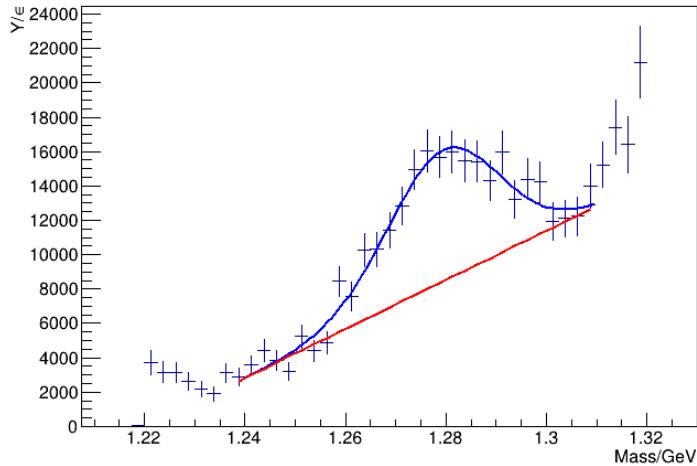
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**Center = 1279(2) MeV
FWHM = 24(5) MeV**

No PDG meson state at 1280 MeV
But...

$$K^+ K^- \pi^0$$



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Photoproduction and Decay Modes of the $x(1280)$ Meson

Show affiliations

Dickson, Ryan ; Schumacher, Reinhard

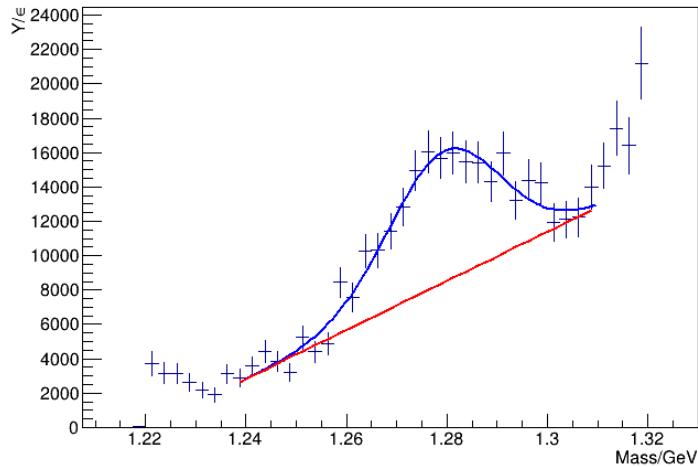
A meson of mass $m_x=1281$ MeV and a FWHM of $\gamma_x=18$ MeV is seen at Jefferson Lab with CLAS in photoproduction off the proton using real photons in the energy range between 1.9 GeV and 3.4 GeV. Both the $f_1(1285)$ and the poorly-known $\eta(1295)$ are candidates for this observed state. The decay modes seen are $x \rightarrow \eta + \pi^+ + \pi^-$, $K^+ + K^0 + \pi^-$, $K^0 + K^0 + \pi^0$, and $K^+ + K^- + \pi^0$ with a substantial fraction going through $a_0(980)\pi$. No signal is seen in $x \rightarrow 0\gamma$. The relative branching fraction $\gamma_{KK\pi}/\gamma_{\eta\pi\pi}$ is consistent with world data for the $f_1(1285)$ state. The unseen 0γ decay mode is not consistent with the $f_1(1285)$ state, however, and may be more consistent with the $\eta(1295)$. Angle and energy dependencies of the measured cross-sections are in fair agreement among the observed decay modes.

Publication: American Physical Society, 2009 APS April Meeting, May 2-5, 2009, abstract id.
Q10.004

Pub Date: May 2009

Bibcode: 2009APS..APRQ10004D

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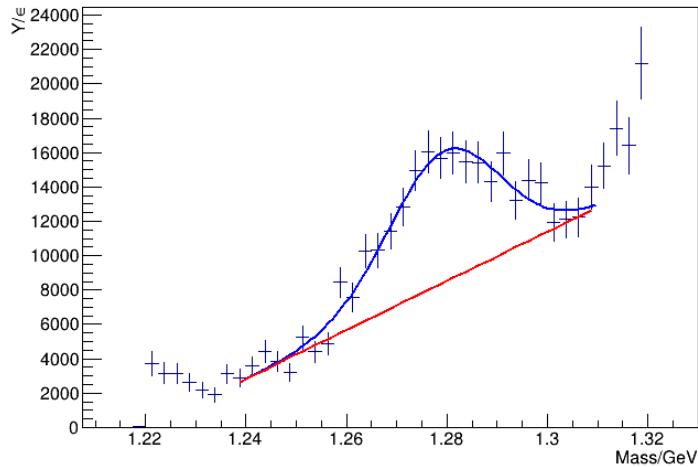
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Sent email to Reinhard asking what came of the CMU study of this $x(1280)$ bump. Waiting for response.

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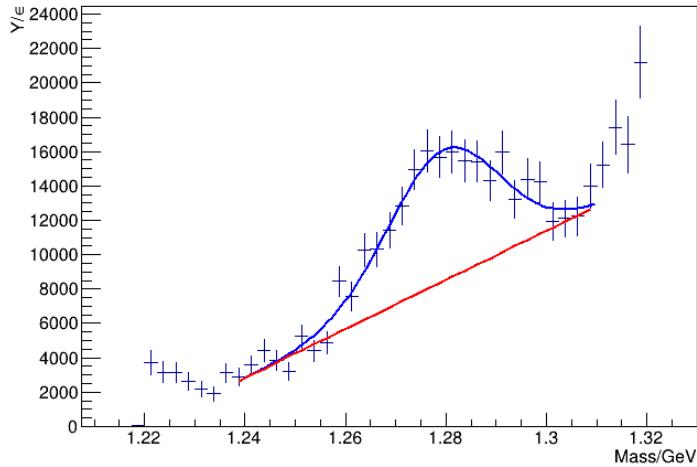
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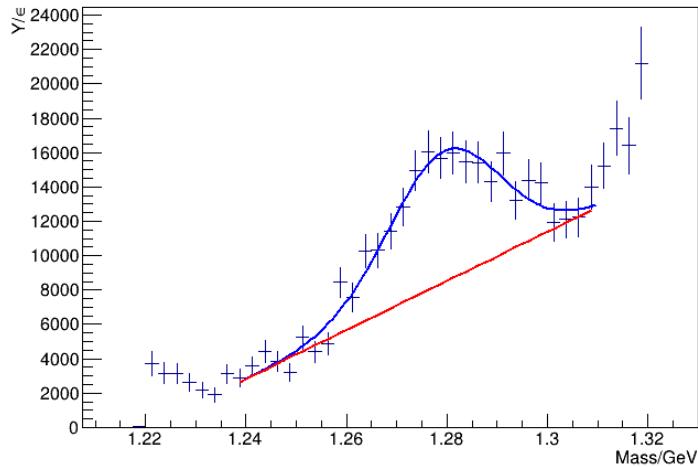
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Definition of (θ, φ) and (θ_H, φ_H)

- The (θ, φ) angles defined from polar and azimuthal angles of the K^+K^- isobar in the Gottfried-Jackson frame of $K^+K^-\pi^0$ system: z -axis coincident with the incident photon and y -axis normal to the production plane



