

# Search for Excited $E$ states and Preliminary Cross Section for $E(1530)$

Brandon Sumner



# Outline

- Preliminary total  $E^{*-}(1530)$  cross section
- PWA of the  $E(1530)$

Preliminary  $E^{*-}(1530) \rightarrow E^{-}\pi^0$  cross  
section

# Decay chain

$$\gamma p \rightarrow K^+ K^+ \Xi^{-*}$$

$$\Xi^{-*} \rightarrow \Xi^- \pi^0$$

$$\Xi^- \rightarrow \Lambda \pi^-$$

Note:  $\pi^0 \rightarrow \gamma\gamma$  and  $\Lambda \rightarrow p\pi$

# Decay chain

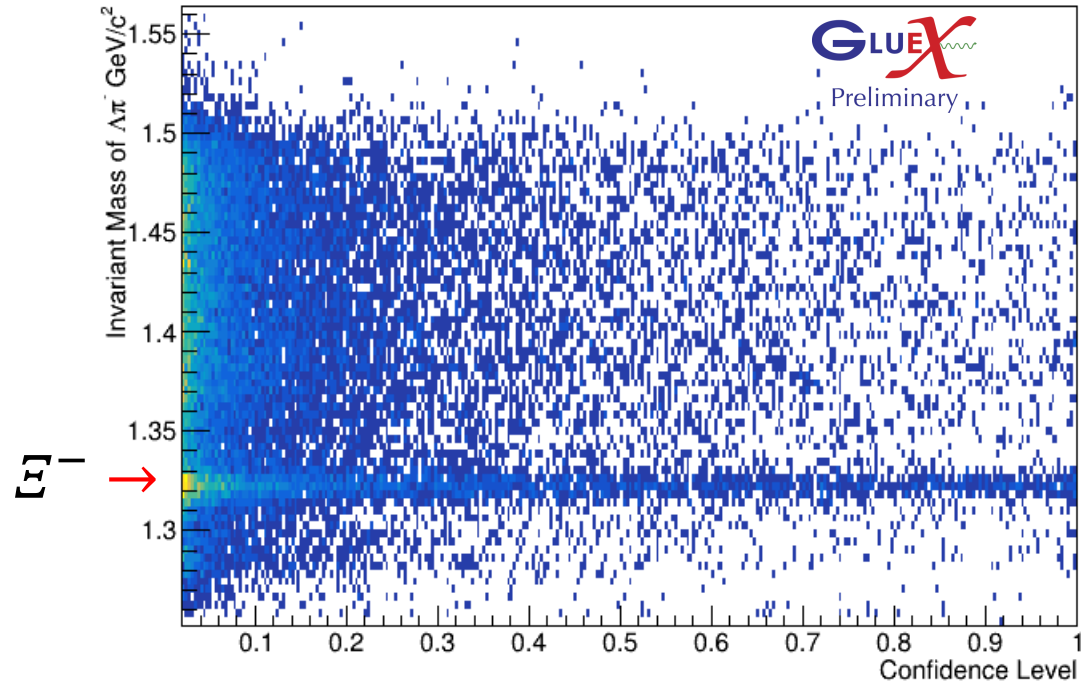
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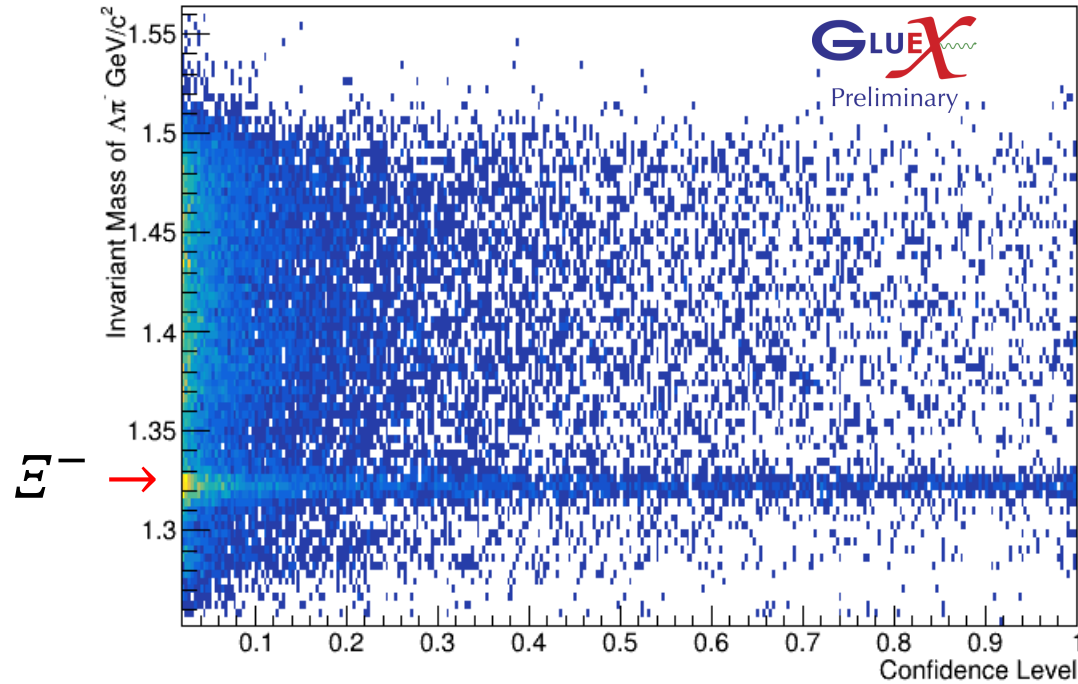
$$\Xi^- \rightarrow \Lambda \pi^-$$

- The masses of  $\Lambda$  and  $\pi$ 's are constrained to the known masses in the kinematic fit.
- To remove the background associated with low confidence level an analysis cut of confidence level above  $10^{-4}$  was made

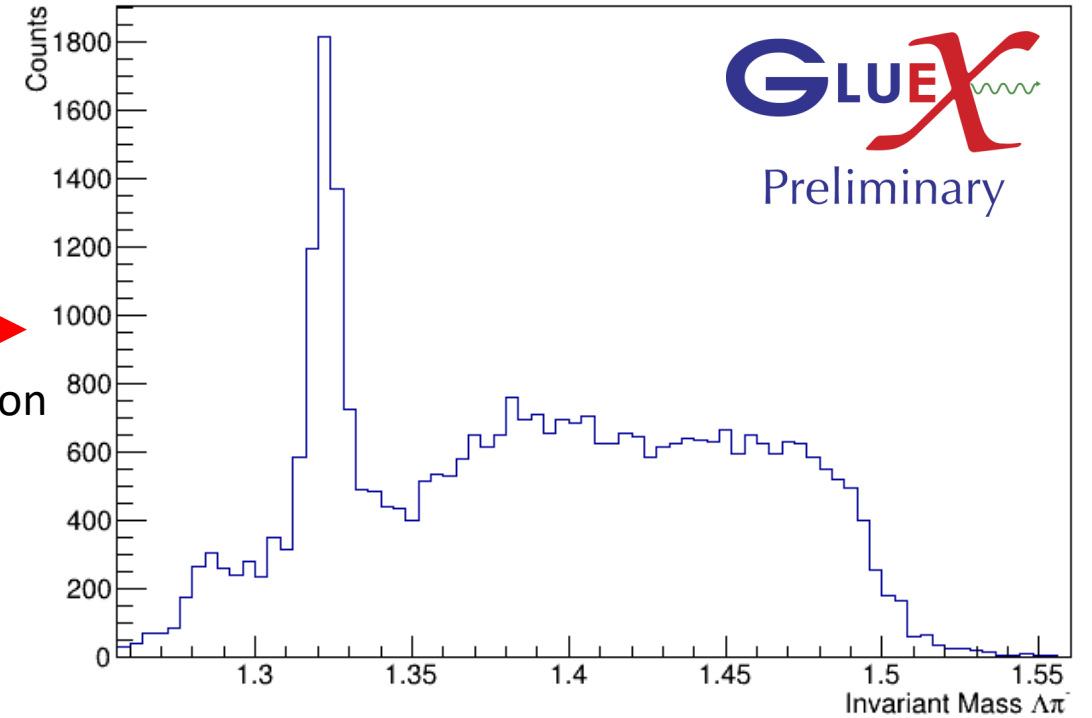
# $E^-$ Invariant mass selection



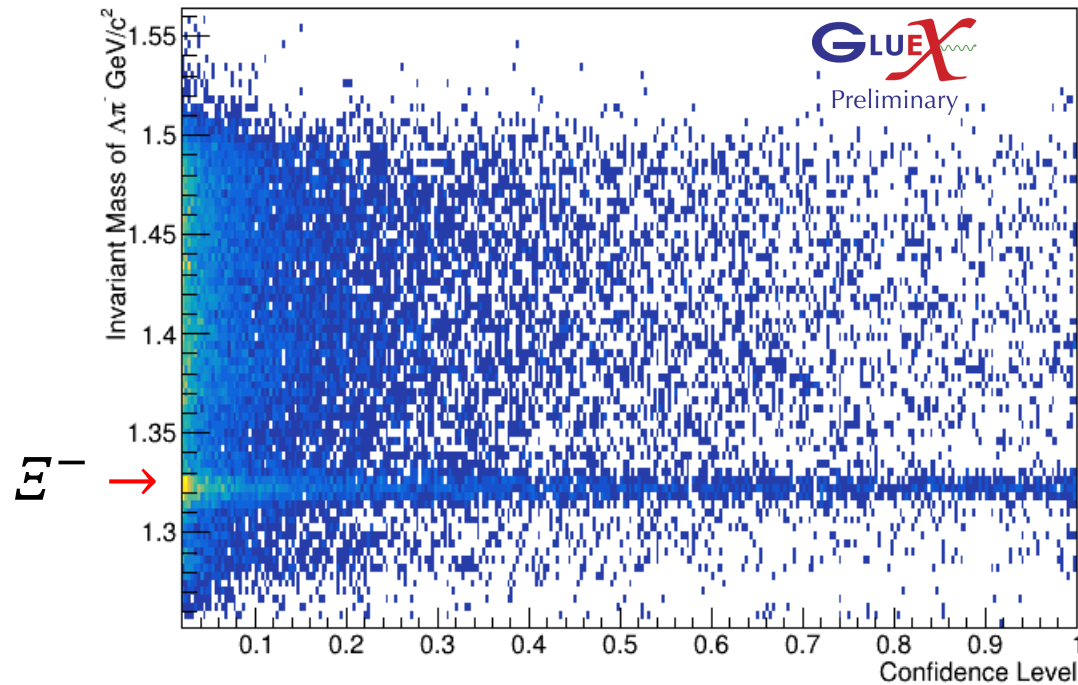
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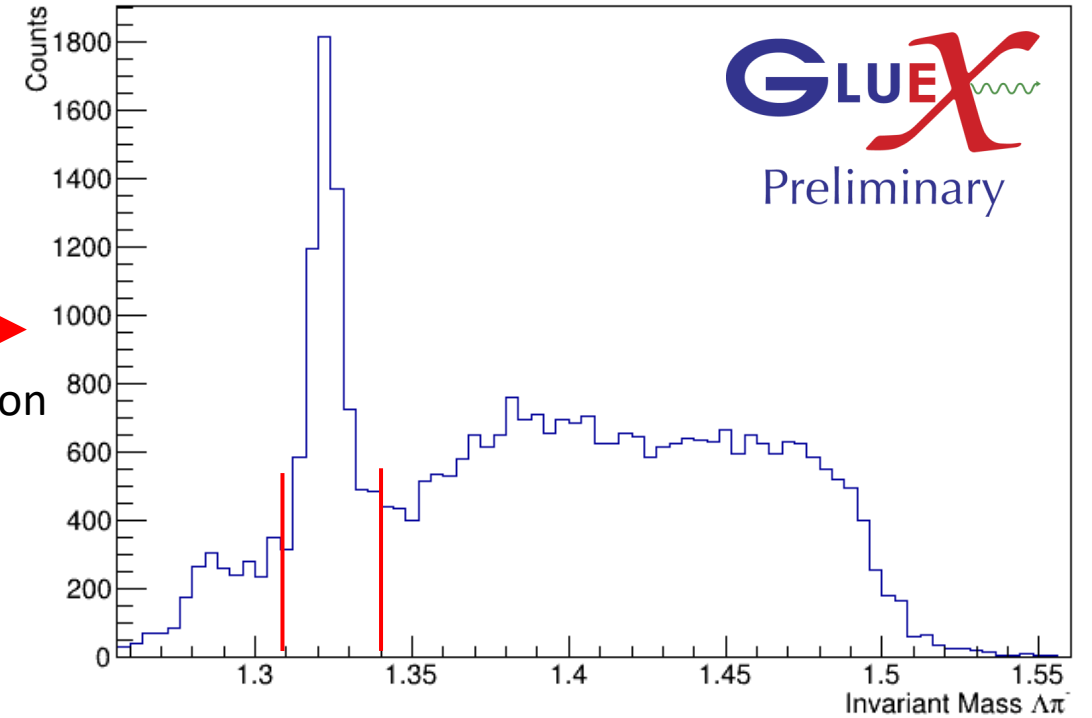
→  
Y-Projection



# $E^-$ Invariant mass selection



→  
Y-Projection



- Cut around the signal of the ground state cascade



# Background contamination from $K^*$

- From the combinatorics of all final state particles, there can be an incorrectly linked  $K^*$  meson associated with the reaction

$$\gamma p \rightarrow K^+ K^+ \Xi^{-*}$$

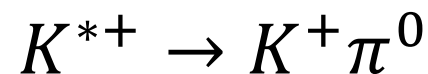
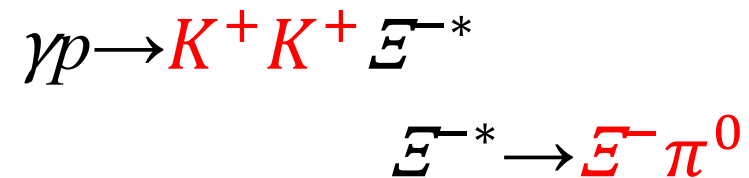
$$\Xi^{-*} \rightarrow \Xi^- \pi^0$$

$$\gamma p \rightarrow K^+ (K^+ \pi^0) \Xi^-$$

$$K^{*+} \rightarrow K^+ \pi^0$$

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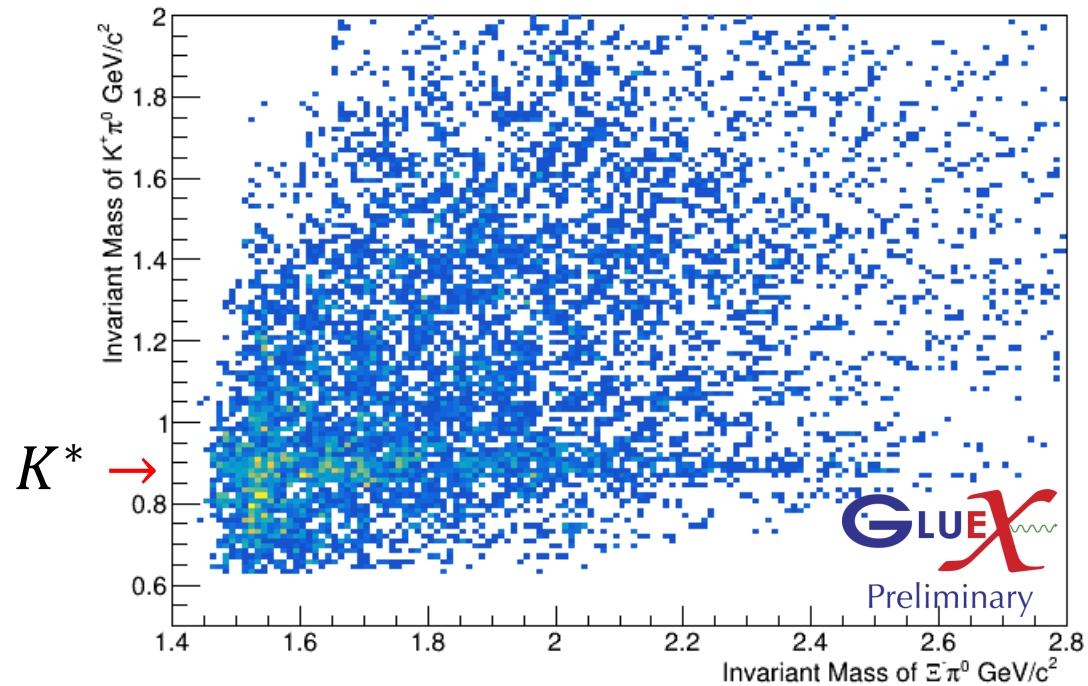
$$\gamma p \rightarrow K^+ K^+ \Xi^{-*}$$