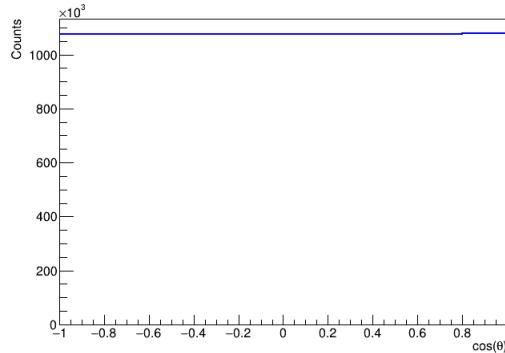
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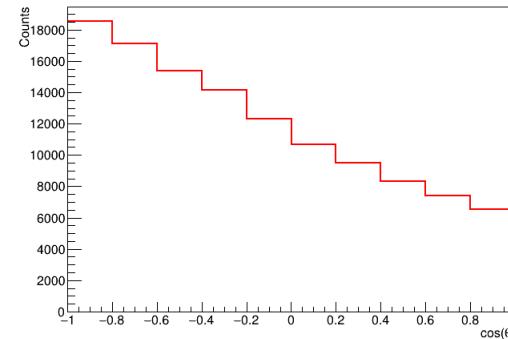


Distributions of $\cos(\theta)$ and φ

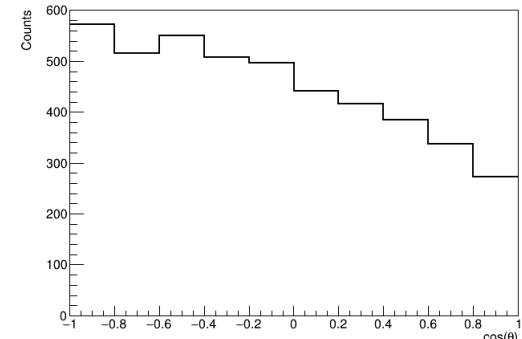
MC thrown



MC seen

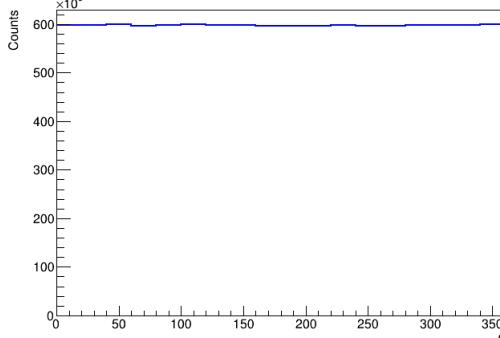


Real data

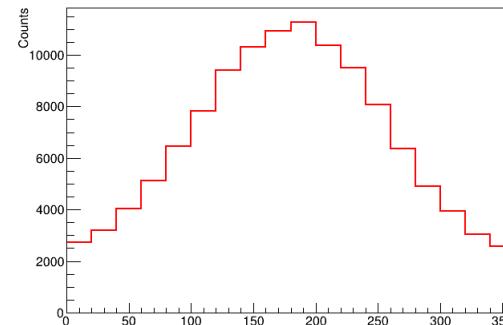


$\cos(\theta)$ distributions

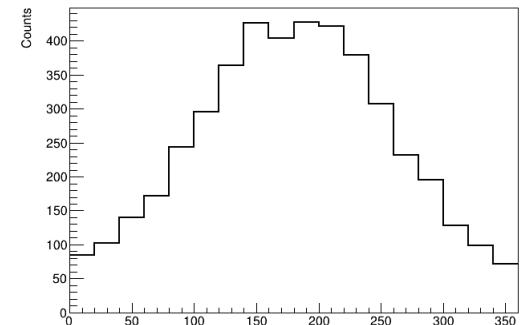
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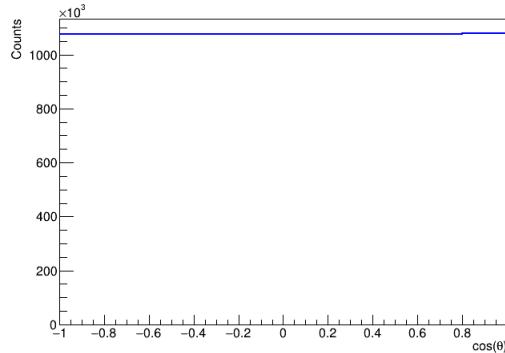


φ distributions

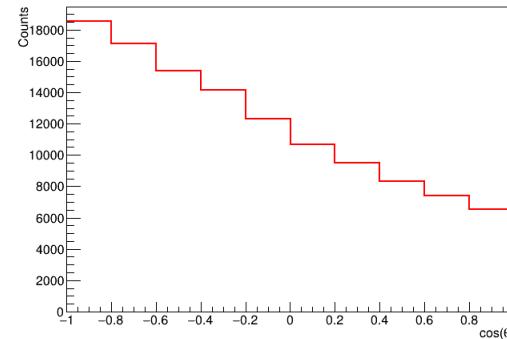


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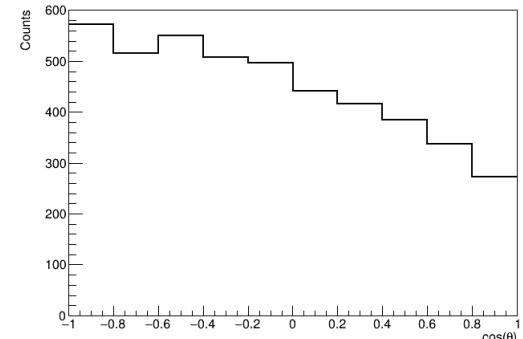
MC thrown



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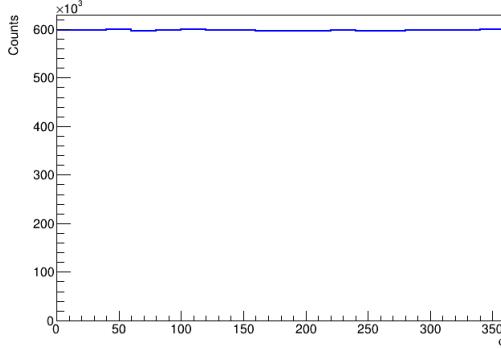


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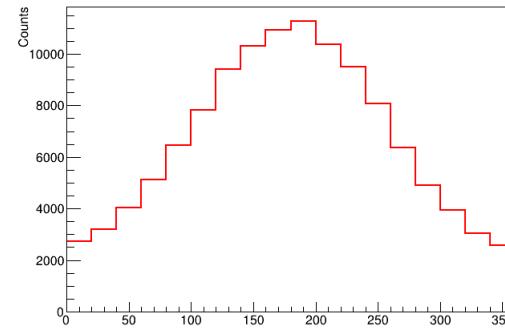


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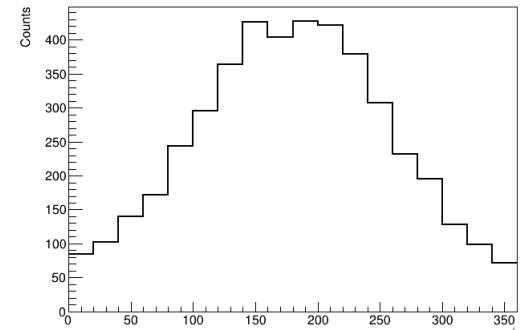
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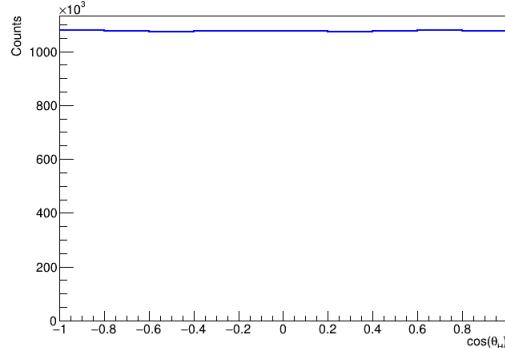
φ distributions