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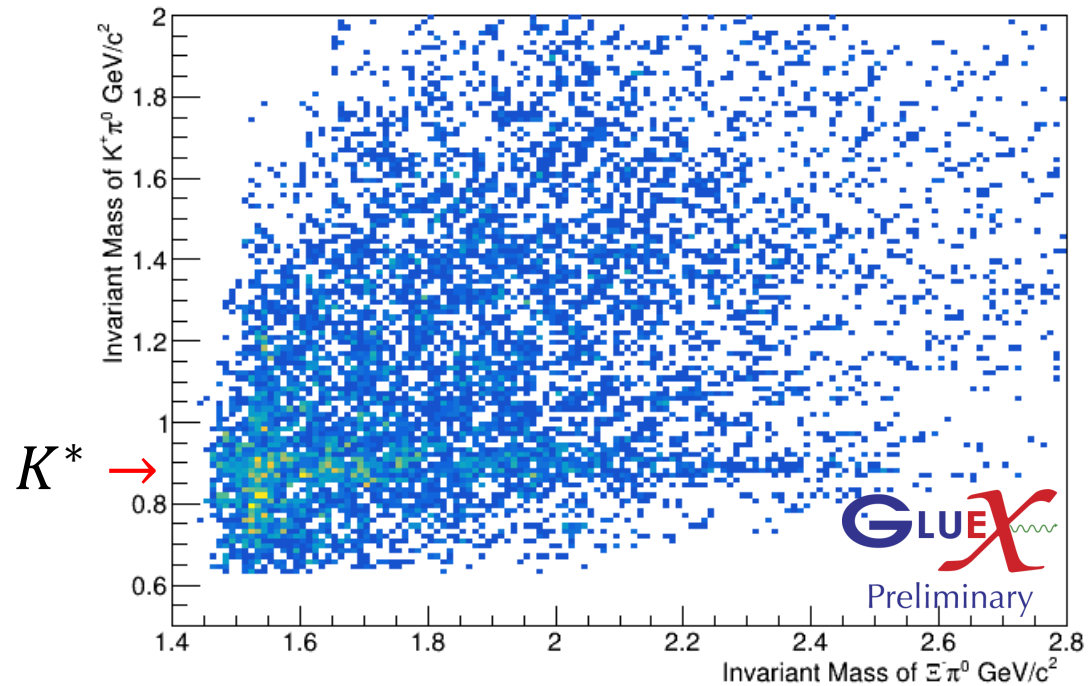
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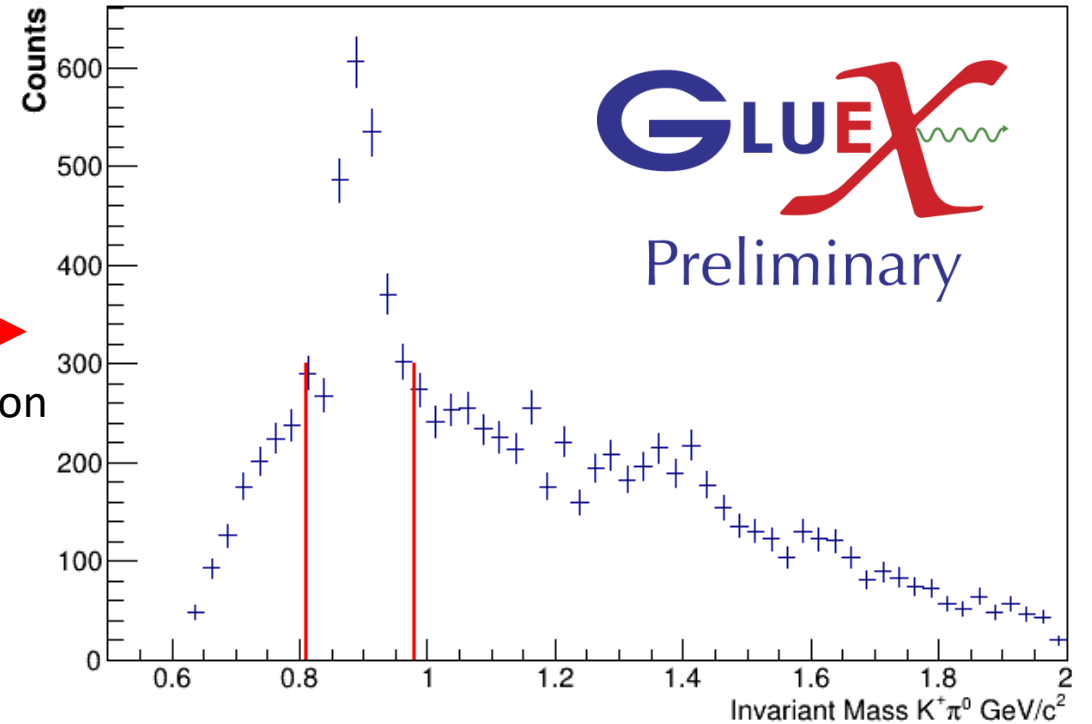
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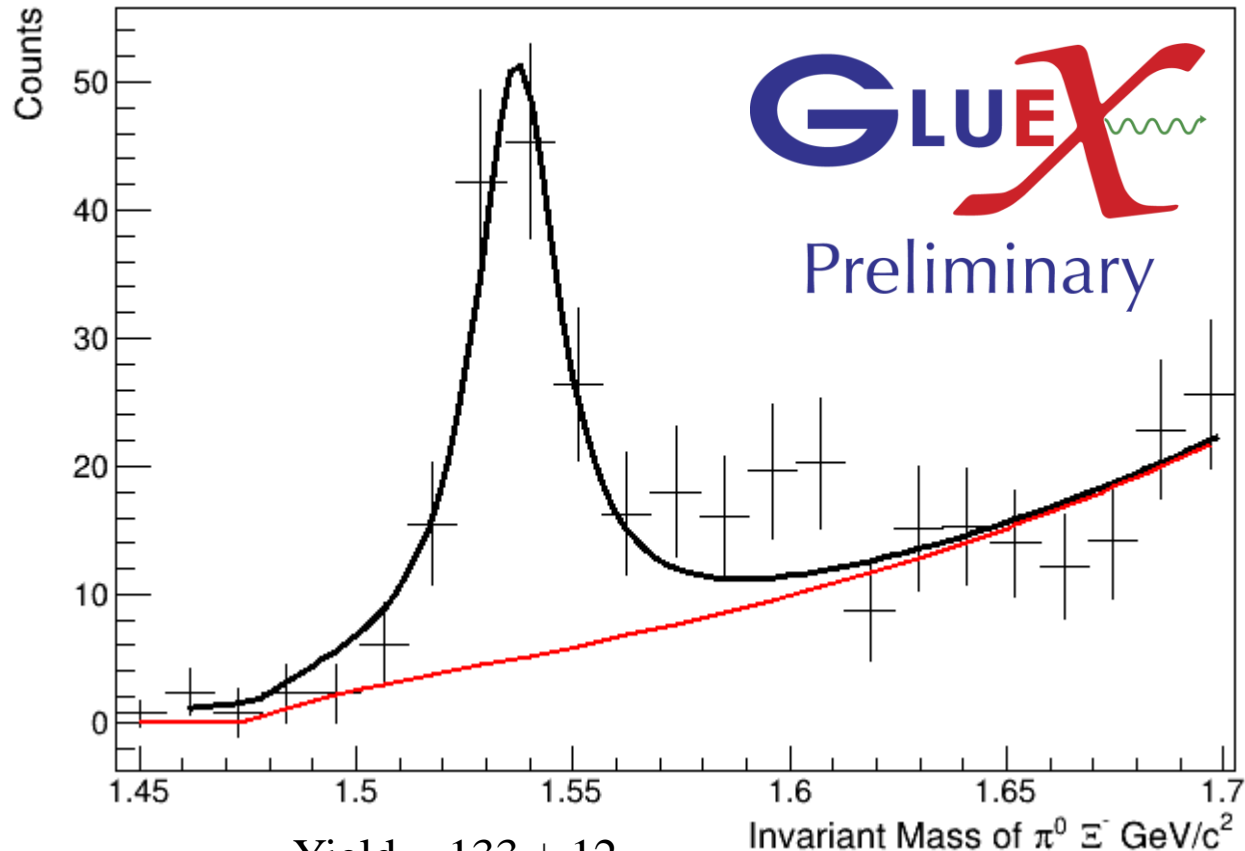
→  
Y-Projection



- Reject events associated with  $K^* \rightarrow K^+\pi^0$  contamination

# Excited Cascade 1530 Reconstruction

~1/2 GlueX Phase 1 Dataset



Yield =  $133 \pm 12$

Center =  $1.537(2) \text{ GeV}/c^2$

Width =  $12(3) \text{ MeV}/c^2$

$\Xi(1530) 3/2^+$

$$I(J^P) = \frac{1}{2}(\frac{3}{2}^+)$$

$\Xi(1530)^0$  mass  $m = 1531.80 \pm 0.32 \text{ MeV}$  ( $S = 1.3$ )

$\Xi(1530)^-$  mass  $m = 1535.0 \pm 0.6 \text{ MeV}$

$\Xi(1530)^0$  full width  $\Gamma = 9.1 \pm 0.5 \text{ MeV}$

$\Xi(1530)^-$  full width  $\Gamma = 9.9^{+1.7}_{-1.9} \text{ MeV}$

$\Xi(1530)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$P$ (MeV/c)
$\Xi \pi$	100 %		158
$\Xi \gamma$	<4 %	90%	202

# Modeling the cascade production in signal MC

- Theoretical Calculations done by Nakayama, Oh and Haberzettl proposed the cascade/excited cascade are produced by a two-step process:

$$\gamma p \rightarrow K^+ Y^*$$

$$Y^* \rightarrow K^+ \Xi^{-*}$$

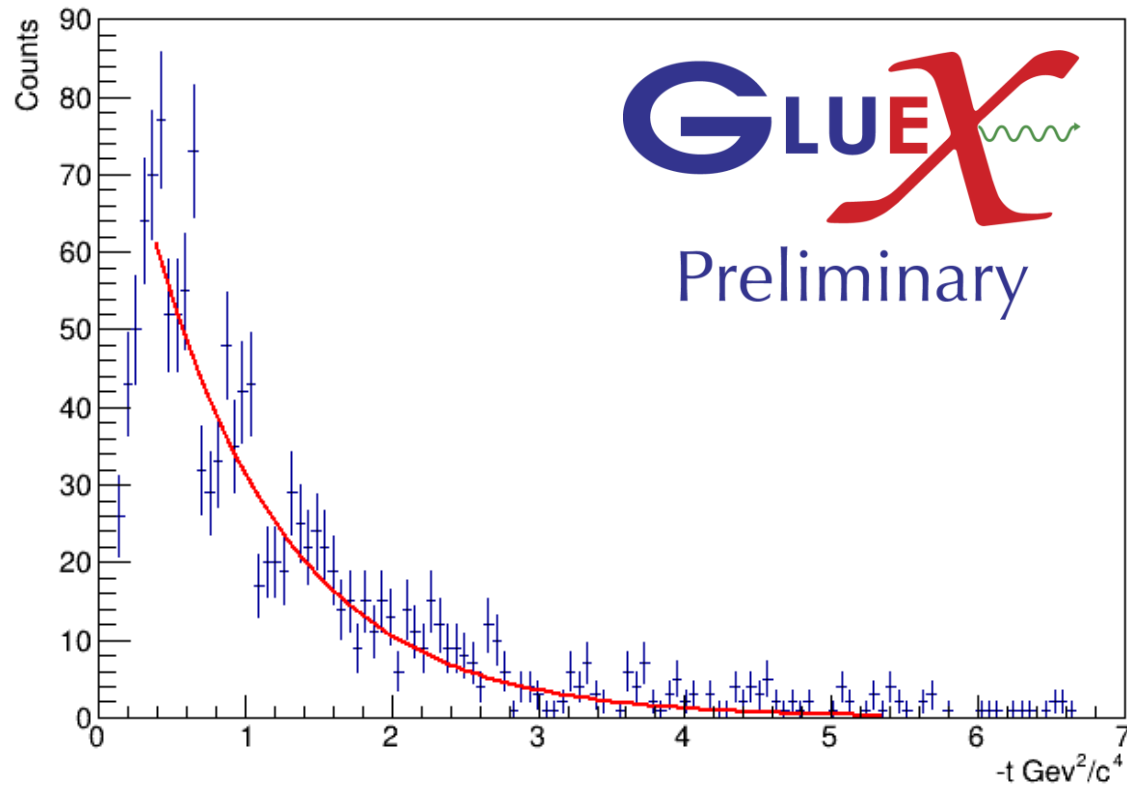
- Direct production of the  $\Xi^{-*}$  would be OZI suppressed with two strange- antistrange pairs at the production vertex. Therefore, I defined  $t$  as  $t = (P_\gamma - P_{K^+})^2$

# *t*-Slope extraction

- Selecting events within the excited cascade 1530 peak

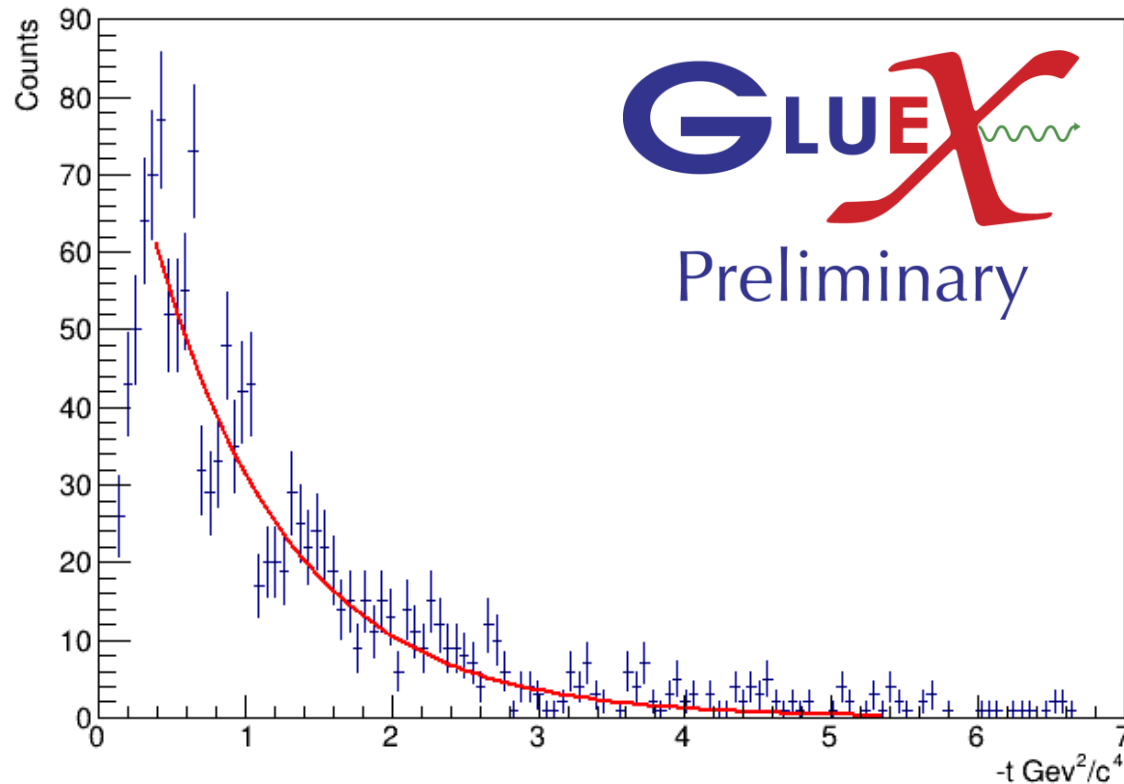


# $t$ -Slope extraction



- Selecting events within the excited cascade 1530 peak
- Assuming :  $\frac{d\sigma}{dt} \propto e^{-bt}$