- Real data looks similar to detector accepted phase space²¹

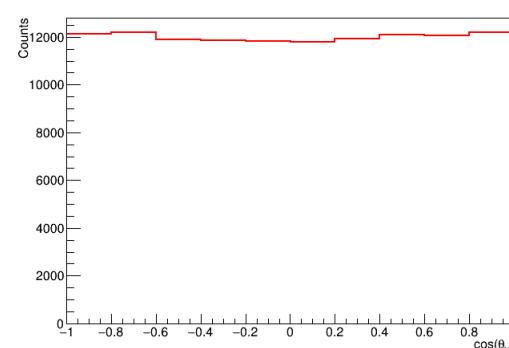


Distributions of $\cos(\theta_H)$ and ϕ_H

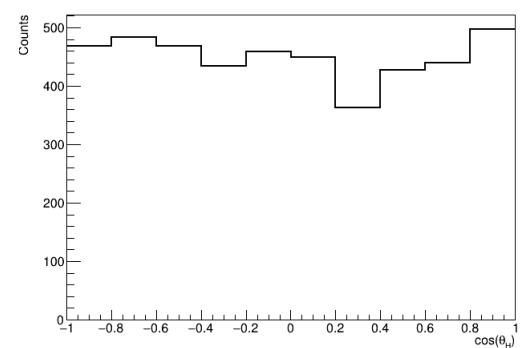
MC thrown



MC seen

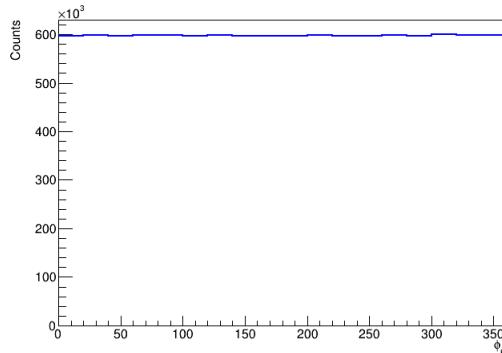


Real data

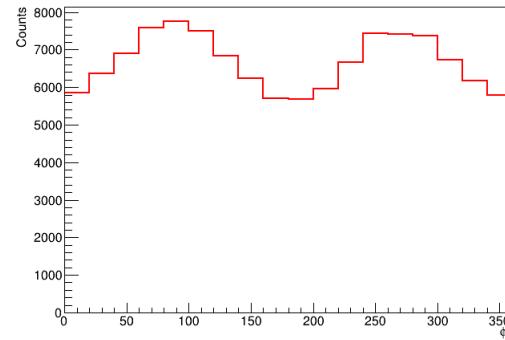


$\cos(\theta_H)$ distributions

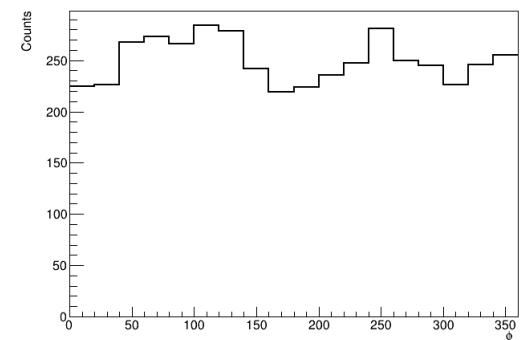
MC thrown



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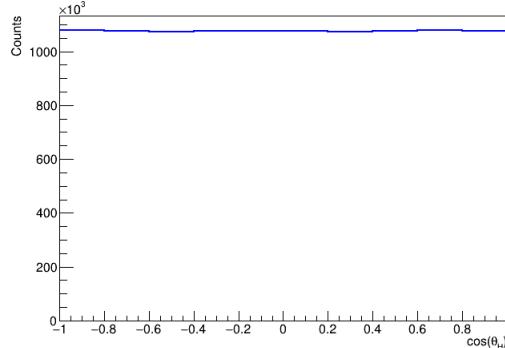


ϕ_H distributions

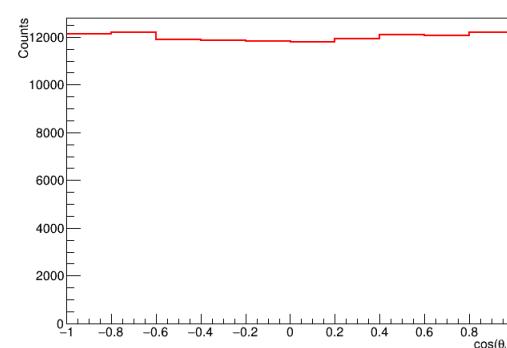


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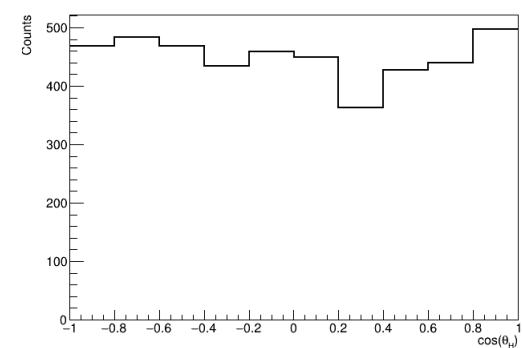
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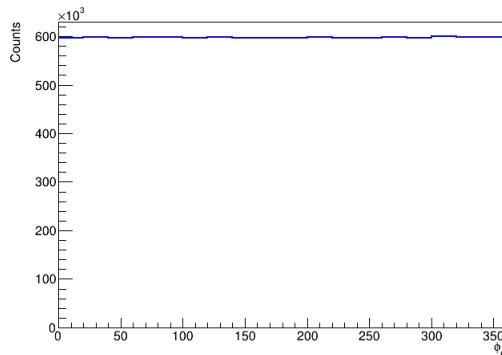


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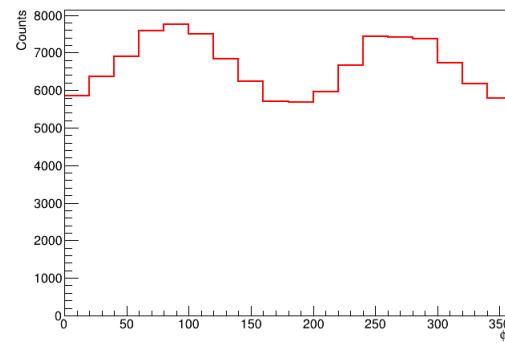


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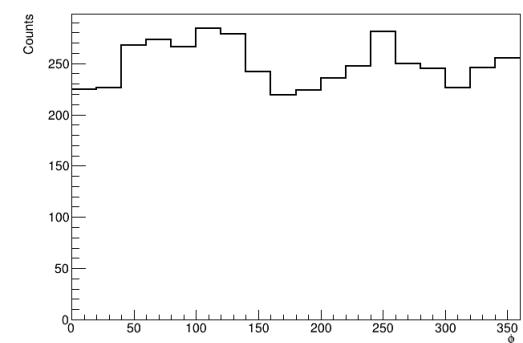
MC thrown



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ϕ_H distributions

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Initial PWA setup

- Used PWA expressions:

$$a_{Jlsm} \sum_{\lambda} D_{m\lambda}^{J*}(\varphi_{GJ}, \theta_{GJ}) D_{\lambda 0}^{s*}(\varphi_h, \theta_h) \langle l0s\lambda | J\lambda \rangle,$$



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- Used AmpTools for PWA
- Meson Resonance (R) = $KK\pi$ system
- Decay modeled as $R \rightarrow$ Isobar π , where Isobar $\rightarrow K K$