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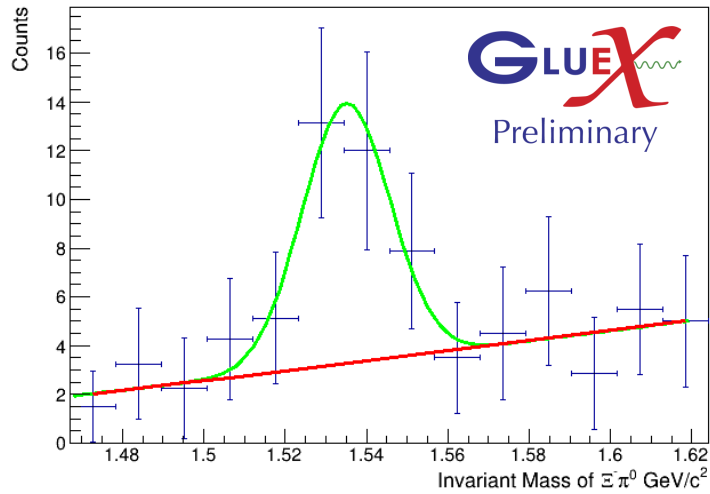
- Selecting events within the excited cascade 1530 peak

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$$b = 1.08(4)/\text{GeV}^2$$

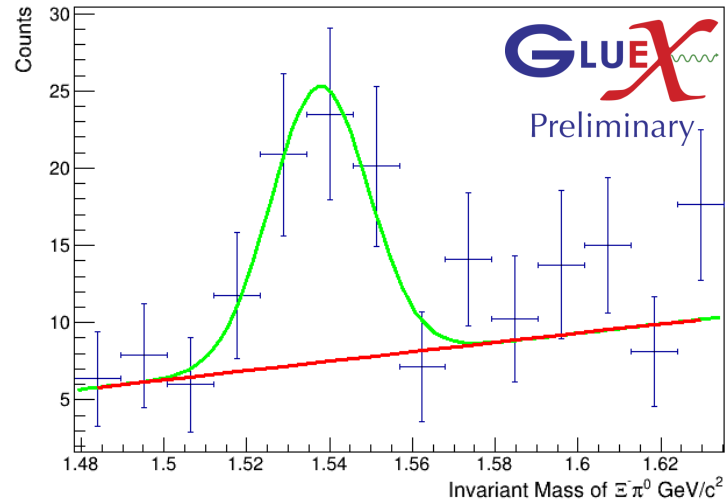
# Energy-dependent $\Xi(1530)$ Yield Extraction

Spring 18 Dataset w/Beam Energy 7400MeV



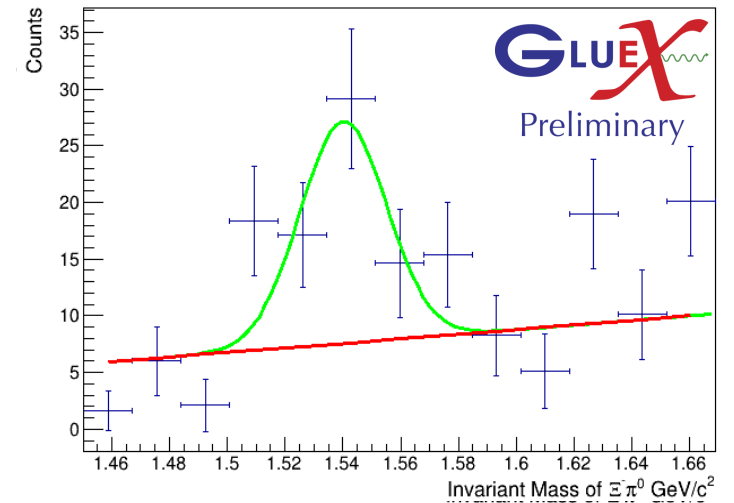
Yield =  $25 \pm 5$

Spring 18 Dataset w/Beam Energy 8200MeV



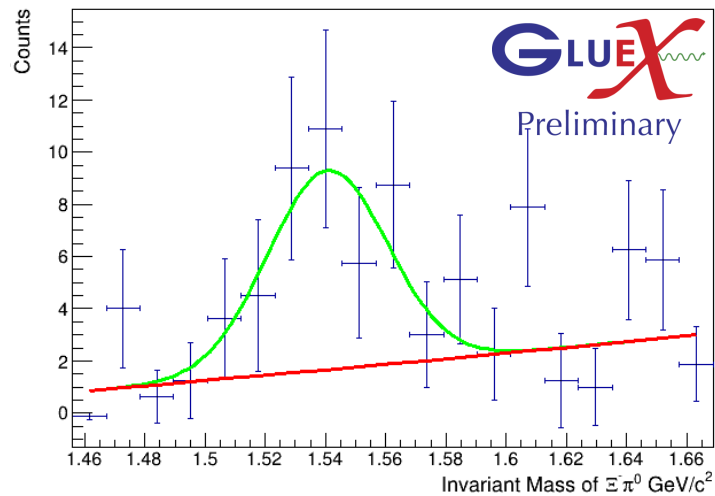
Yield =  $51 \pm 7$

Spring 18 Dataset w/Beam Energy 9000MeV



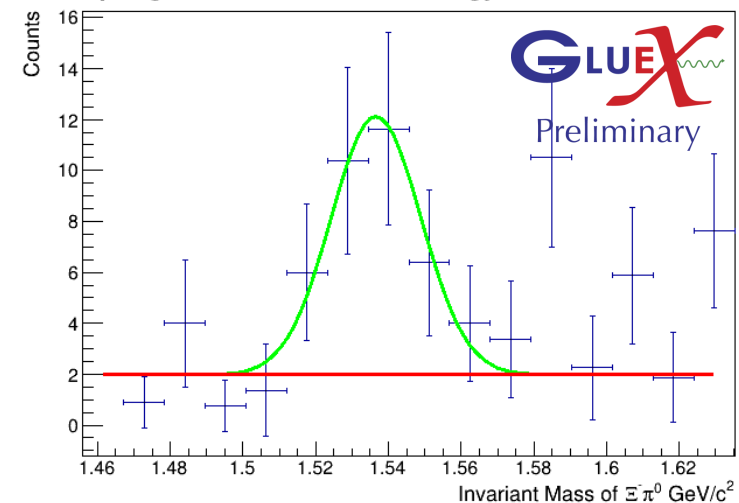
Yield =  $52 \pm 7$

Spring 18 Dataset w/Beam Energy 9800MeV



Yield =  $37 \pm 6$

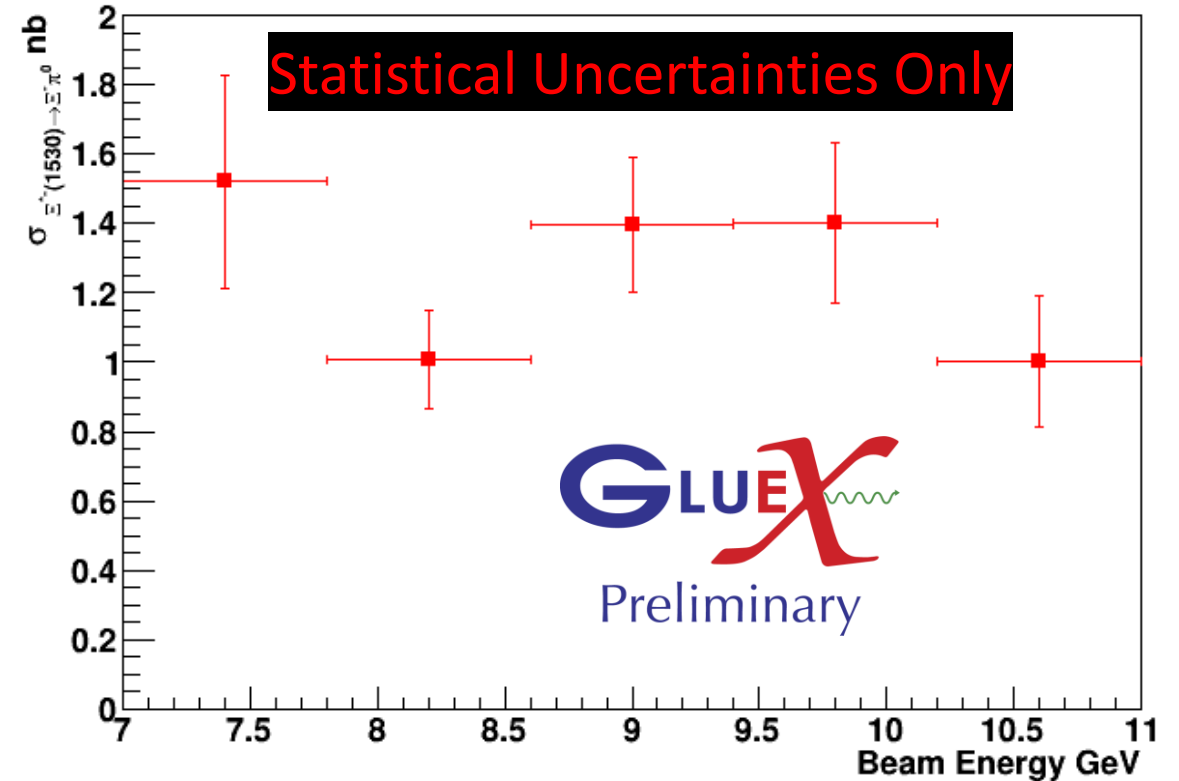
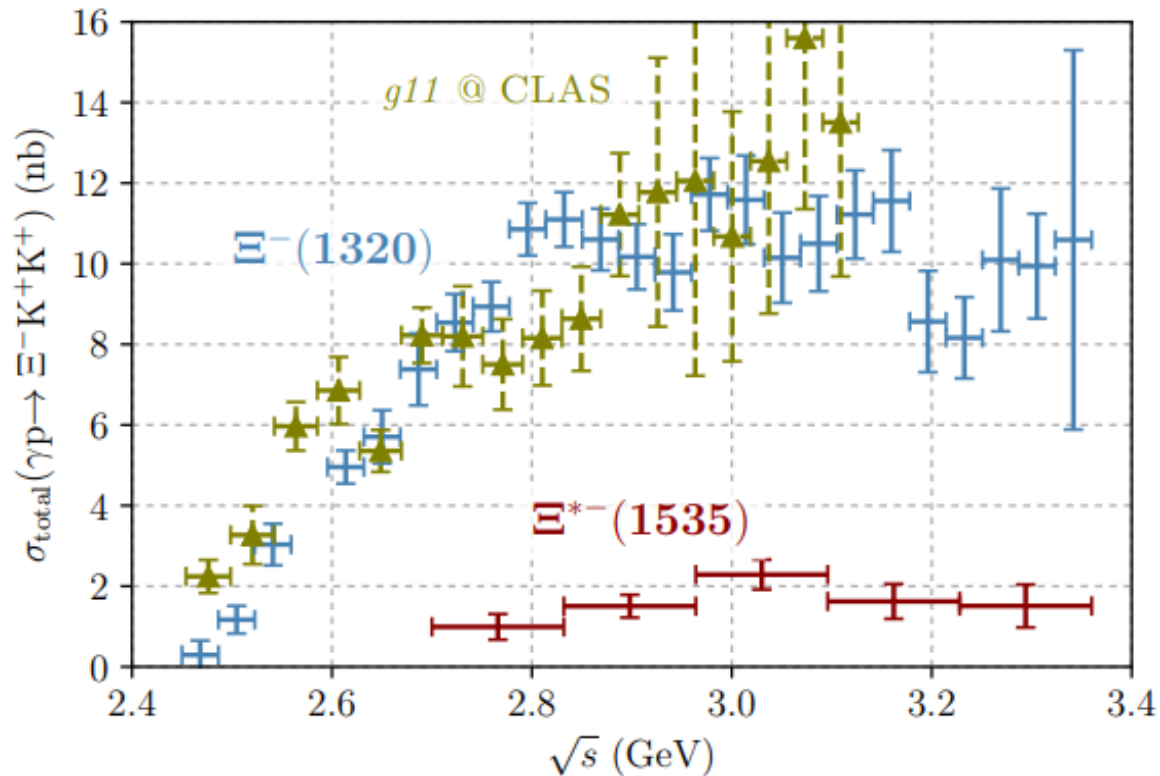
Spring 18 Dataset w/Beam Energy 10600MeV



Yield =  $28 \pm 5$



# Cross sections for cascade baryons



“Upper limits were calculated on the production total cross sections of the three best-known excited states: the  $E(1690)$ , the  $E(1820)$  and the  $E(1950)$  [7] at 0.75 nb, 1.01 nb, and 1.58 nb, respectively”  
 -Study of  $E$  Photoproduction from threshold to  $W = 3.3$  GeV via CLAS collaboration

Preliminary total  $\Xi^{*-}$  (1530) cross section



# Decay chain

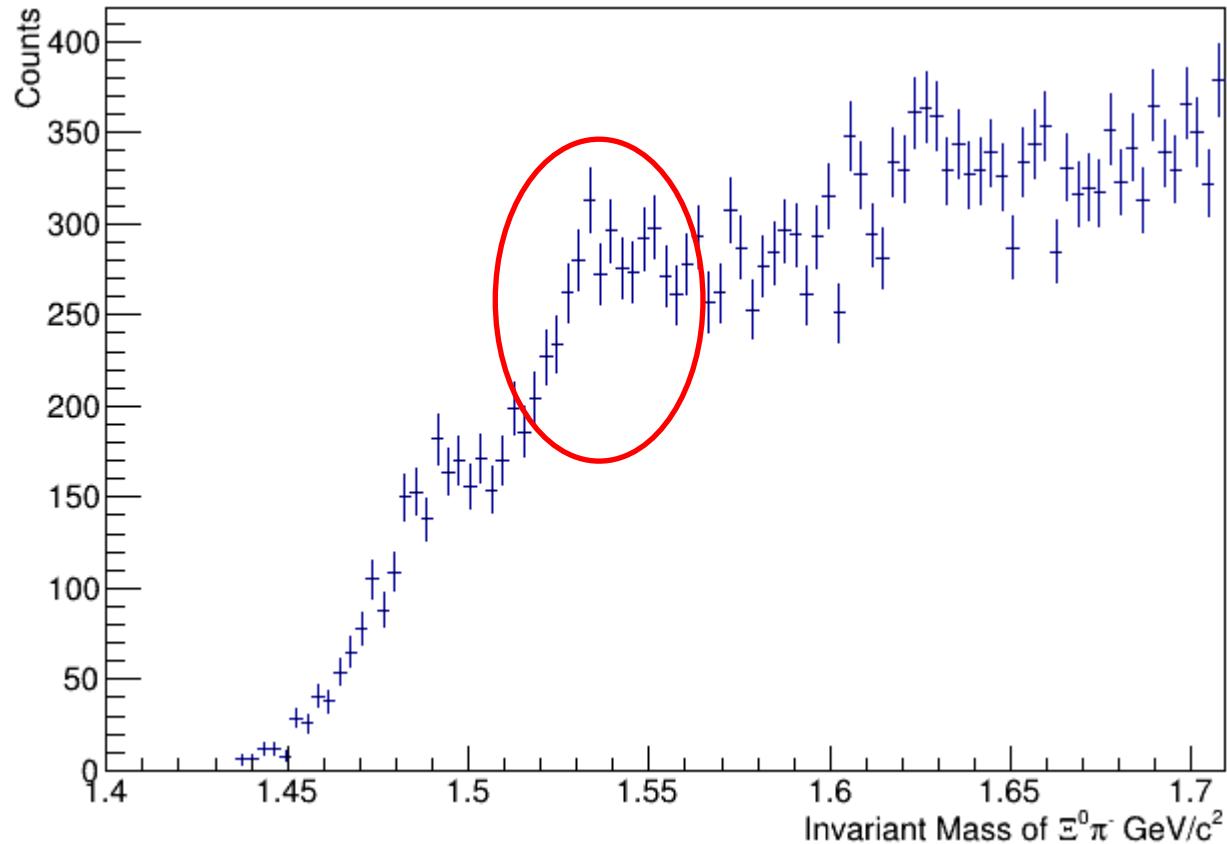
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$$\Xi^0 \rightarrow \Lambda \pi^0$$

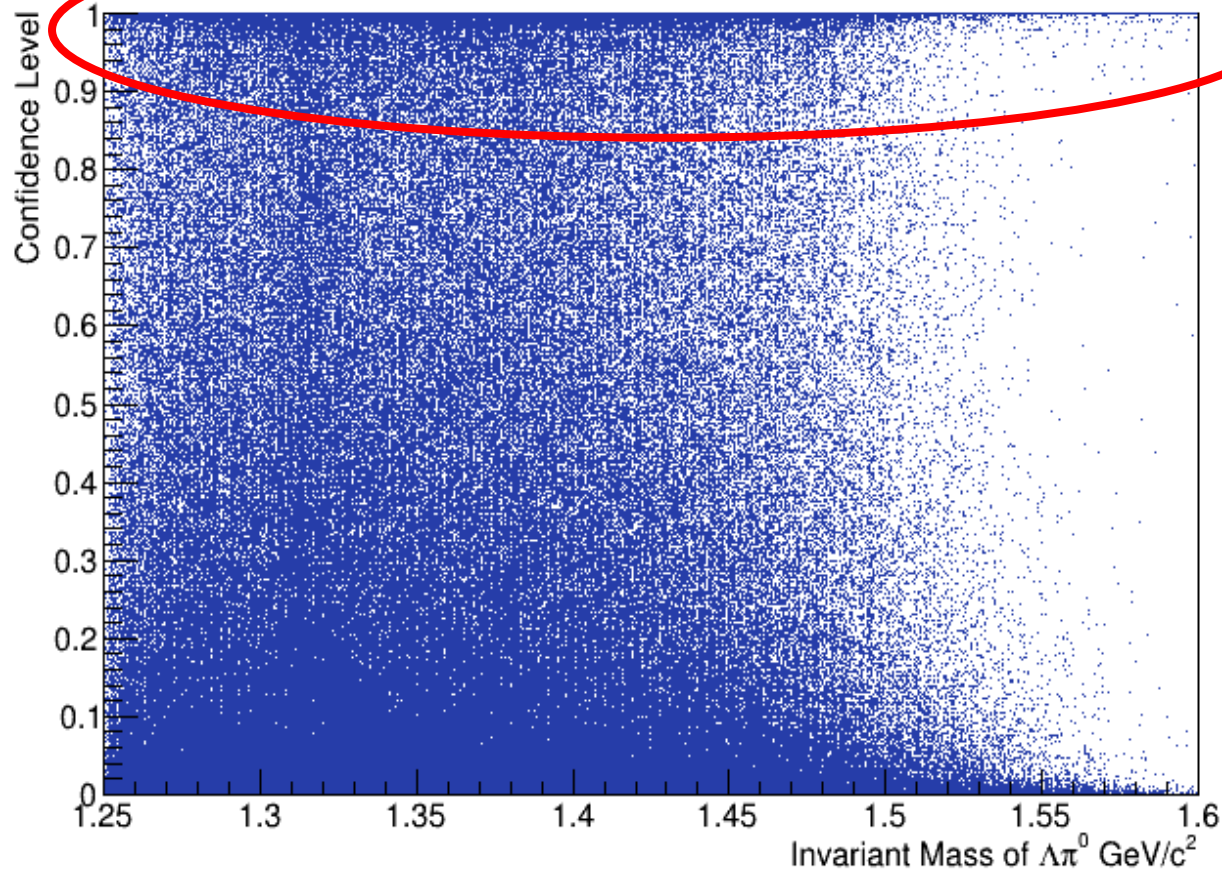
- Where the  $\Lambda$  and  $\pi$ 's are kinematically constrained but does not use vertex fitting

# Reconstructed $\Xi^{*-}(1530) \rightarrow \Xi^0 \pi^-$ w/o vertex fitting



- The above plot uses a confidence level above  $10^{-3}$  and invariant mass restriction on the  $\Lambda \pi^0$  system

# Issues w/Vertex fitting



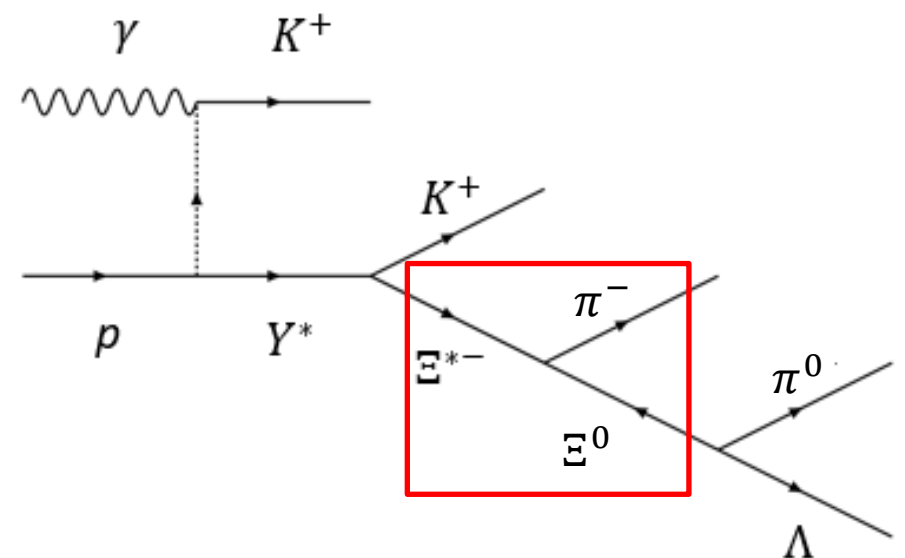
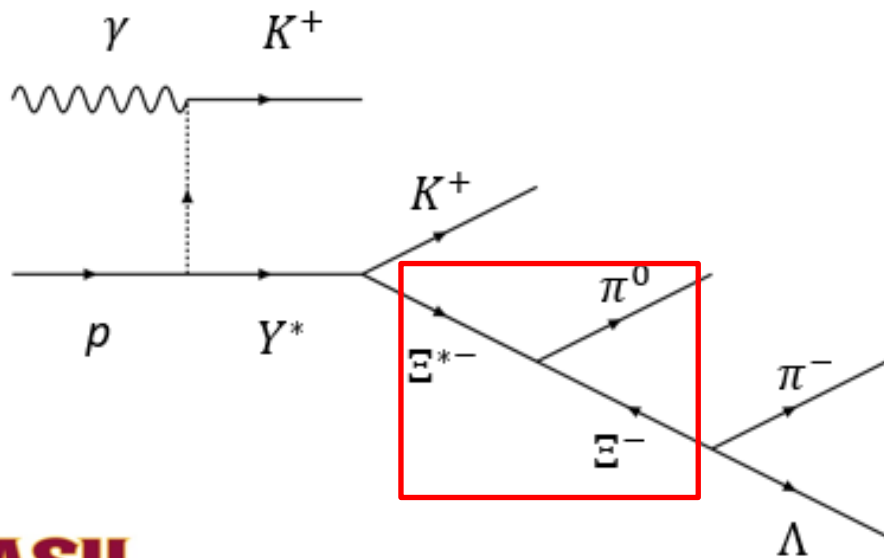
- Large contamination of misidentified particles at high confidence level
- The issues originates from the two neutrals come from the same vertex



# Clebsch Gordan study of $\Xi^0\pi^-$ channel

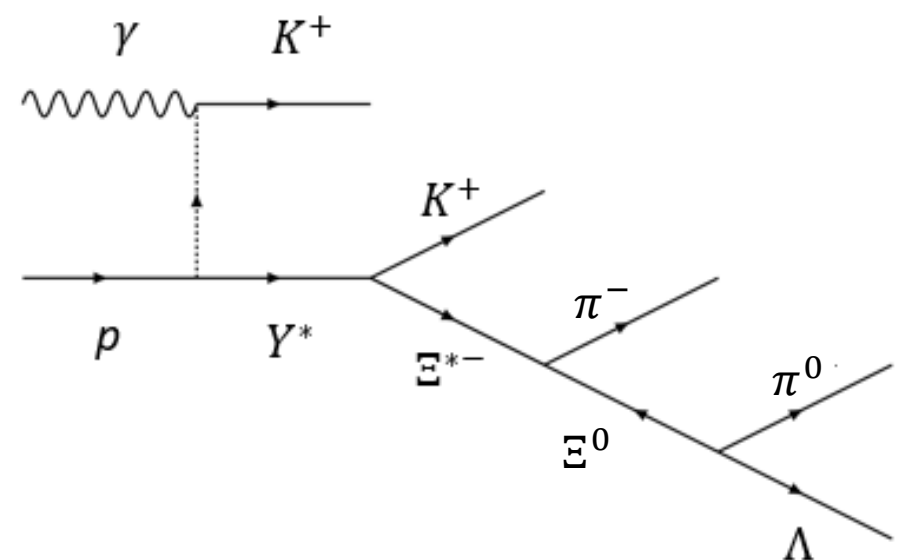
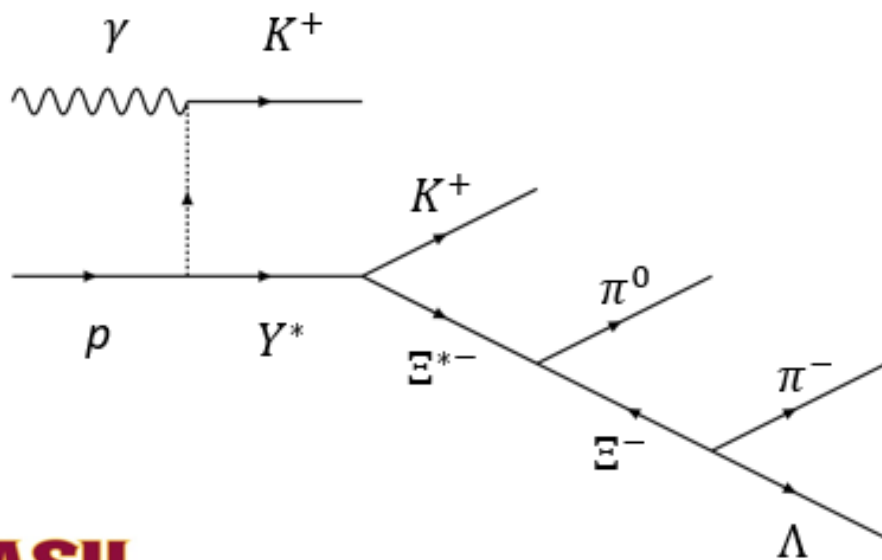
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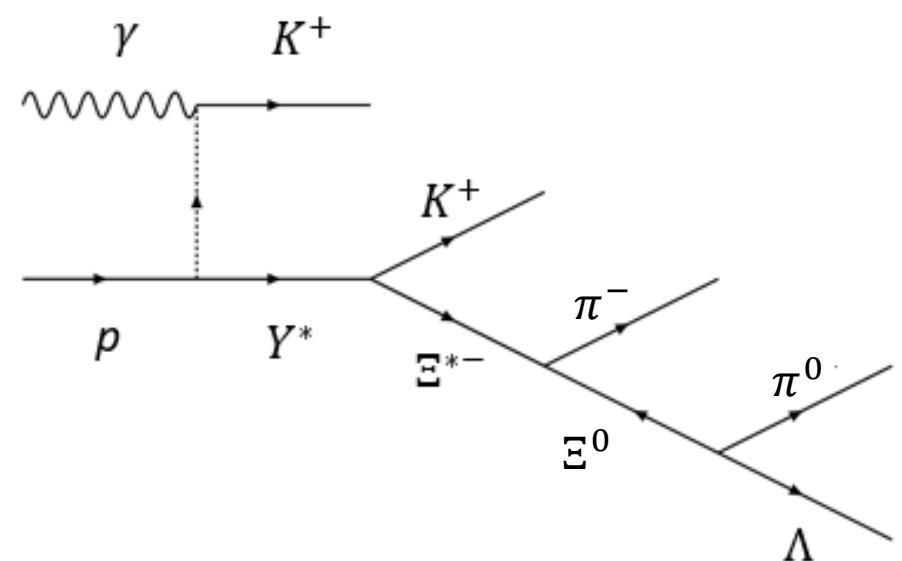
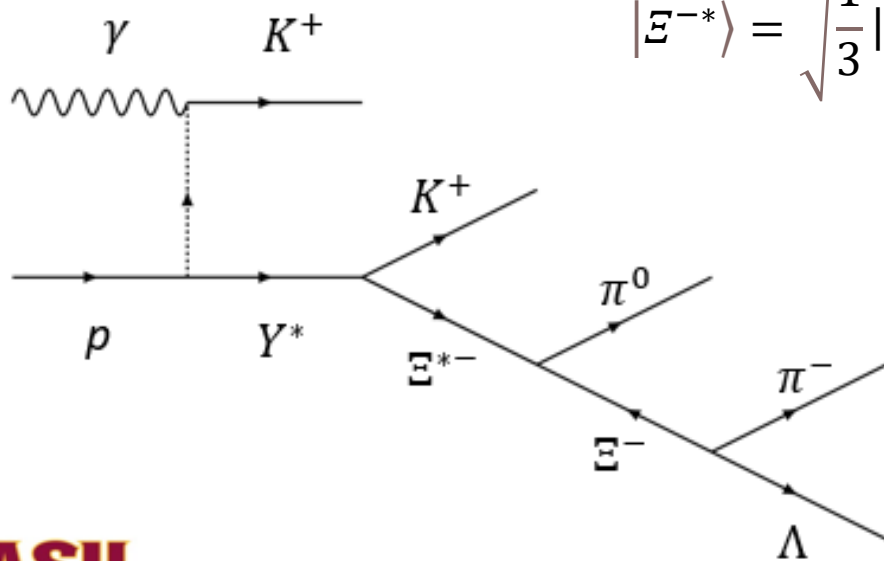