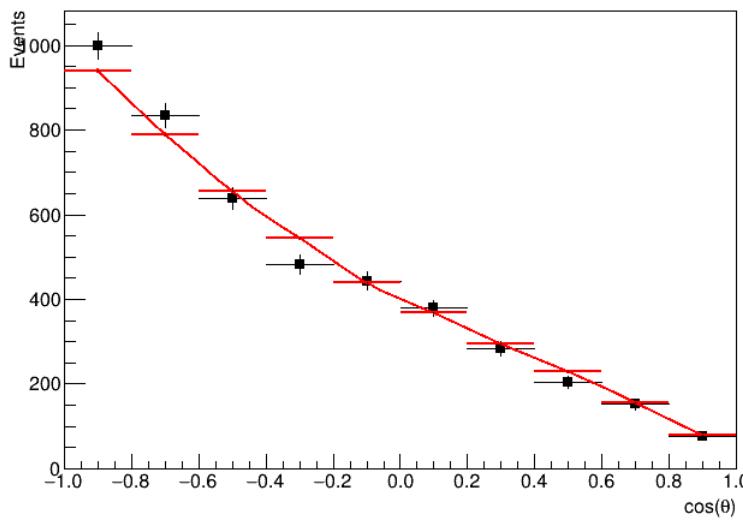
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- Used PWA expressions:
 $a_{Jlsm} \sum_{\lambda} D_{m\lambda}^{J*}(\varphi_{GJ}, \theta_{GJ}) D_{\lambda 0}^{s*}(\varphi_h, \theta_h) \langle l0s\lambda | J\lambda \rangle$, where the form under summation is from Salgado-Weygand and a_{Jlsm} are the coefficients of the fit
- Used AmpTools for PWA
- Meson Resonance (R) = $KK\pi$ system
- Decay modeled as $R \rightarrow$ Isobar π , where Isobar $\rightarrow K K$
- Coherently added:
 - $j=0$, with
 - $l=0, s=0$
 - $l=1, s=1$
 - $j=1$, with
 - $l=1, s=0, m_j = -1, 0, 1$
 - $l=0, s=1, m_j = -1, 0, 1$
 - $l=1, s=1, m_j = -1, 0, 1$

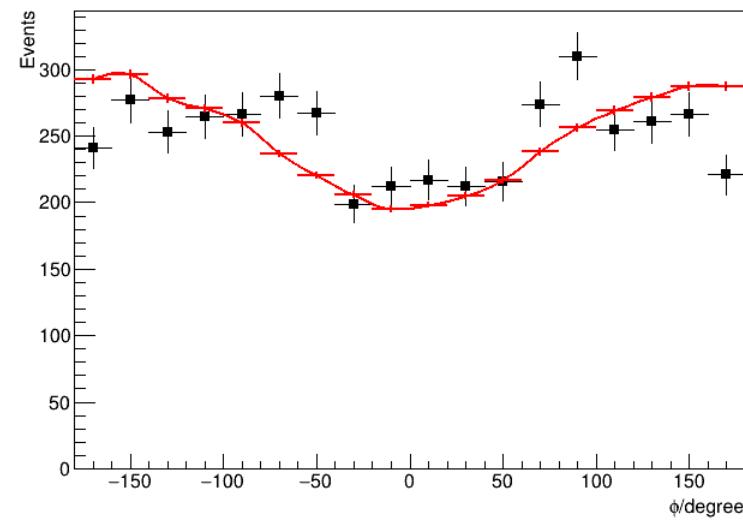


Initial PWA results

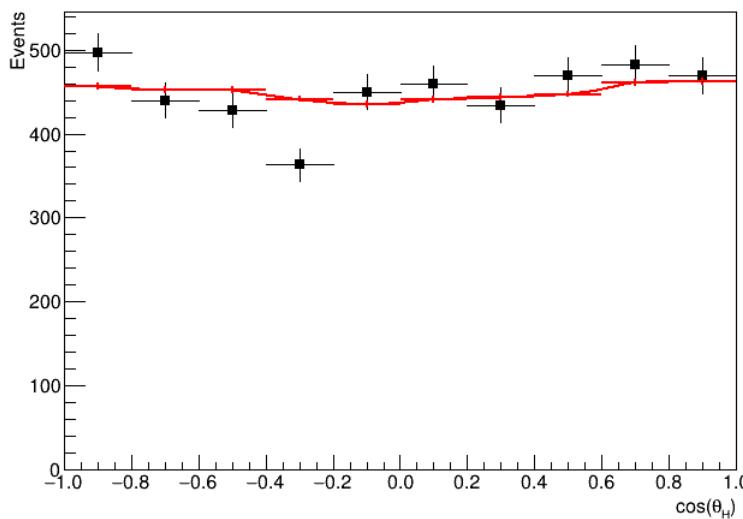
$\cos(\theta)$



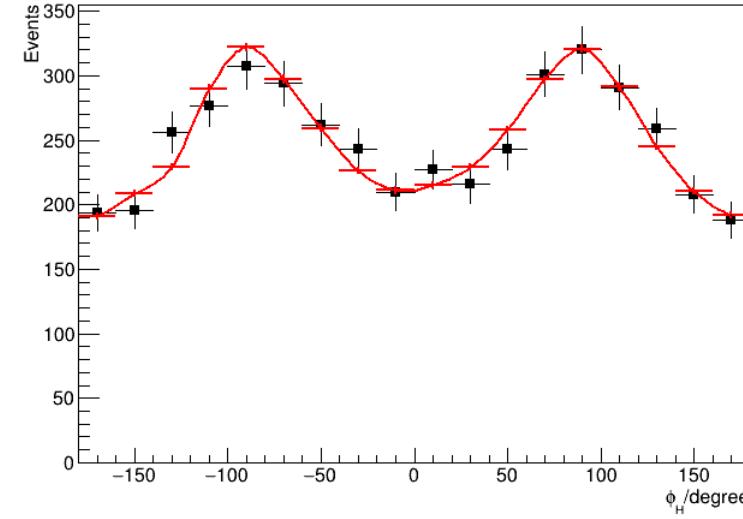
ϕ



$\cos(\theta_H)$



ϕ_H



Initial PWA results

| | |
|--|------------------------------|
| Fit fraction $j=0, l=0, s=0$ | : 0.803564 +- -0.0154223 |
| Fit fraction $j=0, l=1, s=1$ | : 0.0151096 +- -0.00623058 |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | : 0.00870284 +- -0.00527657 |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | : 0.00602312 +- -0.0018275 |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | : 0.00372239 +- -0.00285835 |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | : 0.00440244 +- -0.00297814 |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | : 0.0824543 +- -0.0176945 |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | : 0.00265832 +- -0.00235178 |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | : 0.00107336 +- -0.00148959 |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | : 0.000656921 +- -0.00139304 |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | : 0.000604052 +- -0.00122445 |



Initial PWA results

By far, the most
important
contribution

| | |
|--|------------------------------|
| Fit fraction $j=0, l=0, s=0$ | : 0.803564 +- -0.0154223 |
| Fit fraction $j=0, l=1, s=1$ | : 0.0151096 +- -0.00623058 |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | : 0.00870284 +- -0.00527657 |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | : 0.00602312 +- -0.0018275 |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | : 0.00372239 +- -0.00285835 |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | : 0.00440244 +- -0.00297814 |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | : 0.0824543 +- -0.0176945 |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | : 0.00265832 +- -0.00235178 |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | : 0.00107336 +- -0.00148959 |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | : 0.000656921 +- -0.00139304 |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | : 0.000604052 +- -0.00122445 |