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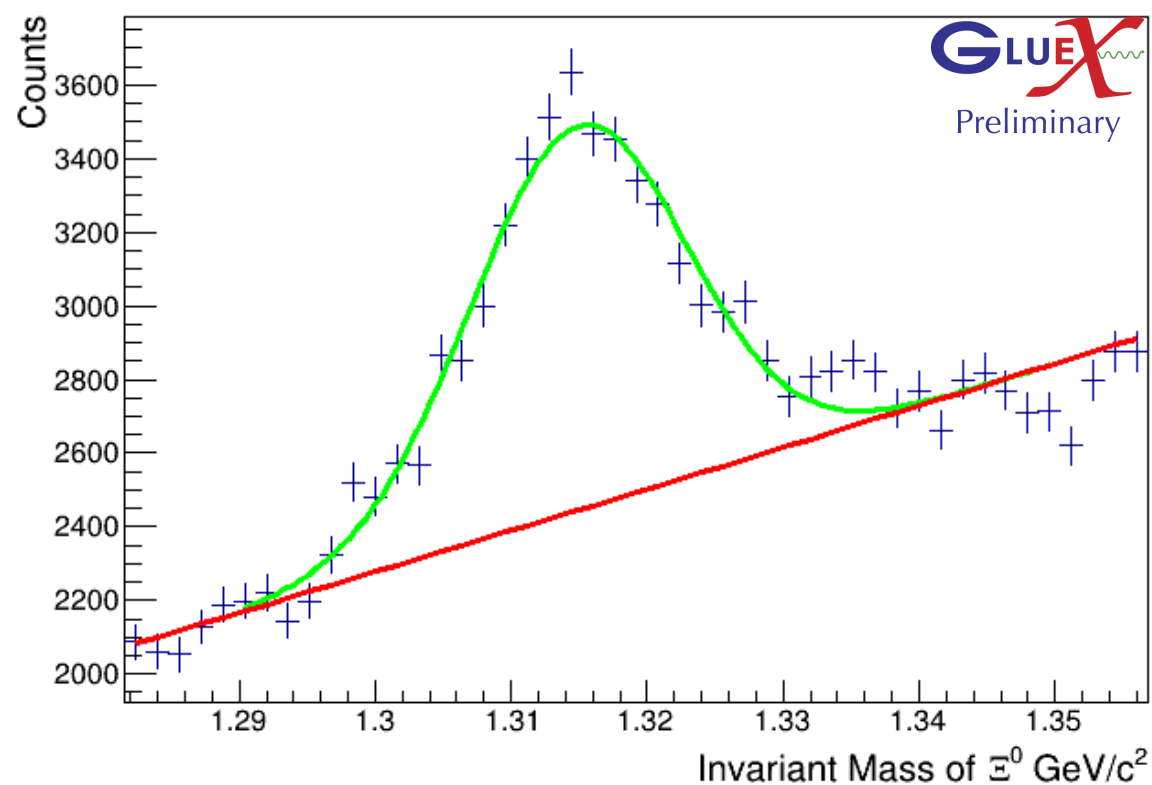
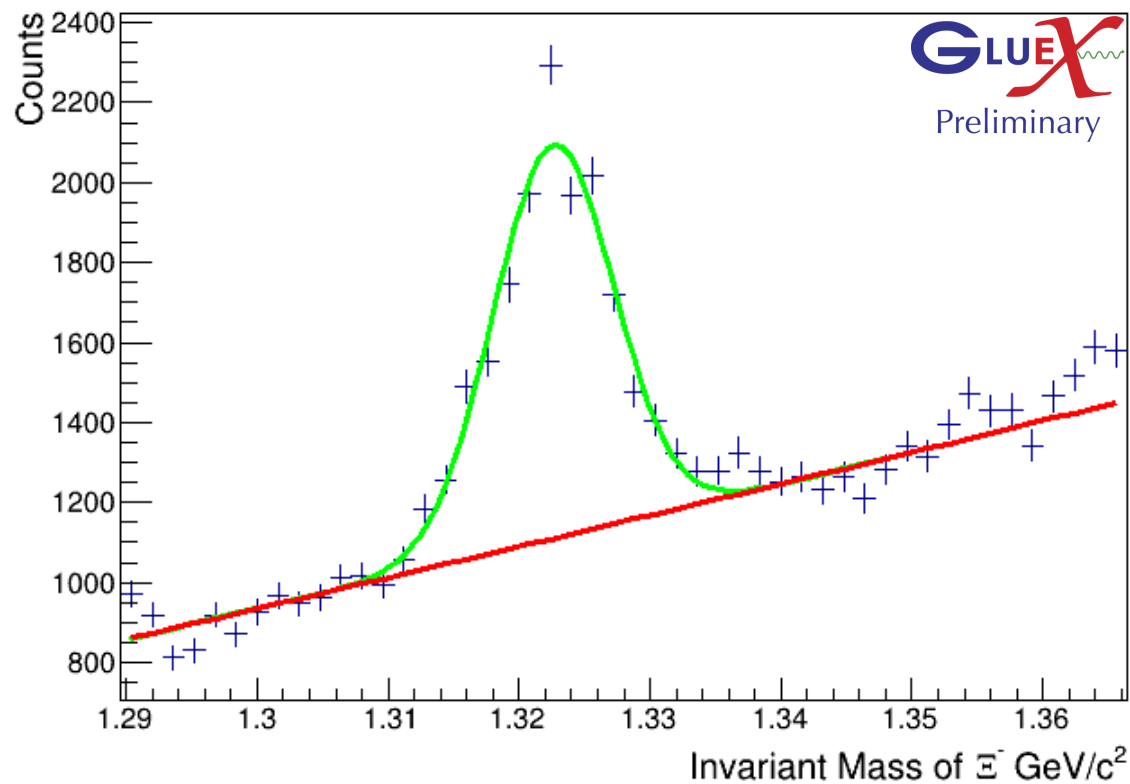
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$$\left| \frac{1}{2}, -\frac{1}{2} \right\rangle = \sqrt{\frac{1}{3}} \left[ |1, 0\rangle \left| \frac{1}{2}, -\frac{1}{2} \right\rangle \right] - \sqrt{\frac{2}{3}} \left[ |1, -1\rangle \left| \frac{1}{2}, \frac{1}{2} \right\rangle \right],$$

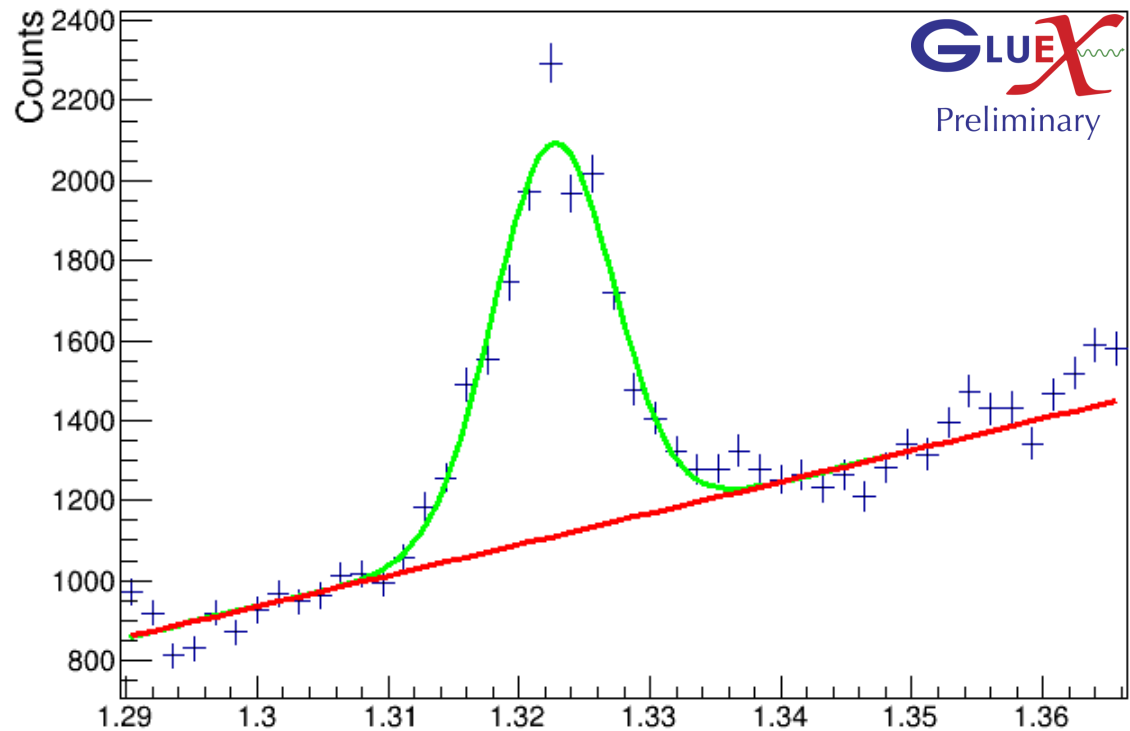
$$|\Xi^{*-}\rangle = \sqrt{\frac{1}{3}} |\pi^0 \Xi^-\rangle - \sqrt{\frac{2}{3}} |\pi^- \Xi^0\rangle$$



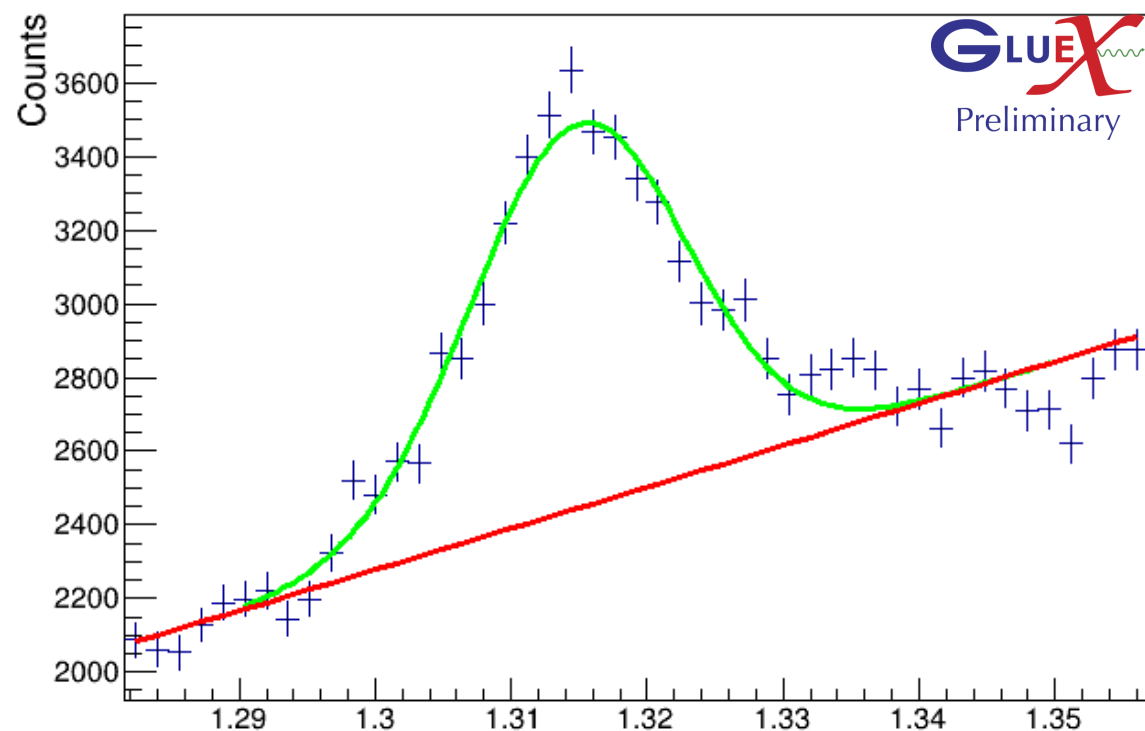
# Yields from $\Xi^0$ and $\Xi^-$ w/o vertex fitting w/CL above $10^{-3}$



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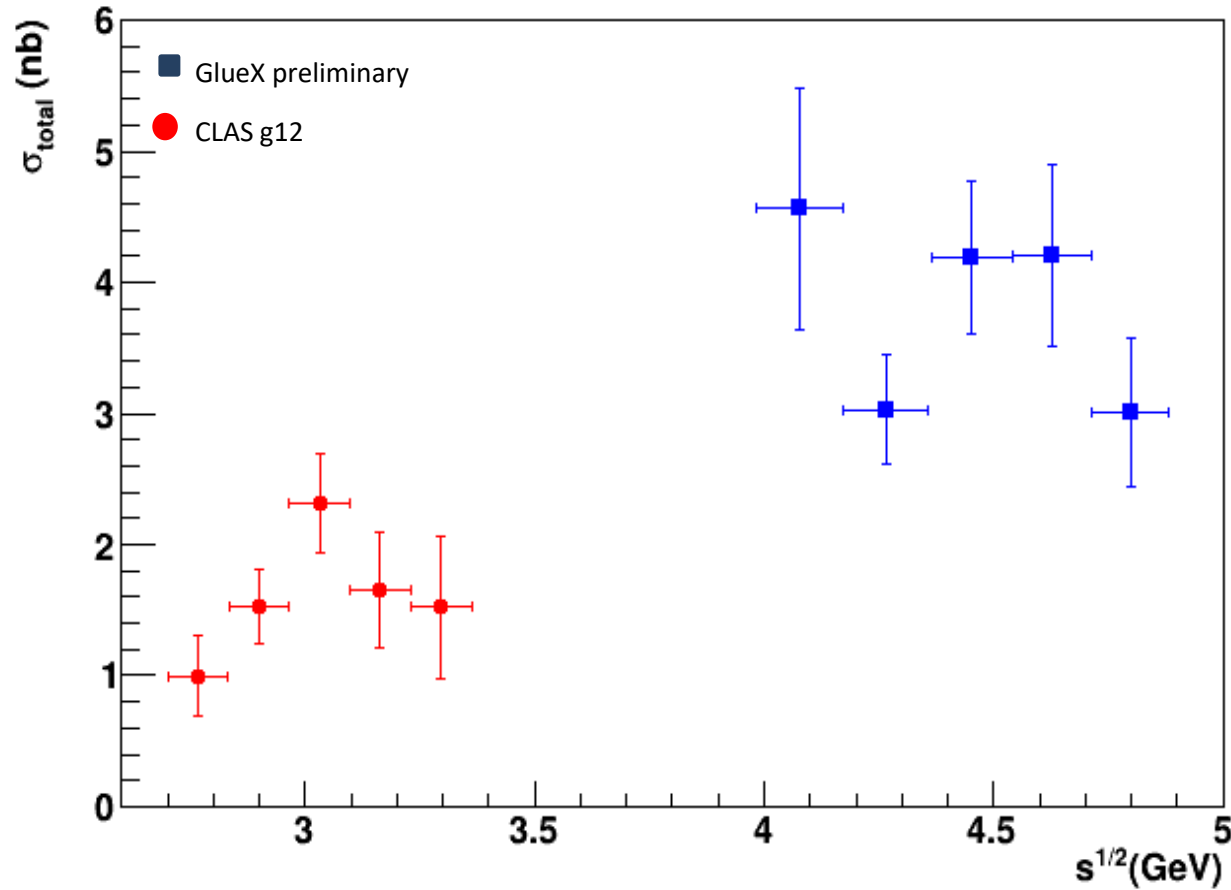
Yield( $\Xi^-$ ) =  $7270 \pm 85$



Yield( $\Xi^0$ ) =  $13351 \pm 116$

$$\frac{N[\Xi^-(1320)]}{N[\Xi^0(1320)]} = 0.54(2)$$

# Preliminary total cross section for $\Xi^{*-}(1530) \rightarrow \Xi\pi$



$$\sigma_T = \sigma_{\Xi^-\pi^0} + \sigma_{\Xi^0\pi^-}$$

$$\sigma_{\Xi^0\pi^-} = 2.0 \sigma_{\Xi^-\pi^0},$$

$$\sigma_T = 3.0 \sigma_{\Xi^-\pi^0}.$$

# Partial Wave Analysis (PWA) of the $E(1530)$



# PWA

- The PWA is performed by selecting a specific frame of reference, extracting the efficiency corrected yields of the  $E(1530)$  in bins of  $\cos(\theta_{GJ})$  and fit the resulting efficiency corrected yield distribution to the intensity function.

# Intensity function

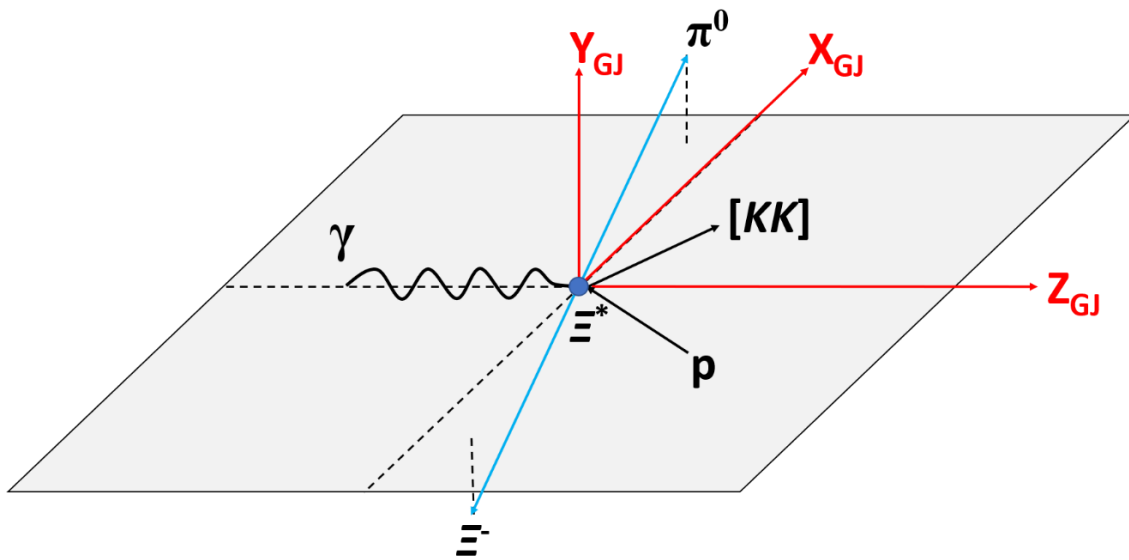
- The intensity function is given by

$$I(\tau) \equiv \sum_{i,j} \sum_{b,b'} {}^i A_b(\tau) {}^{i,j} \rho_{b,b'} {}^j A_{b'}^*(\tau)$$

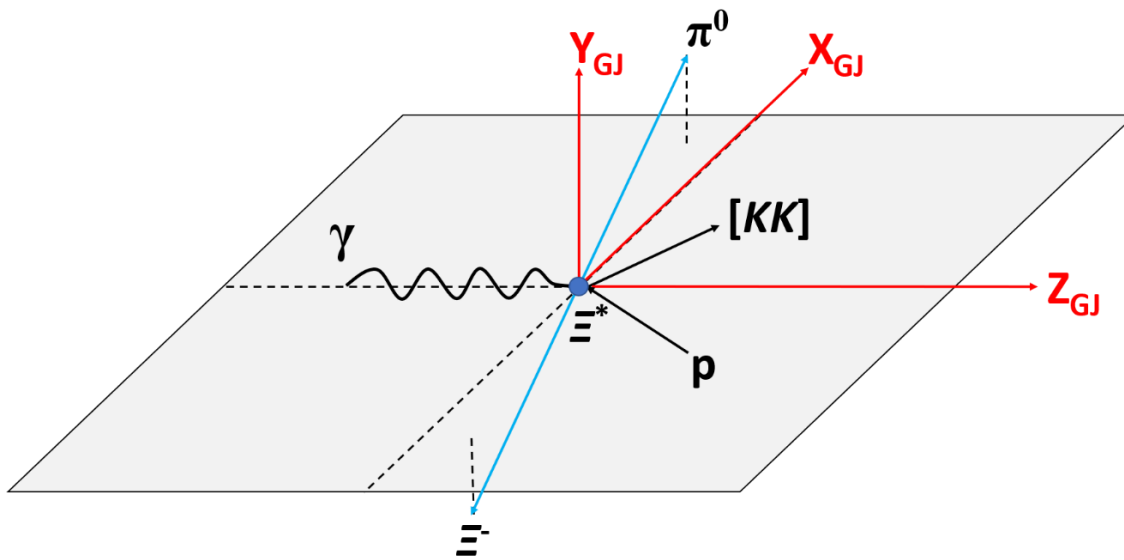
- The  ${}^i A_b(\tau)$  terms are the decay amplitudes where  $i$  represents the initial state,  $b$  represents the set of possible quantum numbers  $(J, l, m)$  and  $\tau$  represents all phase space and  $\rho$  is the final state spin density matrix

# Choice of frame

- The choice of frame is the GJ frame.



# Choice of frame



- The  $z$ -axis points in the direction of the initial photon beam

$$\hat{z}_{GJ} = \frac{\vec{p}_\gamma(\mathcal{E}^*)}{|\vec{p}_\gamma(\mathcal{E}^*)|}$$

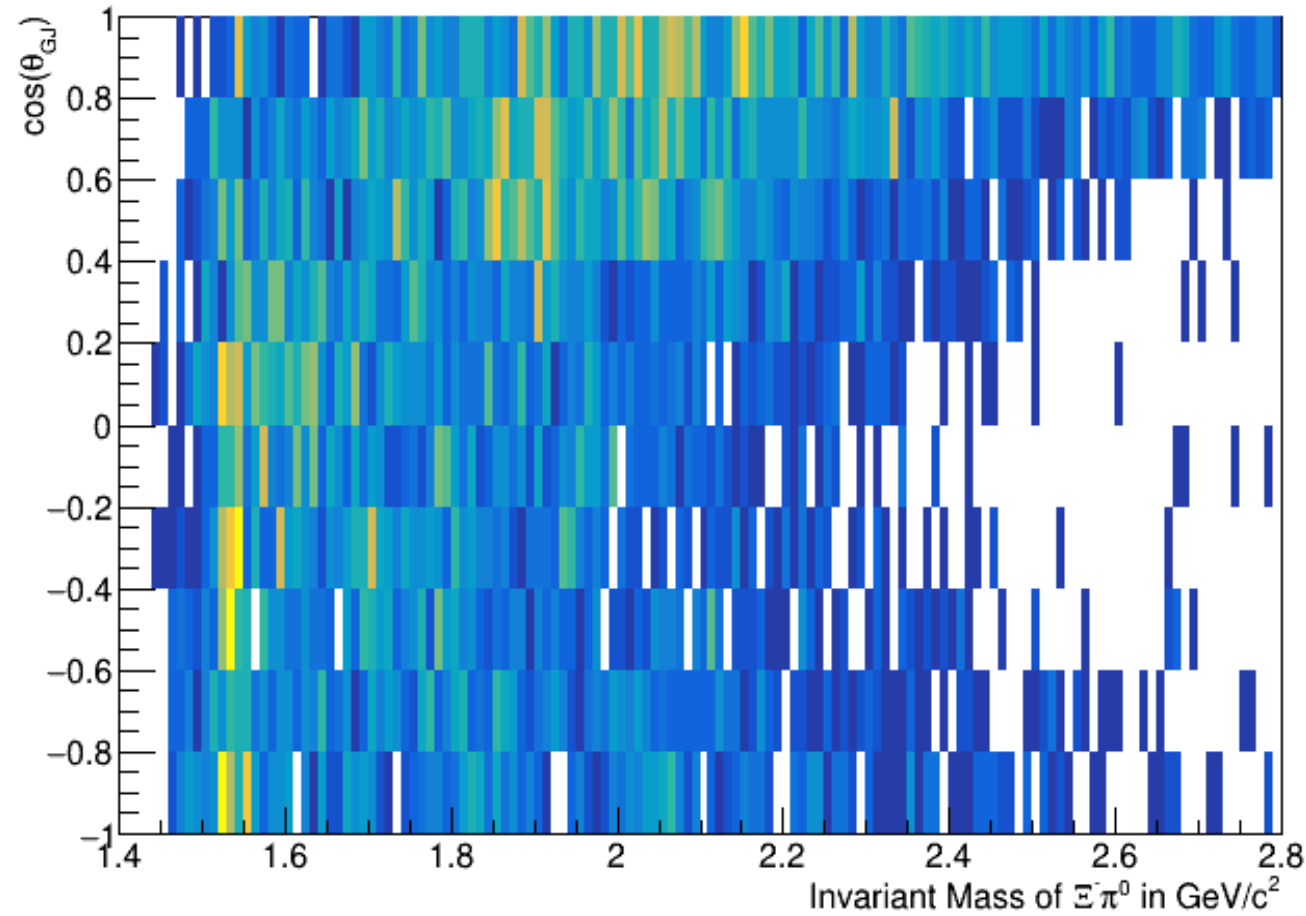
- The  $y$ -axis is defined to be the normal to the production plane of  $\mathcal{E}^*$  in the CM frame.

$$\hat{y}_{GJ} = \frac{\vec{p}_\gamma \times \vec{p}_{\mathcal{E}^*}}{|\vec{p}_\gamma \times \vec{p}_{\mathcal{E}^*}|}$$

- The  $x$ -axis is defined by making the coordinate system right-handed:

$$\hat{x}_{GJ} = \hat{y}_{GJ} \times \hat{z}_{GJ}.$$

# $\cos\theta_{GJ}$ versus invariant mass of $\Xi^-\pi^0$



# Decay amplitudes

- The full expression for a decay amplitude in the GJ frame is:

$$A_b(\tau) = \sqrt{\frac{2l+1}{4\pi}} F_l(p) a_{ls} \sum_{\lambda_1 \lambda_2} D_{m\lambda}^{J*}(\Omega_{GJ}) \langle l0s\lambda | J\lambda \rangle \langle s_1 \lambda_1 s_2^{-\lambda_2} | s\lambda \rangle.$$

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$$A_b(\tau) = \sqrt{\frac{2l+1}{4\pi}} \underbrace{F_l(p)}_{\text{Blatt-Weisskopf centrifugal-barrier factor}} a_{ls} \sum_{\lambda_1 \lambda_2} D_{m\lambda}^{J*}(\Omega_{GJ}) \langle l0s\lambda | J\lambda \rangle \langle s_1 \lambda_1 s_2^{-\lambda_2} | s\lambda \rangle.$$

Blatt-Weisskopf centrifugal-barrier factor dependent on angular momentum  $l$

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Fit parameter that house unknown transition amplitudes



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Wigner-D functions

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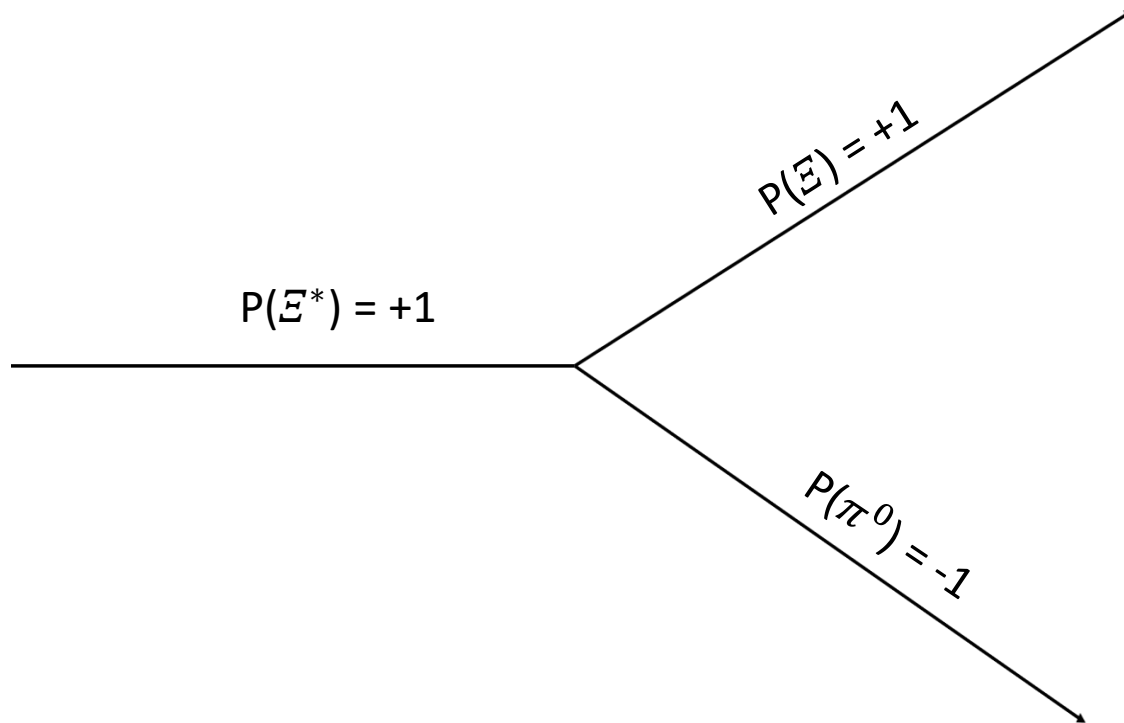
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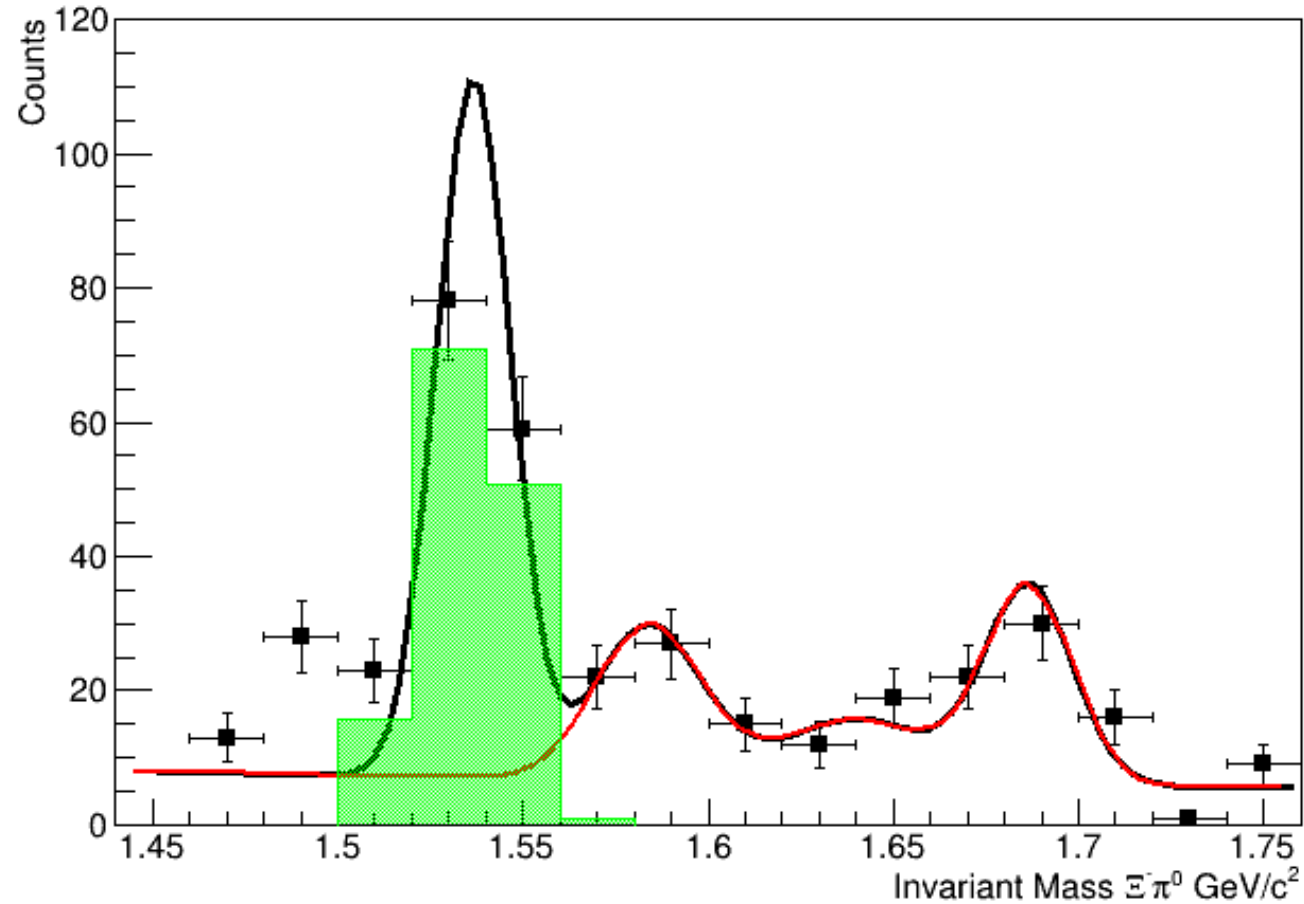
- This term always equals one because the excited cascade decays into a spin 1/2 baryon and pseudo-scalar meson