Initial PWA results

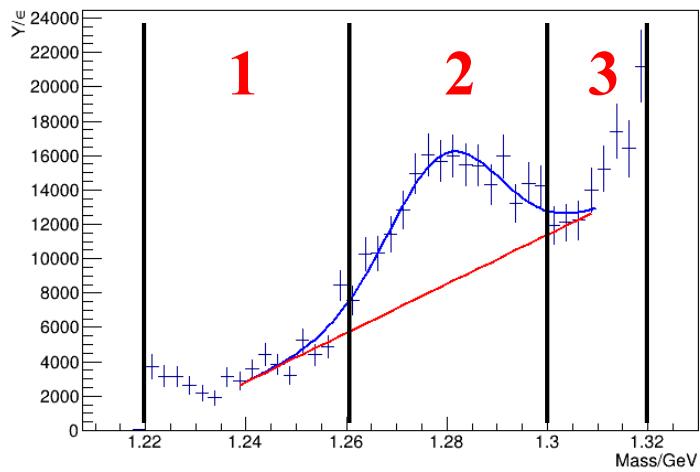
By far, the most
important
contribution

| | |
|--|------------------------------|
| Fit fraction $j=0, l=0, s=0$ | : 0.803564 +- -0.0154223 |
| Fit fraction $j=0, l=1, s=1$ | : 0.0151096 +- -0.00623058 |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | : 0.00870284 +- -0.00527657 |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | : 0.00602312 +- -0.0018275 |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | : 0.00372239 +- -0.00285835 |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | : 0.00440244 +- -0.00297814 |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | : 0.0824543 +- -0.0176945 |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | : 0.00265832 +- -0.00235178 |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | : 0.00107336 +- -0.00148959 |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | : 0.000656921 +- -0.00139304 |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | : 0.000604052 +- -0.00122445 |

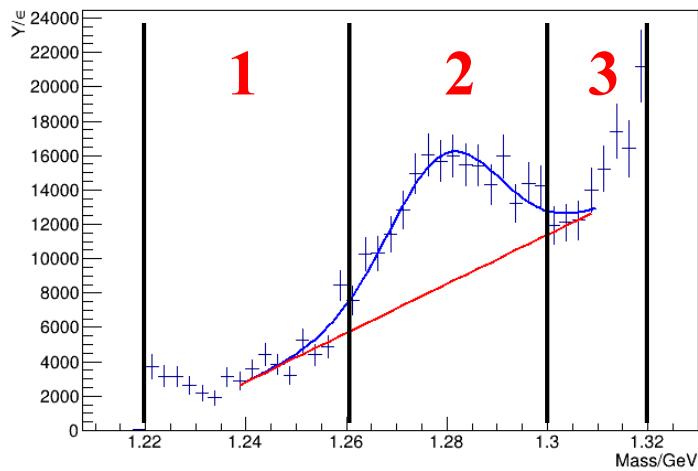
Is $x(1280)$ a $J=0$ or 1 ?



PWA over 3 mass regions



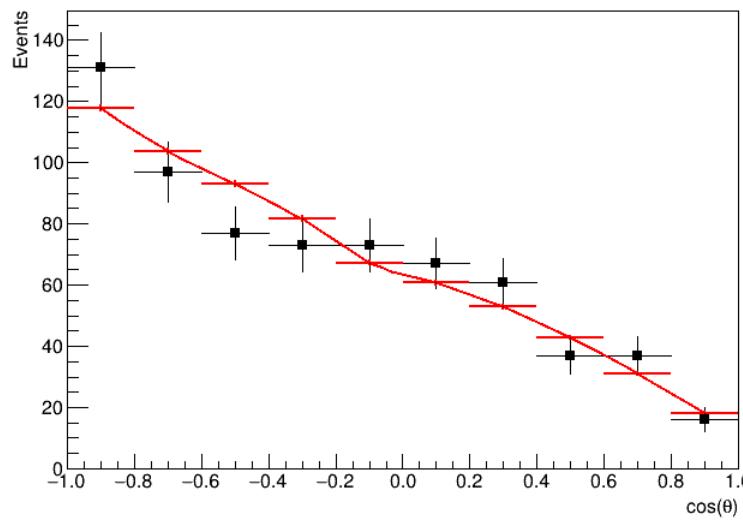
PWA over 3 mass regions



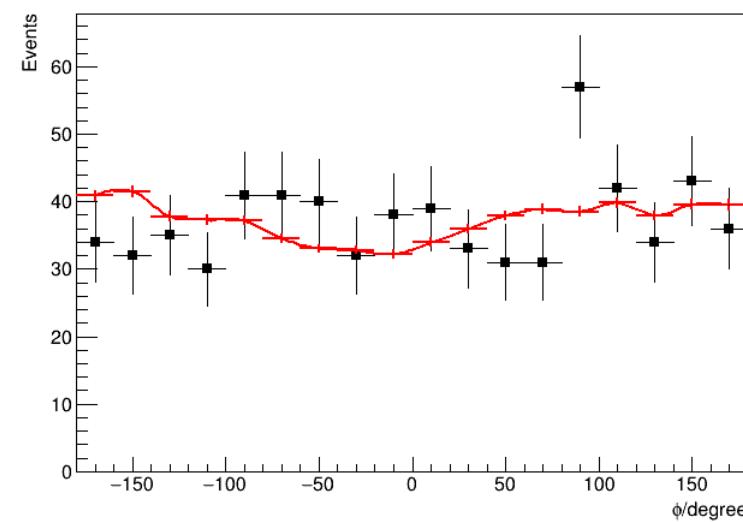
- If $x(1280)$ is $J \neq 0$, fit fraction of $J=0$ in region 2 should decrease relative to the other regions

Region 1 PWA results

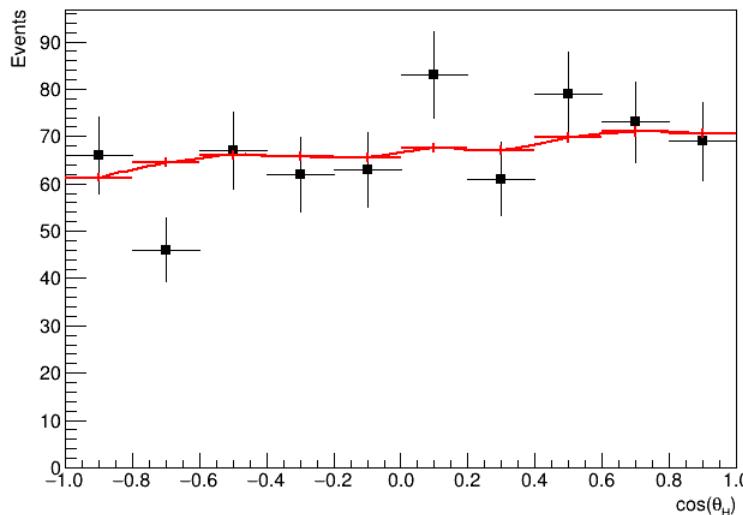
$\cos(\theta)$



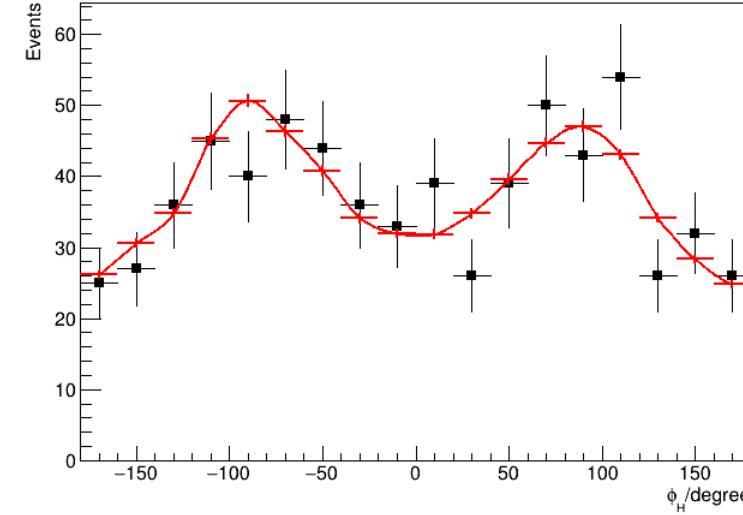
ϕ



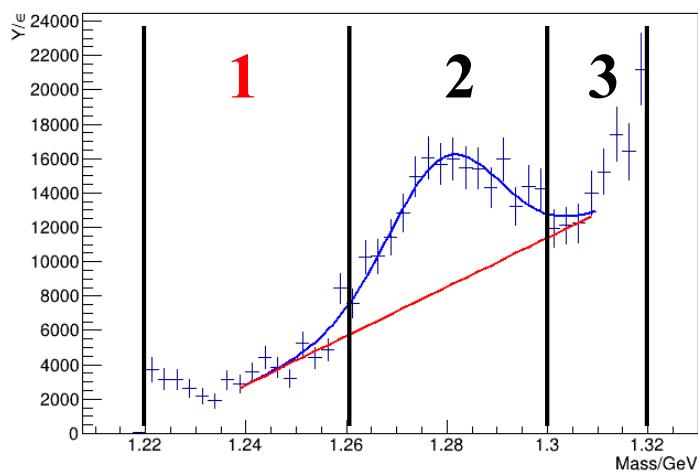
$\cos(\theta_H)$



ϕ_H



Region 1 PWA results

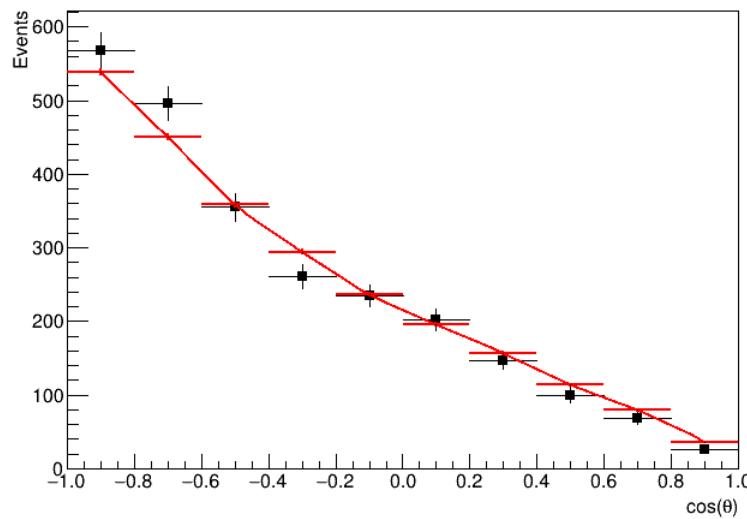


Region 1

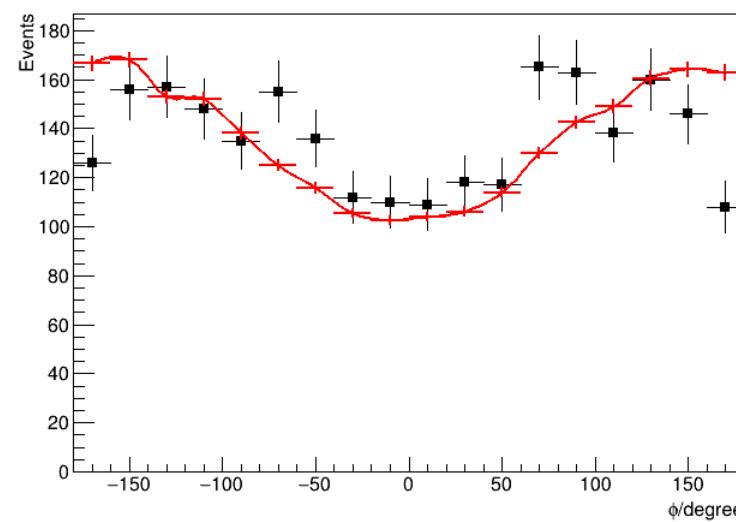
| | |
|--|--------------------------------|
| Fit fraction $j=0, l=0, s=0$ | : 0.755485 ± -0.270702 |
| Fit fraction $j=0, l=1, s=1$ | : 0.0458552 ± -0.194178 |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | : $0.0061852 \pm -0.00818622$ |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | : 0.0381819 ± -0.0266231 |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | : 0.0145478 ± -0.0132996 |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | : $0.00891352 \pm -0.00847945$ |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | : 0.0341858 ± -0.025853 |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | : 0.0151747 ± -0.0114261 |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | : 0.0250261 ± -0.0154815 |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | : $0.00637649 \pm -0.00966565$ |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | : 0.0156042 ± -0.0123044 |