# Parity conservation

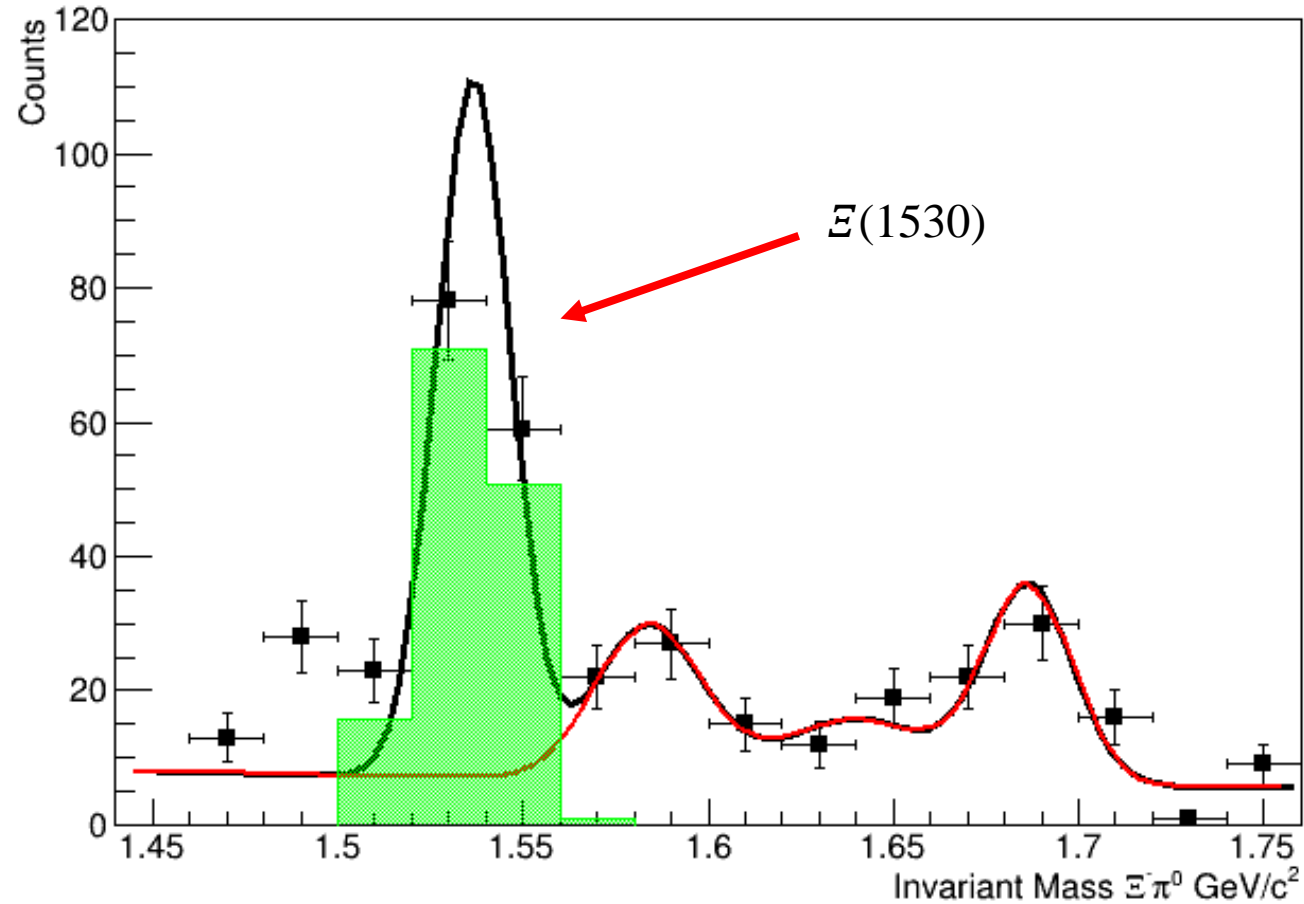


- The overall parity sign must be the same before and after the  $E(1530)$  decay because the strong interaction conserves parity
- The parity of angular momentum eigenstates is  $(-1)^l$
- Therefore  $l = 1$

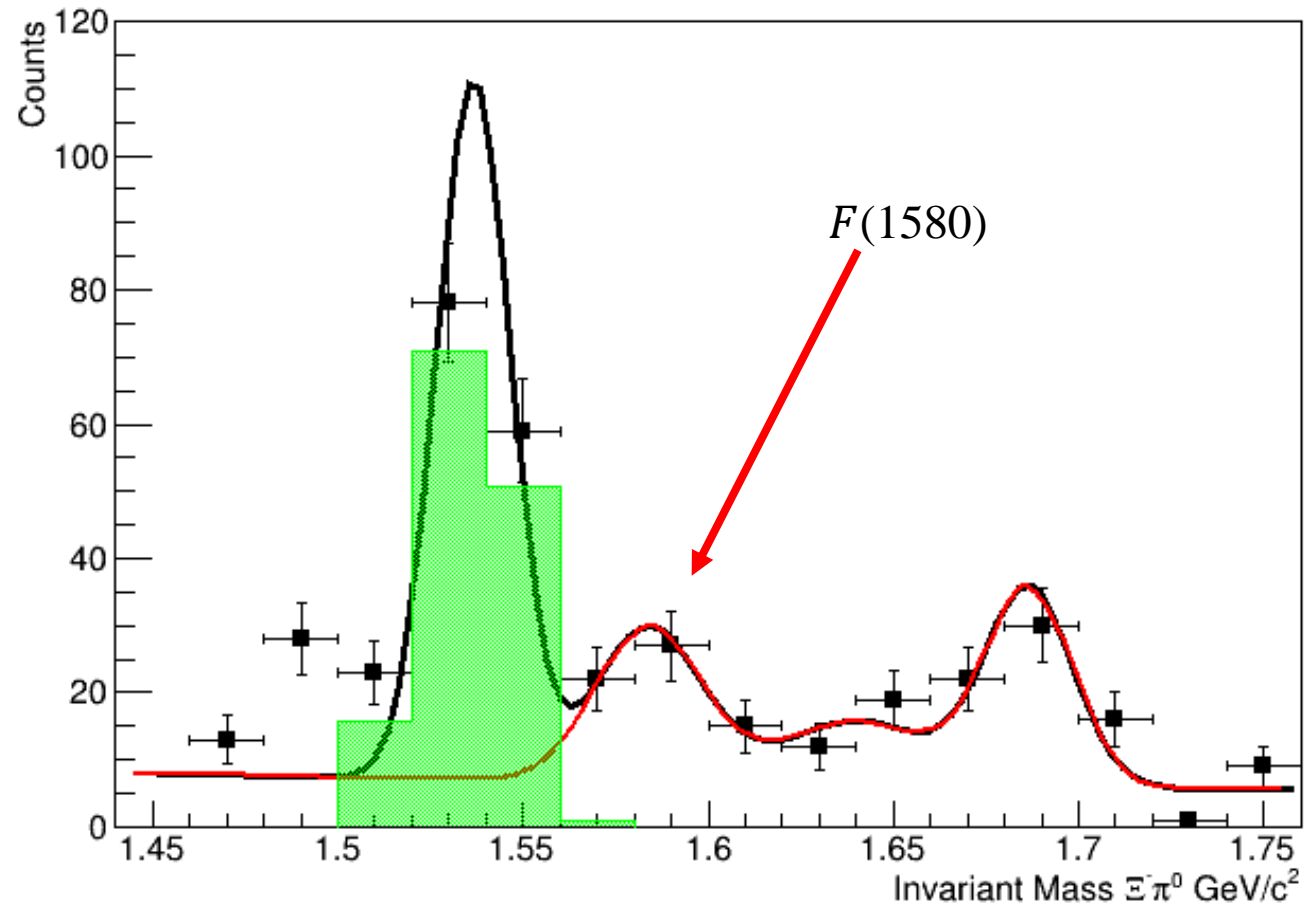
# Invariant mass Distribution of $\Xi^{*-}$ with $\cos\theta_{GJ}$ , between $-1.0$ and $-0.8$



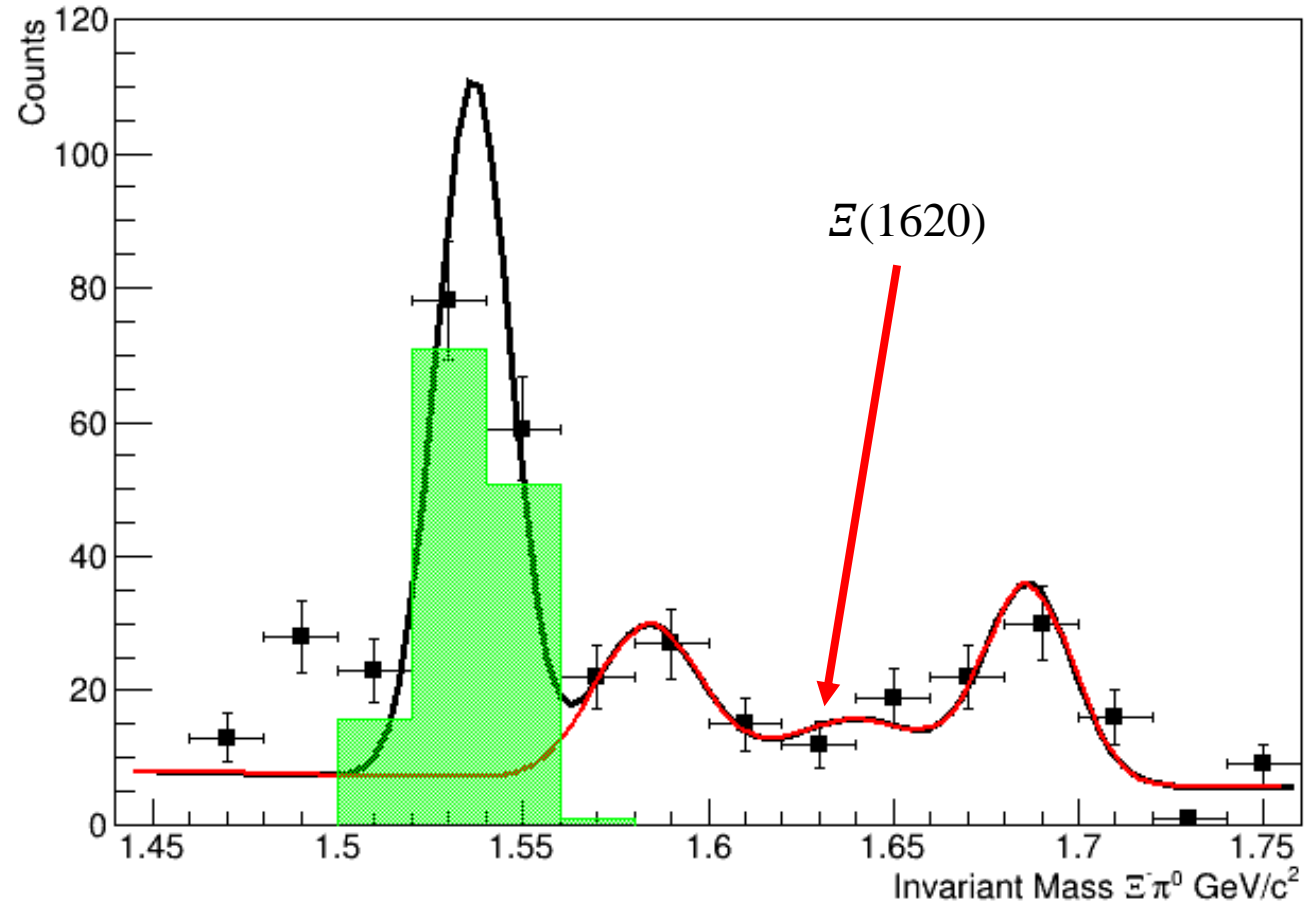
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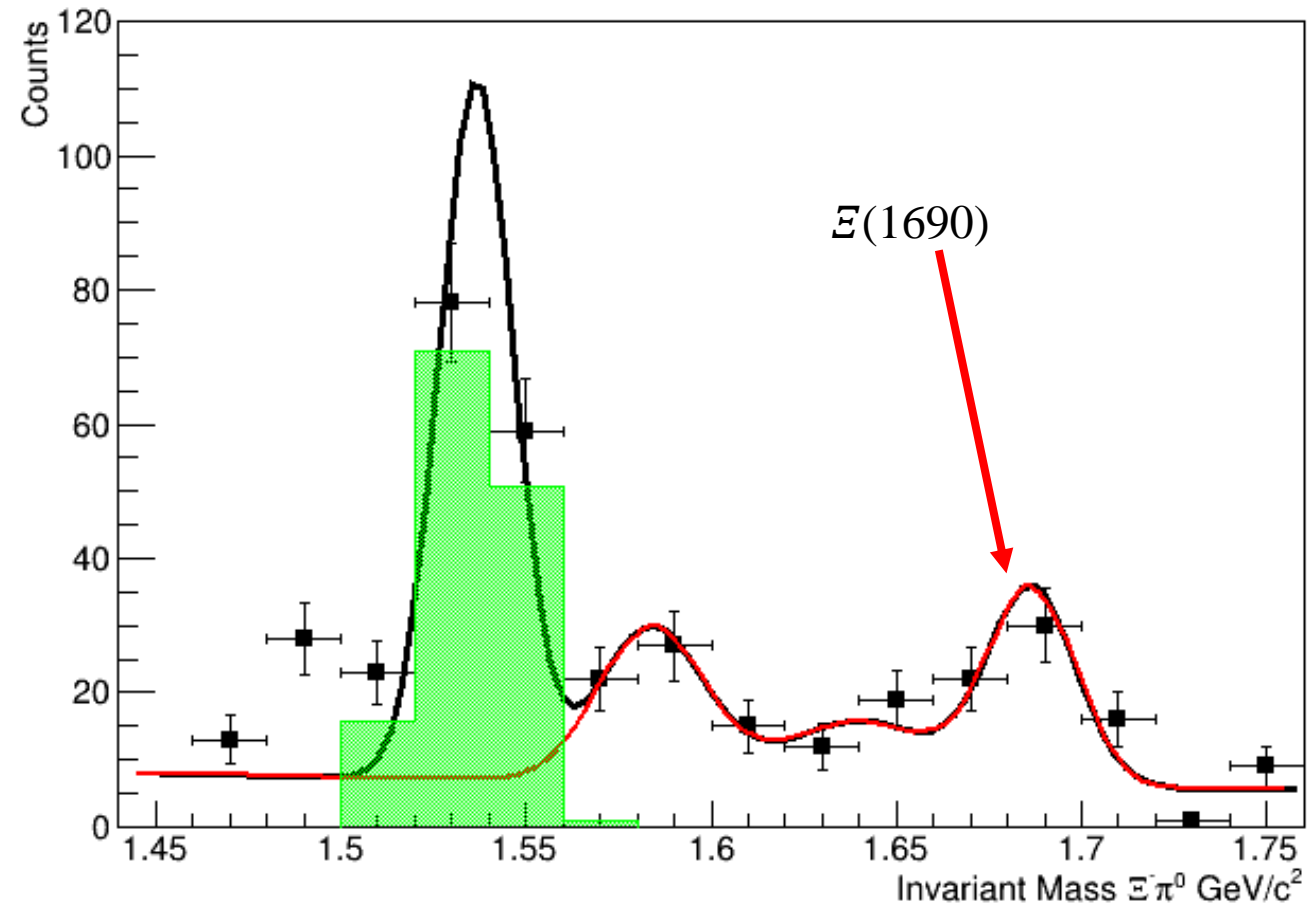