Region 2 PWA results

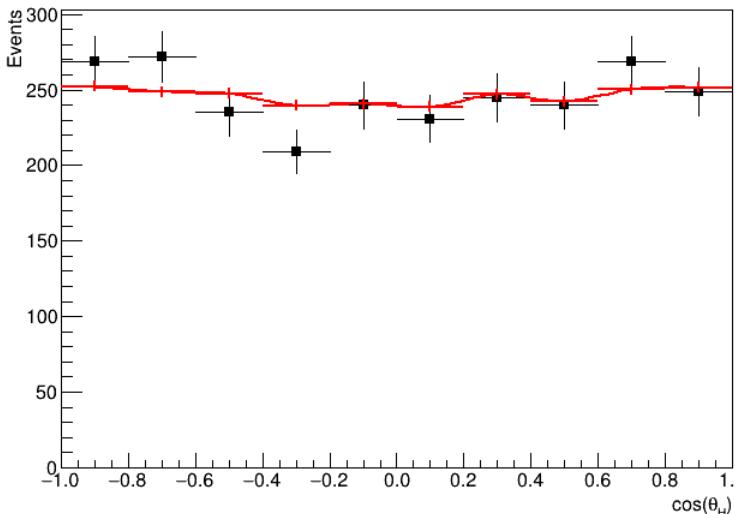
$\cos(\theta)$



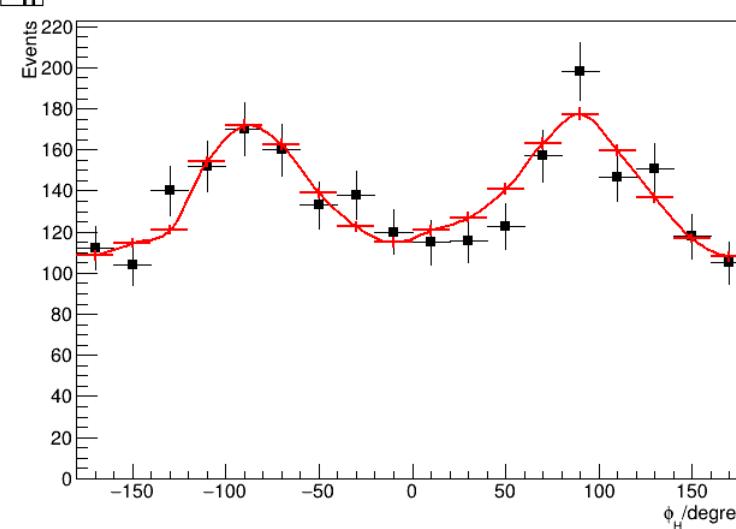
ϕ



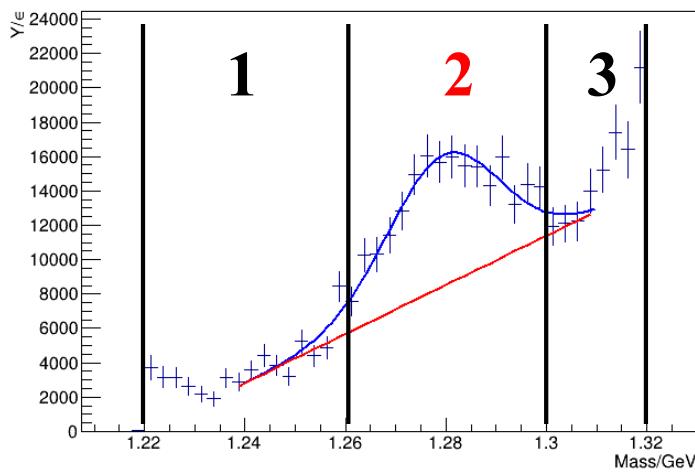
$\cos(\theta_H)$



ϕ_H



Region 2 PWA results



Region 1

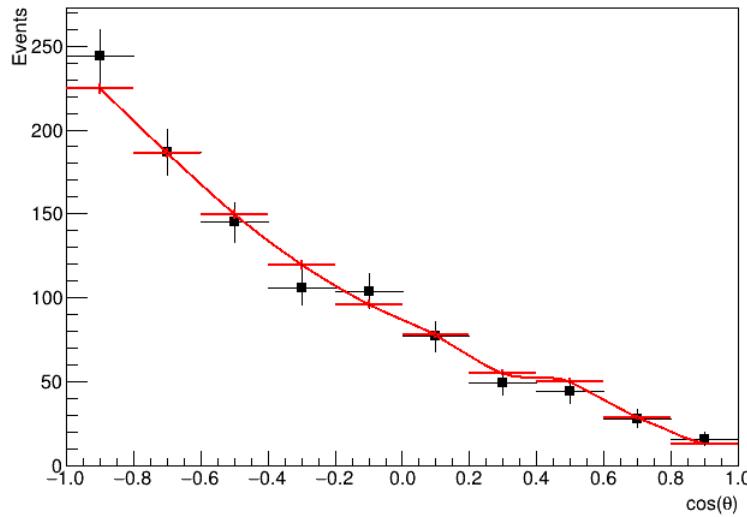
| | |
|--|--------------------------------|
| Fit fraction $j=0, l=0, s=0$ | : 0.755485 ± -0.270702 |
| Fit fraction $j=0, l=1, s=1$ | : 0.0458552 ± -0.194178 |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | : $0.0061852 \pm -0.00818622$ |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | : 0.0381819 ± -0.0266231 |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | : 0.0145478 ± -0.0132996 |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | : $0.00891352 \pm -0.00847945$ |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | : 0.0341858 ± -0.025853 |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | : 0.0151747 ± -0.0114261 |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | : 0.0250261 ± -0.0154815 |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | : $0.00637649 \pm -0.00966565$ |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | : 0.0156042 ± -0.0123044 |

Region 2

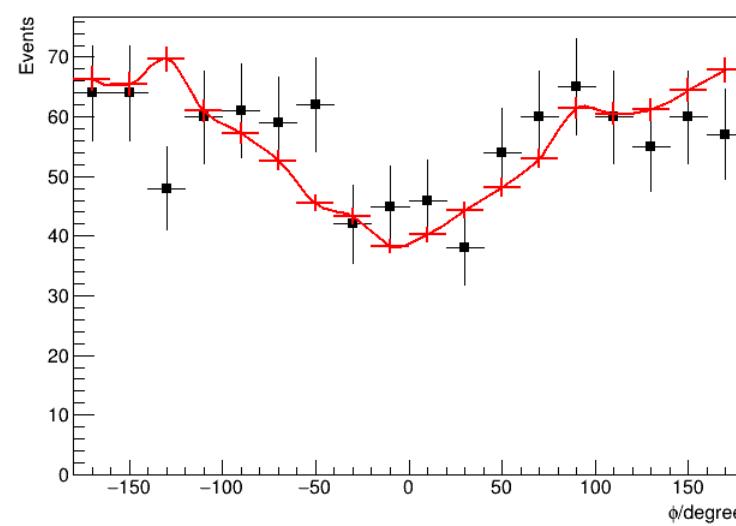
| | |
|--|---------------------------------|
| Fit fraction $j=0, l=0, s=0$ | : 0.824834 ± -0.17209 |
| Fit fraction $j=0, l=1, s=1$ | : $0.00481546 \pm -0.0289436$ |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | : $0.00287929 \pm -0.00362665$ |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | : $0.00922431 \pm -0.00378745$ |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | : 0.01217 ± -0.00801337 |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | : $0.00408659 \pm -0.00355879$ |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | : 0.105621 ± -0.0267424 |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | : $0.0028925 \pm -0.00297443$ |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | : $0.000537718 \pm -0.00118739$ |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | : $0.00209243 \pm -0.00381629$ |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | : $0.00314316 \pm -0.00324201$ |

Region 3 PWA results

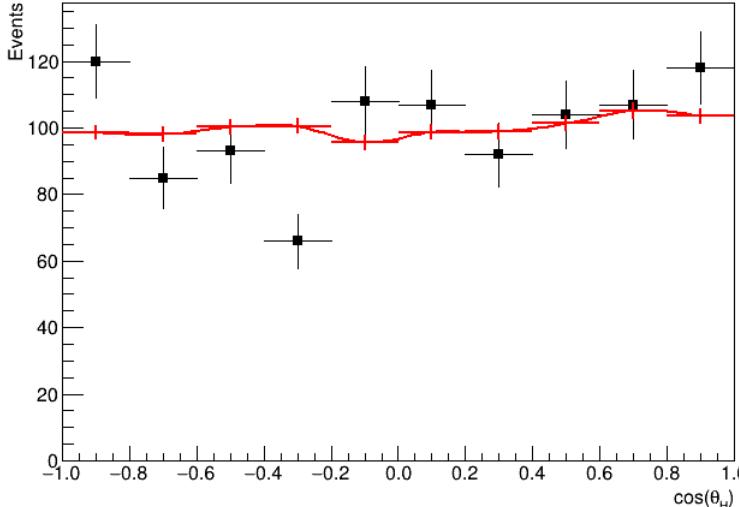
$\cos(\theta)$



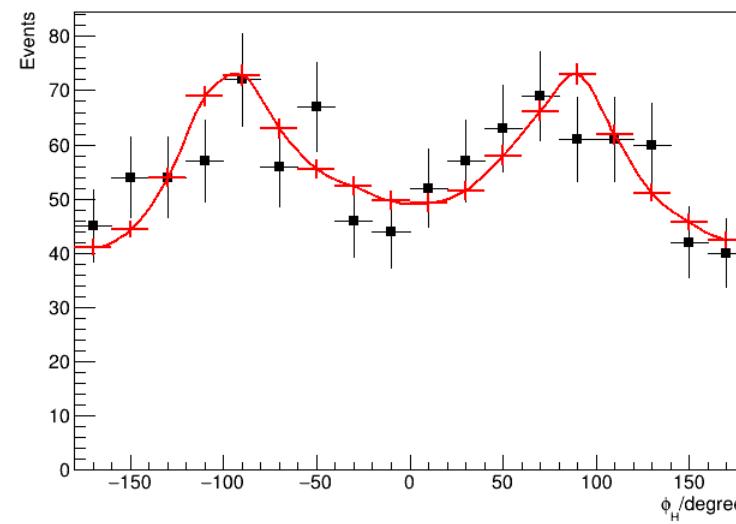
ϕ



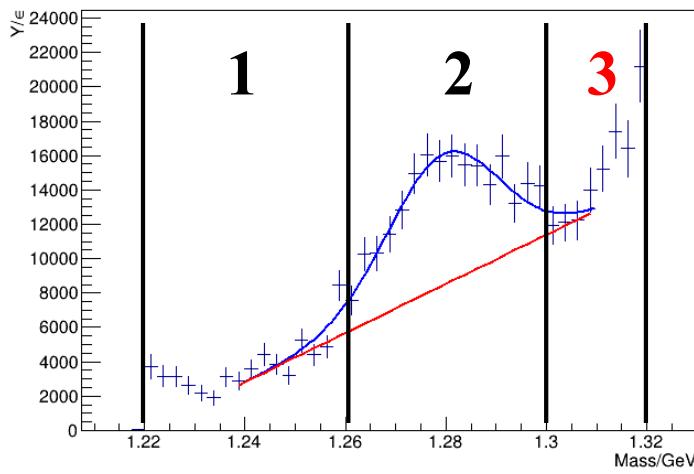
$\cos(\theta_H)$



ϕ_H



Region 3 PWA results



Region 1

| | |
|--|--------------------------------|
| Fit fraction $j=0, l=0, s=0$ | : 0.755485 ± -0.270702 |
| Fit fraction $j=0, l=1, s=1$ | : 0.0458552 ± -0.194178 |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | : $0.0061852 \pm -0.00818622$ |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | : 0.0381819 ± -0.0266231 |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | : 0.0145478 ± -0.0132996 |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | : $0.00891352 \pm -0.00847945$ |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | : 0.0341858 ± -0.025853 |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | : 0.0151747 ± -0.0114261 |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | : 0.0250261 ± -0.0154815 |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | : $0.00637649 \pm -0.00966565$ |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | : 0.0156042 ± -0.0123044 |

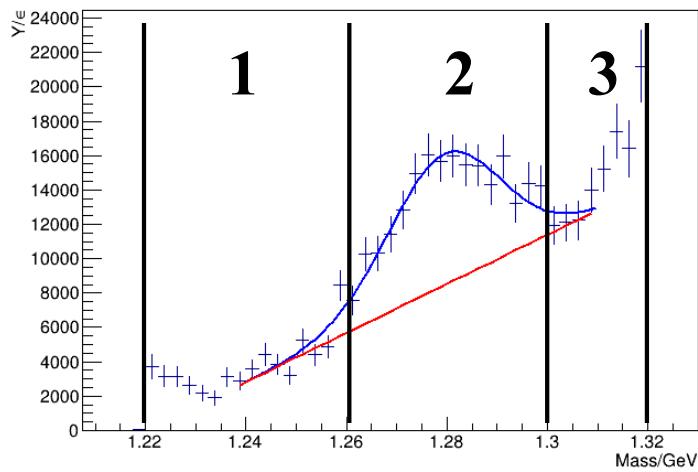
Region 2

| | |
|--|---------------------------------|
| Fit fraction $j=0, l=0, s=0$ | : 0.824834 ± -0.17209 |
| Fit fraction $j=0, l=1, s=1$ | : $0.00481546 \pm -0.0289436$ |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | : $0.00287929 \pm -0.00362665$ |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | : $0.00922431 \pm -0.00378745$ |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | : 0.01217 ± -0.00801337 |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | : $0.00408659 \pm -0.00355879$ |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | : 0.105621 ± -0.0267424 |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | : $0.0028925 \pm -0.00297443$ |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | : $0.000537718 \pm -0.00118739$ |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | : $0.00209243 \pm -0.00381629$ |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | : $0.00314316 \pm -0.00324201$ |

Region 3

| | |
|--|---------------------------------|
| Fit fraction $j=0, l=0, s=0$ | : 0.850564 ± -0.164146 |
| Fit fraction $j=0, l=1, s=1$ | : 0.0104863 ± -0.084152 |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | : 0.0194442 ± -0.0133443 |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | : $0.00899986 \pm -0.00572817$ |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | : 0.0131453 ± -0.0104488 |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | : $0.0115804 \pm -0.00781986$ |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | : 0.072999 ± -0.0413188 |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | : $0.0085873 \pm -0.00689471$ |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | : $0.000705245 \pm -0.00232508$ |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | : $0.00087639 \pm -0.00304636$ |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | : $0.00147296 \pm -0.00319896$ |

PWA over 3 mass regions



Region 1

| | |
|--|--------------------------------|
| Fit fraction $j=0, l=0, s=0$ | $: 0.755485 \pm -0.270702$ |
| Fit fraction $j=0, l=1, s=1$ | $: 0.0458552 \pm -0.194178$ |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | $: 0.0061852 \pm -0.00818622$ |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | $: 0.0381819 \pm -0.0266231$ |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | $: 0.0145478 \pm -0.0132996$ |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | $: 0.00891352 \pm -0.00847945$ |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | $: 0.0341858 \pm -0.025853$ |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | $: 0.0151747 \pm -0.0114261$ |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | $: 0.0250261 \pm -0.0154815$ |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | $: 0.00637649 \pm -0.00966565$ |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | $: 0.0156042 \pm -0.0123044$ |

Region 2

| | |
|--|---------------------------------|
| Fit fraction $j=0, l=0, s=0$ | $: 0.824834 \pm -0.17209$ |
| Fit fraction $j=0, l=1, s=1$ | $: 0.00481546 \pm -0.0289436$ |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | $: 0.00287929 \pm -0.00362665$ |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | $: 0.00922431 \pm -0.00378745$ |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | $: 0.01217 \pm -0.00801337$ |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | $: 0.00408659 \pm -0.00355879$ |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | $: 0.105621 \pm -0.0267424$ |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | $: 0.0028925 \pm -0.00297443$ |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | $: 0.000537718 \pm -0.00118739$ |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | $: 0.00209243 \pm -0.00381629$ |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | $: 0.00314316 \pm -0.00324201$ |

Region 3

| | |
|--|---------------------------------|
| Fit fraction $j=0, l=0, s=0$ | $: 0.850564 \pm -0.164146$ |
| Fit fraction $j=0, l=1, s=1$ | $: 0.0104863 \pm -0.084152$ |
| Fit fraction $j=1, l=1, s=0, m_j = -1$ | $: 0.0194442 \pm -0.0133443$ |
| Fit fraction $j=1, l=1, s=0, m_j = 0$ | $: 0.00899986 \pm -0.00572817$ |
| Fit fraction $j=1, l=1, s=0, m_j = 1$ | $: 0.0131453 \pm -0.0104488$ |
| Fit fraction $j=1, l=0, s=1, m_j = -1$ | $: 0.0115804 \pm -0.00781986$ |
| Fit fraction $j=1, l=0, s=1, m_j = 0$ | $: 0.072999 \pm -0.0413188$ |
| Fit fraction $j=1, l=0, s=1, m_j = 1$ | $: 0.0085873 \pm -0.00689471$ |
| Fit fraction $j=1, l=1, s=1, m_j = -1$ | $: 0.000705245 \pm -0.00232508$ |
| Fit fraction $j=1, l=1, s=1, m_j = 0$ | $: 0.00087639 \pm -0.00304636$ |
| Fit fraction $j=1, l=1, s=1, m_j = 1$ | $: 0.00147296 \pm -0.00319896$ |

Title