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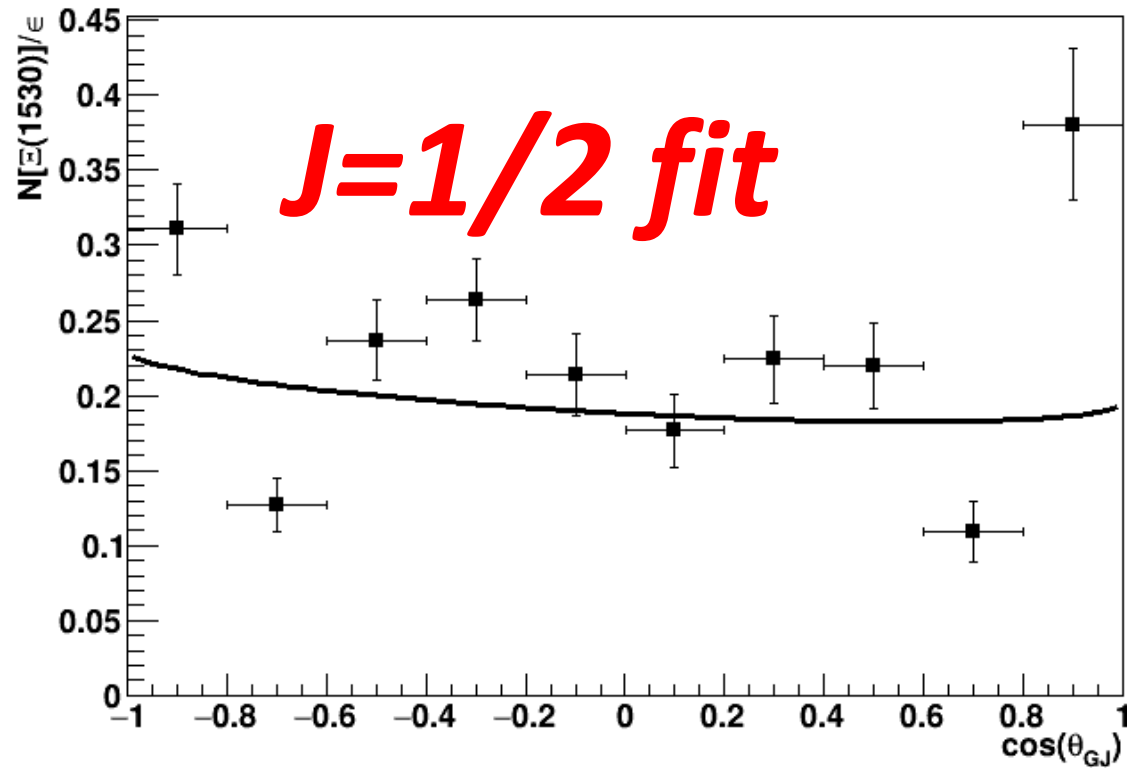


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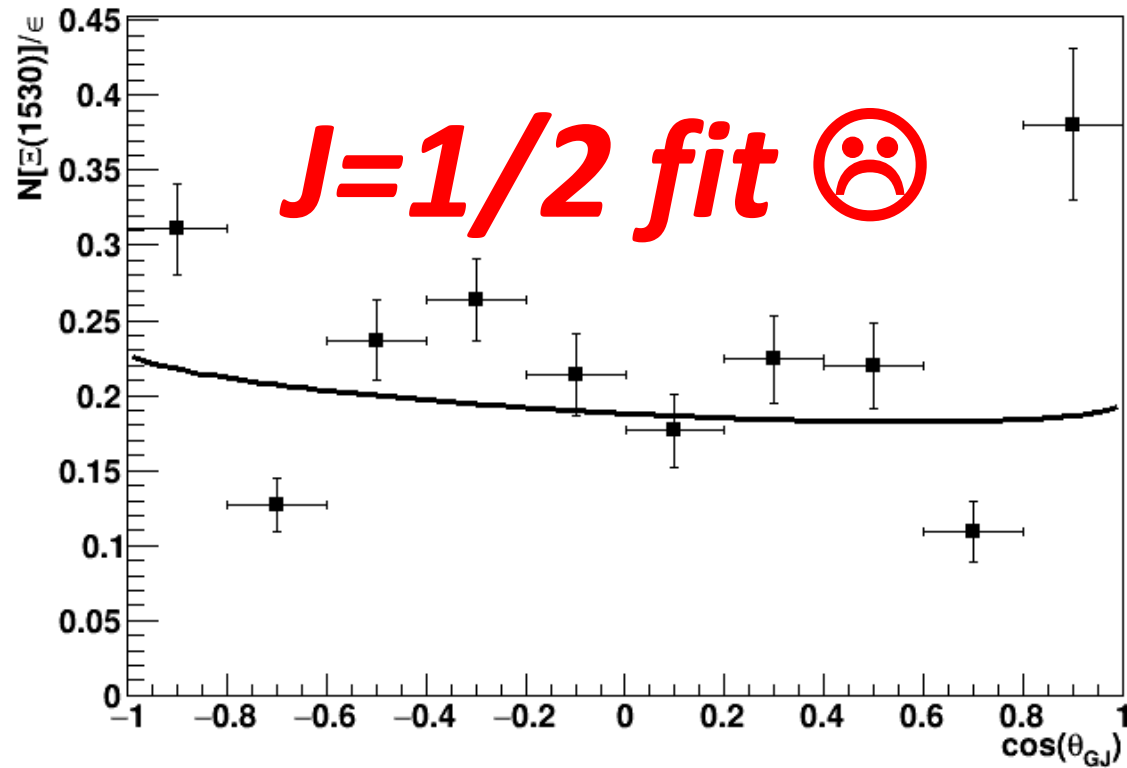




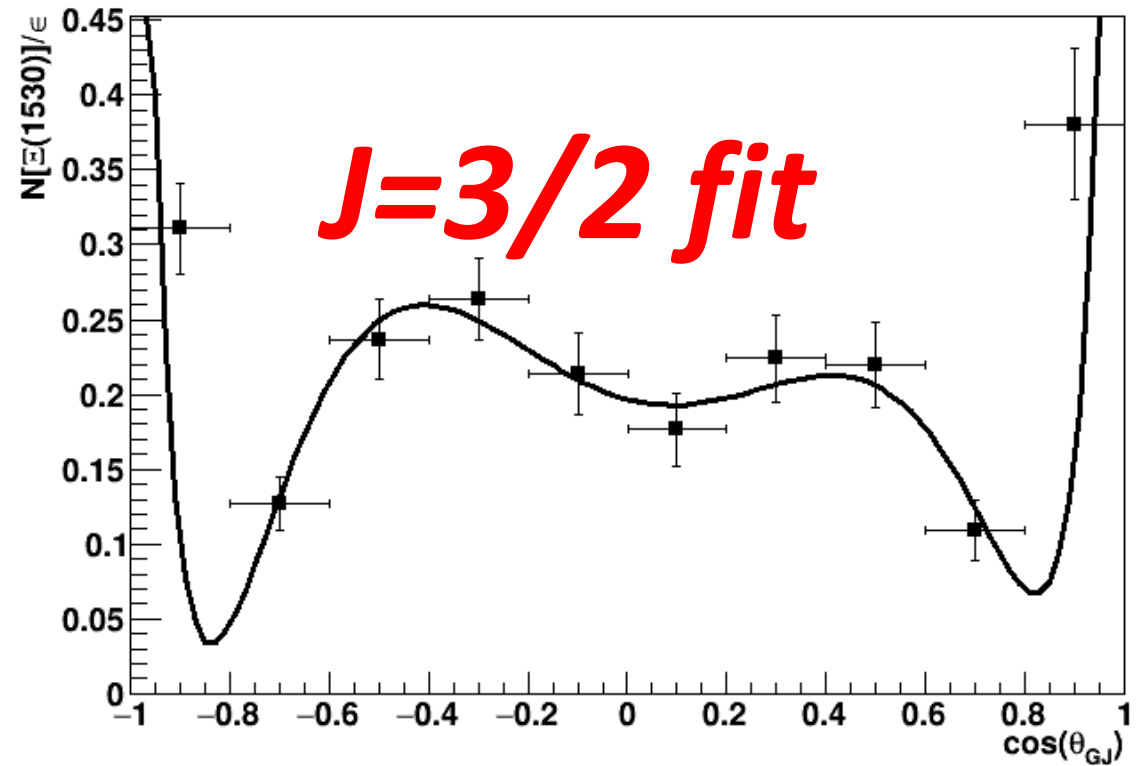
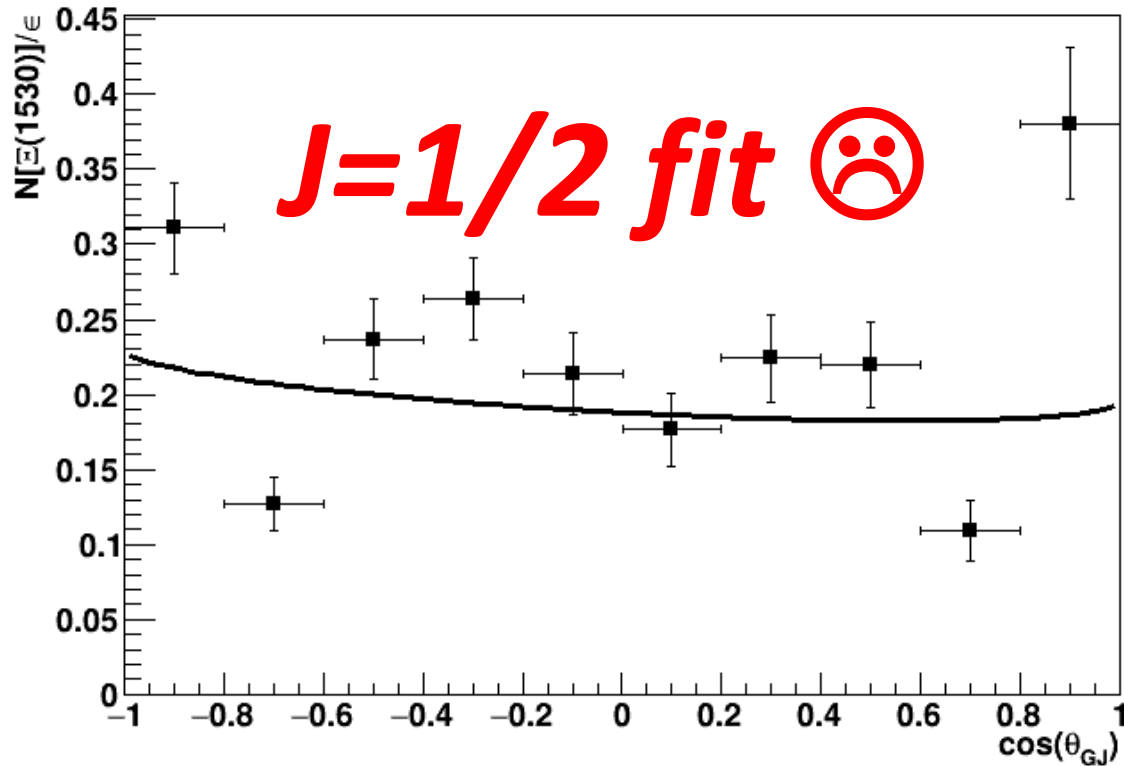
# Normalized Yield Fits



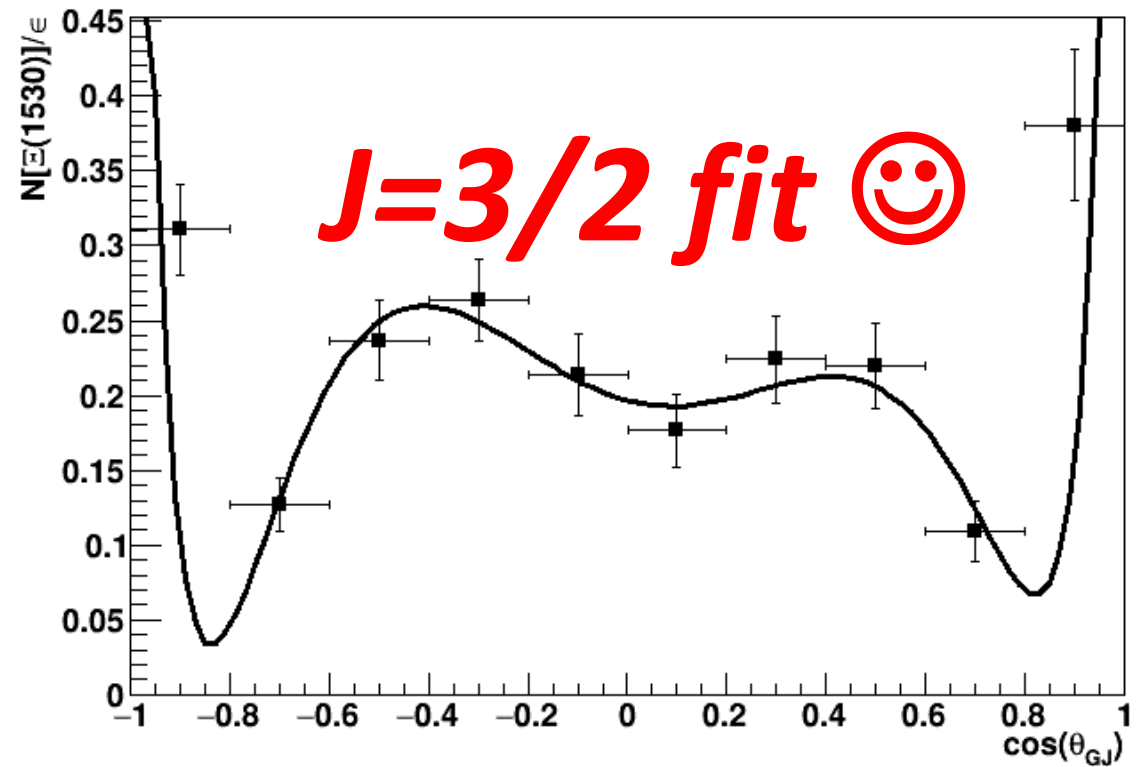
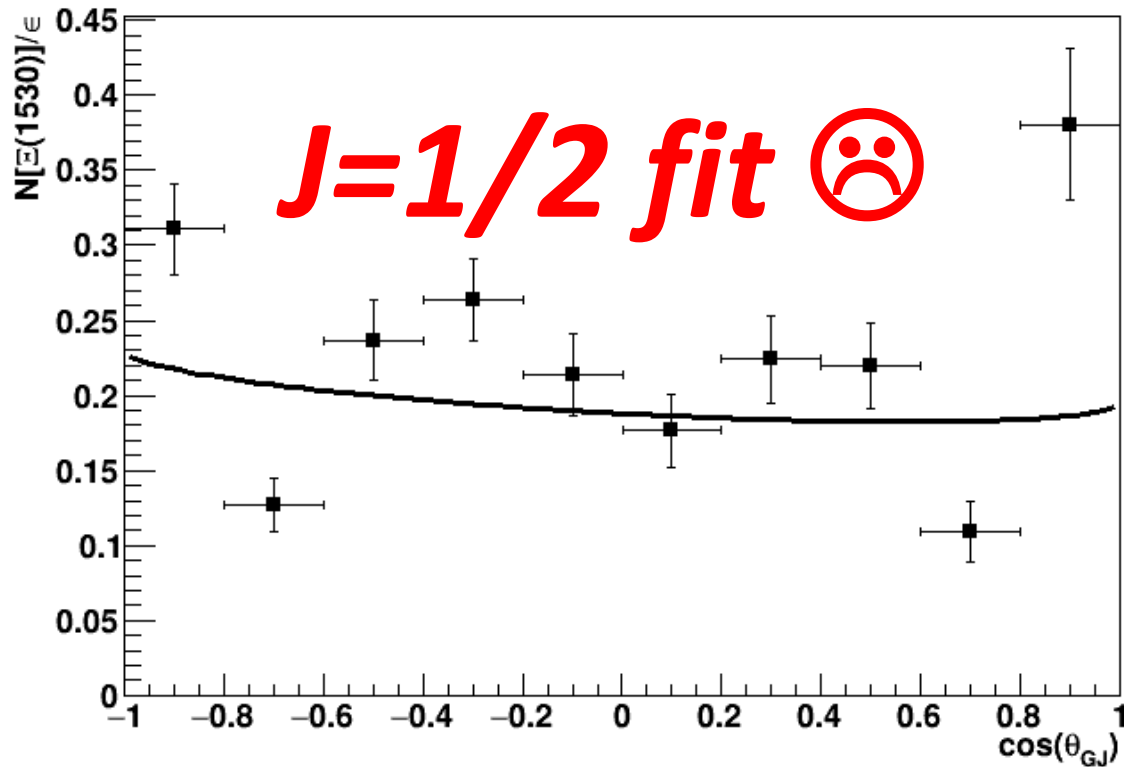
# Normalized Yield Fits



# Normalized Yield Fits



# Normalized Yield Fits



# The End

## THANK YOU !!!!!

